# FOUR-BODY $\boldsymbol{d}+\boldsymbol{d}$ REACTION AT $46.7 \mathrm{MeV}^{*}$ 

B. Struzhko

Institute for Nuclear Researches of the Ukrainian Academy of Science Kyiv, Ukraine

(Received December 31, 1998)

Two-dimensional proton-proton ( $p p$ ) and proton-proton-neutron ( $p p n$ ) coincidence spectra from $\mathrm{d}+\mathrm{d}$ reaction were calculated, taking into account quasi free scattering (QFS) of protons and final state interaction (FSI) of neutron-proton pairs. Deuteron beam energy $E_{0}=46.7 \mathrm{MeV}$, proton emission angles $\vartheta_{1}=\vartheta_{2}=38.75^{\circ}, \varphi_{1}-\varphi_{2}=180^{\circ}$ and a neutron one $\vartheta_{n}=0^{\circ}$ are the pp QFS kinematic conditions. The results are compared to appropriate experimental data. Contribution from singlet deuterons disintegration seems to prevail in coincidence spectra and about one fourth part of all coincidence events is from pp QFS.

PACS numbers: 24.10.-i, 24.10.Cn

Some researches of four-body $d+d$ reaction are known at present [1-6]. It was found that quasi free scattering (QFS) and final state interaction (FSI) processes are important. Neutron-neutron ( $n n$ ) and proton-proton ( $p p$ ) FSI effects were observed in experiments [1,2]. QFS of protons was identified in the proton-proton-neutron ( $p p n$ ) coincidence spectrum [6]. The increased yield of pp coincidence events was noticed at energies of pp QFS as well [36]. On the other hand, such interpretation of the double coincidence spectra cannot be only possible because $n p$ FSI processes are allowed, moreover proton angular and energy distributions from the ${ }^{2} \mathrm{H}\left(d, d^{*}\right) d^{*}$ reaction are similar to those from $p p$ QFS $[7,8]$.

In this work the attempt is undertaken to estimate the contribution of various mechanisms, simulating $p p$ and $p p n$ coincidence spectra taking into account the $n p$ FSI and pp QFS and comparing them with the experimental data [6]. Effects of the target and detector dimensions and resolutions are taken into account. Beam energy $E_{0}=46.7 \mathrm{MeV}$ and emission angles of

[^0]protons $\vartheta_{1}=\vartheta_{2}=38.75^{\circ}, \varphi_{1}-\varphi_{2}=180^{\circ}$ and a neutron one $\vartheta_{n}=0^{\circ}$ correspond to the $p p$ QFS kinematic condition. The differential cross sections of the four-particle ${ }^{2} \mathrm{H}(d, p p)$ reaction are calculated by using the prescription [7]:
\[

$$
\begin{equation*}
\frac{d^{4} \sigma\left(E_{1}, E_{2}, \vartheta_{1}, \varphi_{1}, \vartheta_{2}, \varphi_{2}\right)}{d \Omega_{1} d \Omega_{2} d E_{1} d E_{2}}=\frac{(2 \pi)^{4}}{v} \int \rho|F|^{2} \sin \vartheta d \vartheta d \varphi \tag{1}
\end{equation*}
$$

\]

$E_{1}$ and $E_{2}$ are energies of protons, $v=p_{0} / 2 m$ is a velocity of the deuteron in the beam, $\boldsymbol{p}_{0}$ is a deuteron momentum, m is the nucleon mass, $\rho$ is a phase space factor [9], $\vartheta$ and $\varphi$ are angles of a relative neutron-neutron momentum $\boldsymbol{k}_{n n}$. In calculations of the double coincidence spectrum $N_{p p}\left(E_{1}, E_{2}\right)$ an integration domain covers all possible directions $\boldsymbol{k}_{n n}$ (i.e. within of $4 \pi$ ), and for threefold coincidence $N_{p p n}$ it is defined by a solid angle of the neutron detector. Transition matrix element is approximated as a sum

$$
\begin{equation*}
|F|^{2}=c_{1}\left|F_{\mathrm{QF}}\right|^{2}+c_{2}\left|F_{\mathrm{S}}\right|^{2}+c_{3}\left|F_{\mathrm{T}}\right|^{2} \tag{2}
\end{equation*}
$$

$F_{\mathrm{S}}$ and $F_{\mathrm{T}}$ are the ${ }^{1} \mathrm{~S}_{0}$ and ${ }^{3} \mathrm{~S}_{1} n p$ FSI amplitudes, $F_{\mathrm{QF}}$ is the $p p$ QFS amplitude evaluated in the plain wave impulse approximation (PWIA) [10]:

$$
\left|F_{\mathrm{QF}}\right|^{2}=\left|\psi\left(\boldsymbol{p}_{p p} / 2-\boldsymbol{k}_{n n}\right)\right|^{2}\left|\psi\left(\boldsymbol{k}_{n n}-\boldsymbol{p}_{n n} / 2\right)\right|^{2} \frac{d \sigma_{p p}\left(k_{p p}\right)}{d \Omega} .
$$

$\boldsymbol{p}_{p p}=\boldsymbol{p}_{1}+\boldsymbol{p}_{2}, \boldsymbol{p}_{1}, \boldsymbol{p}_{2}$ are momenta of protons in the laboratory system, $\boldsymbol{p}_{n n}=\boldsymbol{p}_{0}-\boldsymbol{p}_{p p}, k_{n n}=\sqrt{m E_{n n}}, E_{n n}=E_{0}+Q-E_{1}-E_{2}-p_{n n}^{2} / 4 m$, $Q=-4.449 \mathrm{MeV}, \boldsymbol{k}_{p p}=\left(\boldsymbol{p}_{1}-\boldsymbol{p}_{2}\right) / 2, \boldsymbol{\psi}(\boldsymbol{k})$ is a Fourier component of the deuteron wave function. It is taken in the Hulthen form :

$$
\psi(r)=\frac{\sqrt{a b(a+b) / 2 \pi}}{a-b} \frac{\exp (-a r)-\exp (-b r)}{r}
$$

$h^{2} a^{2}=m E_{a}, E_{a}=2.2245 \mathrm{MeV}, h^{2} b^{2}=m E_{b}, E_{b}=59.8 \mathrm{MeV}$. Calculations are carried out in the simple impulse approximation (SIA) [10, 11] and in the modified one (MIA) [12] with $R=4.6 \mathrm{fm}$ chosen.

Keeping in mind that $k_{p p}$ is rather moderate for S wave interaction to be used and rather high for Coulomb terms to be neglected the cross section of proton-proton elastic scattering is calculated as [13]:

$$
\frac{d \sigma_{p p}(k)}{d \Omega}=\frac{1}{k^{2}+\left(-1 / a+r k^{2} / 2\right)^{2}}
$$

with $a=-7.813 \mathrm{fm}$ and $r=2.78 \mathrm{fm}[14]$.
$F_{\mathrm{S}}$ and $F_{\mathrm{T}}$ terms in (2) are calculated by using the Watson-Migdal approximation:

$$
\left|F_{\mathrm{S}}\right|^{2}=\left|F_{1 \mathrm{~S}}\right|^{2}\left|F_{\mathrm{SS}}\right|^{2} .
$$

$F_{1 \mathrm{~S}}$ and $F_{2 \mathrm{~S}}$ are for neutron-proton pairs emitted to the left and to the right of a beam direction,

$$
\begin{align*}
F_{1(2) \mathrm{S}}(k) & =\frac{r\left(k^{2}+\alpha^{2}\right)}{2\left(-1 / a+r k^{2} / 2-i k\right)}, \\
\alpha & =\frac{1+\sqrt{1-2 r / a}}{r}, \quad h k=\sqrt{m E_{n p}} . \tag{3}
\end{align*}
$$

The expressions for $F_{\mathrm{T}}{ }^{2}$ are similar. Parameters $a$ and $r$ are equal -23.748 and 2.75 fm for the ${ }^{1} S_{0} \mathrm{np}$ state and 5.424 and 1.759 fm for ${ }^{3} S_{1}$ [14]. As


Fig. 1. Two-dimensional $p p$ coincidence spectrum [6]
we know, at our energies SIA does not reproduce absolute values of cross sections [15], but the relative distributions of spectator momenta are consistent with experimental ones [13], so it is possible to estimate the QFS contribution to the double pp coincidence spectrum from the threefold ppn coincidence one. The experimental $p p$ coincidence spectrum is shown in the Fig. 1. Calculated cross sections and data on the cut along a diagonal $E_{1}=E_{2}$ are shown in Fig. 2. Only the first term in the sum (2) was taken into account. Calculated cross sections are multiplied with a factor
$c_{\text {norm }}=0.2$. SIA and MIA calculations without target and detector dimensions and resolutions taken into account are shown as dashed and dotted lines. Factors $c_{\text {norm }}$ are 0.2 and 1.0 respectively. Angular distribution of neutrons - 'spectators' from ${ }^{2} \mathrm{H}(d, p p n)$ reaction is strongly directed forward. Function $d N / d(\cos \vartheta) \sim 1 /\left(0.0019+\sin ^{3} \vartheta\right)$ is a good approximation for angular distribution at angles $\theta_{n}<20^{\circ}$. Equally Gaussian function $d N / d E_{n} \sim \exp \left\{-\ln 2\left(E_{0}-E_{n}\right)^{2} / H^{2}\right\}$ is a good approximation for the neutron spectrum at $\theta_{n}=0^{\circ}$ with $E_{0}=23.4 \mathrm{MeV}$ and $H=5.5 \mathrm{MeV}$. The average efficiency $\eta$ of the neutron detector is calculated with the adapted Stanton code [16]. Calculated ratio $\eta N_{p p n} / N_{p p}=0.026$, that 4 times exceeds the experimental value $0.0061 \pm 0.0007$ [6]. This result can be interpreted assuming that pp QFS contribution to the pp coincidence spectrum in Fig. 1 really exists but amounts only to about quarter of all events. By the way the value $c_{\text {norm }} / 4=0.05$ almost coincides with a factor 0.049 obtained for ${ }^{3} \mathrm{He}\left({ }^{3} \mathrm{He}, d d\right) p p$ reaction at beam energy $50 \mathrm{MeV}[10]$.


Fig. 2. Simulated cross sections for pp QFS and data along the diagonal $E_{1}=E_{2}$. Dashed and dotted lines are SIA and MIA calculations for dot geometry and ideal resolution.

Simulated spectrum with all three amplitudes in the sum (2) taken into account is given in Fig. 3. The fitting area in a plane $E_{1}-E_{2}$ is bounded with thresholds $E_{1}, E_{2}=7.8 \mathrm{MeV}$ and four-body limit of the $d+d \rightarrow p+p+n+n$ reaction and contains $m=2694$ elements $N_{i j \exp }$ of an experimental matrix with errors $d N_{i j \exp }$ and simulated ones $N_{i j \operatorname{sim}}$. The value

$$
\chi^{2}=\frac{1}{m-3} \sum \frac{\left(N_{i j \exp }-N_{i j \operatorname{sim}}\right)^{2}}{d N_{i j \exp }^{2}}
$$



Fig. 3. Simulated pp coincidence spectrum with pp QFS and np FSI amplitudes taken into account. Fitting with the least squares method.


Fig. 4. Cuts of surfaces in Fig. 1 and 3 along a diagonal $E_{1}=E_{2}$. Dasheddotted, dashed and dotted lines are for the pp QFS (SIA), singlet and triplet $n p$ FSI respectively and solid line is their total contribution.
has appeared to be equal 1.5 , and ratio of contributions from the separate terms in (2) on this area is $(0.20 \pm 0.04):(0.65 \pm 0.07):(0.15 \pm 0.03)$ in agreement with the value $N_{p p n} / N_{p p}$. Calculated cross sections and data [6] on the cut along $E_{1}=E_{2}$ are shown in Fig. 4. The dash-dotted, dashed
and dotted lines show the QFS component and FSI ones for ${ }^{1} S_{0}$ and ${ }^{3} S_{1} n p$ states, respectively. So in an incomplete ${ }^{2} \mathrm{H}(d, p p)$ experiments FSI effects are rather essential even at angles of $p p$ QFS. It should be taken into account in interpretation of the data [3-6], and in the projects of future experiments.

I am grateful to the computer center staff and my colleagues I. Drjapachenko, Val. Pirnak, Vit. Pirnak, O. Povoroznyk, A. Ustinov for help in carrying out the investigation and preparing this manuscript.

## REFERENCES

[1] R.E. Warner, S.B. Dicenzo, G.C. Ball et al., Nucl. Phys. A243, 189 (1975).
[2] Y-J. Zhang, J-Q. Yang, J. Zhang, J-H. He, Phys. Rev. C45 528 (1992).
[3] B.Th. Leeman, M.G. Pugh, N.S. Chant et al., Phys. Rev. C17 410 (1978).
[4] N. Koori, T. Ohsawa, S. Seki et al., Phys. Rev. C31, 246 (1985).
[5] L.A. Golovach, V.I. Grantcev, V.V. Zerkin et al., Izvestija AN USSR, physical series, 51, 166 (1987).
[6] V.I. Konfederatenko, Vit.M. Pirnak, V.A. Pylypchenko et al., Ukrainian Physical Journal 42, 1175 (1997).
[7] R.E. Warner, Phys. Rev. C24, 2759 (1981).
[8] B. Struzhko, Ukrainian Physical Journal, 1998, to be published.
[9] M. Furic, H.H. Forster, Nucl. Instrum. Methods Phys. Res. 98, 301 (1972).
[10] R.G. Allas, L.A. Beach, R.O. Bondelid et al., Nucl. Phys. A304, 461 (1978).
[11] I. Slaus, R.G. Allas, L.A. Beach et al., Nucl. Phys. A286, 67 (1977).
[12] G. Paic, J.C. Koung, O.J. Margaziotis, Phys. Lett. B32, 437 (1970).
[13] W. Kluge, Fortscritte der Physik, 22, 691 (1974).
[14] R. Machleidt, Adv. Nucl. Phys. 19, 189 (1989).
[15] Ian H. Sloan, Phys. Rev. 185, 1361 (1969).
[16] R.A. Cecil, B.D. Anderson, R. Madey, Nucl. Instrum. Methods Phys. Res. 161, 439 (1979).


[^0]:    * Presented at the International Conference "Nuclear Physics Close to the Barrier", Warszawa, Poland, June 30-July 4, 1998.

