# SHAPE TRANSITION AND COLLECTIVE DYNAMICS IN EVEN 94-100Zr NUCLEI

J. Skalski<sup>1,2</sup>, P.-H. Heenen<sup>2</sup>, P. Bonche<sup>3</sup> and H. Flocard<sup>4</sup>

(1) Soltan Institute for Nuclear Studies, PL- 00 681, Warsaw, Poland (2) SPhNT U.L.B - C.P. 229 - 1050 Brussels, Belgium (3) SPhT CEN Saclay - 91191 Gif sur Yvette Cedex, France (4) DPhT 5, IPN - 91406 Orsay Cedex, France

## ABSTRACT

Quadrupole and octupole excitations in even 94-100 Zr nuclei are studied within the fully microscopic generator coordinate method using a basis generated by the selfconsistent Hartree-Fock method. Results relevant for the A=100 shape transition and for the octupole mode propertis are reported.

# 1. Introduction

The isotopic chain of neutron rich zirconium nuclei offers an example of a very rapid spherical to deformed shape transition: 96Zr shows features typical of a spherical nucleus while the isotope 100Zr has already one of the largest known ground state deformations,  $\beta_2 \approx 0.35$  [1] 6. There are also other unusual and interesting properties of these isotopes: 1) Shape coexistence - found in 98,100 Zr by extensive experimental studies, in particular, of low lying excited 0+ states (see refs. [2,3,4] and references quoted therein). 2) The enhanced "sphericity" of 96Zr with respect to the expected trend of losing spherical properties when going from the magic 90Zr towards larger neutron numbers [3]. Since semimagic properties of Z=40 are neutron number dependent (e.g. enhanced in 96Zr by a large 2d<sub>5/2</sub>-3s<sub>1/2</sub> neutron subshell spacing) the special role of the neutron-proton interaction was suggested to explain the latter effect [5]. 3) Relatively low lying 3- states in 92-98Zr nuclei and unusually large  $B(E3,3^- \rightarrow 0^+)$  value of  $65(\pm 10)$  W.u. in <sup>96</sup>Zr [6], the largest B(E3) known.

A correct theoretical description of these data is difficult both due to frequently encountered troubles with the reproduction of single particle spectrum in A≈100 Zr nuclei by phenomenological potentials [7,8] or within the Hartree-Fock+BCS (HFBCS) method [9,10] and to the necessity of going beyond the static models, i.e., beyond the Strutinsky or HFBCS methods. Motivated especially by the latter point, we have used in the recent work [11] the fully microscopic generator coordinate method (GCM) based on the selfconsistent HF approach with the Skyrme force SkM\* to describe the properties of 94-100Zr nuclei.

### 2. Method

As described in detail in the ref.[12], our GCM calculations start from the generation of the HFBCS states  $|\Phi(q_i)\rangle$ , having prescribed quadrupole/octupole moments. The GCM eigenstates  $|\Psi_k\rangle$  result then from the diagonalization of the hamiltonian <sup>7</sup> within the nonorthogonal basis of HFBCS states  $|\Phi(q_i)\rangle$  corresponding to different

<sup>&</sup>lt;sup>5</sup>Unité de recherches des Universités Paris XI et Paris VI associée au C.N.R.S..

<sup>&</sup>lt;sup>6</sup> An equally sharp shape transition is observed in Sr isotopes, while it becomes smooth in Mo, Ru and Pd elements.

<sup>7</sup>the same as the one used in the generation of HFBCS states.

$$|\Psi_k\rangle = \sum_{q_i} f(q_i) |\Phi(q_i)\rangle. \tag{1}$$

Quadrupole shapes are described by the quadrupole moment,  $Q = \langle 2z^2 - x^2 - y^2 \rangle$ , and triaxiality  $\gamma$ . For such a shape we include its six orientations resulting from a relabelling of the principal axes of the nucleus. Working in so enlarged GCM basis we classify the GCM solutions according to the irreps of the group of permutations of three coordinate axes,  $S_3$ . This corresponds to a partial angular momentum projection [13]. Within this approach, the  $0^+$  and  $2^+$  states are represented by: the symmetric irrep containing all the I=0, and parts of the I=4 and  $I\geq 6$  components, and the two-dimensional irrep containing all the I=2 and I=5, and parts of the I=4 and I>6 components, respectively.

Separately, we study negative parity excitations introducing axial octupole deformation by means of the constraint on the octupole moment,  $q_3 = \langle r^3 Y_{30} \rangle$ , of

the HFBCS states [14].

# 3. Results

From the previous HF study of the A=80 and A=100 deformed regions [10] it is clear that with the the Skyrme force SIII one cannot account for any spherical-prolate shape coexistence in  $^{98,100}$ Zr nuclei. We have found that the SkM\* interaction [15] is better for the A≈100 Zr nuclei, in particular, its spherical spectrum is much closer to experimental suggestions. In the pairing channel we use the spin singlet pairing generated by the zero-range  $\delta$  interaction,  $V_0^r/4(1-\sigma_1\sigma_2)\delta(\mathbf{r}_1-\mathbf{r}_2)$ , as described in the ref.[16]. This pairing interaction is state dependent, i.e., weaker between spatially different orbitals. The particle number projection (PNP) has been included in order to eliminate any smoothing of nuclear properties depending on particle numbers.

The obtained HF energy maps, Fig. 1, show that <sup>94,96,98</sup>Zr nuclei all have spherical minima with quadrupole softness increasing with A. The prolate secondary minimum around Q=8b appears in <sup>98</sup>Zr, 600 keV above the spherical one. In <sup>100</sup>Zr the deformed minimum, around 9b, becomes the absolute one, with the spherical point 1.65 MeV above. Along the prolate axis the minimum and the spherical point are separated by a small barrier, which can be bypassed via nonaxial shapes. The spherical point is not a minimum; the secondary oblate minimum appears instead. The obtained static HF results well agree with the known behaviour of zirconium isotopes.

Some results of GCM calculations in the Q- $\gamma$  coordinates are compared to the experimental data in Table 1. As seen there, the agreement with experiment is much harder to obtain within the full dynamical calculation. The typical shell model configurations in  $^{94}$ Zr are not reproduced within the GCM and the stiffnes against the quadrupole deformations seems to be overestimated. The calculated  $0^+_2$  energy in  $^{96}$ Zr is not far from the experimental one and this GCM state has substantial deformed components, as required by experiment. The first  $2^+$  state is much worse reproduced. In  $^{98}$ Zr, the GCM candidate for the first excited  $0^+$  state is deformed, so it could correspond nicely to the coexisting deformed band head. However, the GCM energy of the lowest  $2^+$  state and the  $\rho_{12}$  values, increasing rapidly at A=98, signal a problem of this calculation: the prominent shape coexistence pattern is predicted at A=98 instead of A=100. Indeed, the energy difference between the competing HF minima is the smallest for A=98. Therefore, the coexisting states can strongly mix and the large E0 strength occurs two mass units too early [17]. The first, mainly prolate, GCM  $2^+$  state in  $^{100}$ Zr is degenerated with the ground state, which is not too bad representation of a rotational  $2^+_1$  state in a GCM calculation.

The 0½ state comes out too high, as expected from what was said about 98Zr results.

The calculated GCM octupole energy in 94Zr, 3.0 MeV, is much too high. We have quite good agreement beteen the calculated and experimental 3- energies in 96,98Zr, and we predict very high, more than 3.9 MeV, octupole energy in 100Zr. The most disturbing are the predicted B(E3) values which persistently come out eight times smaller than the one measured in 96Zr. This is, in fact, independent of the forces used.

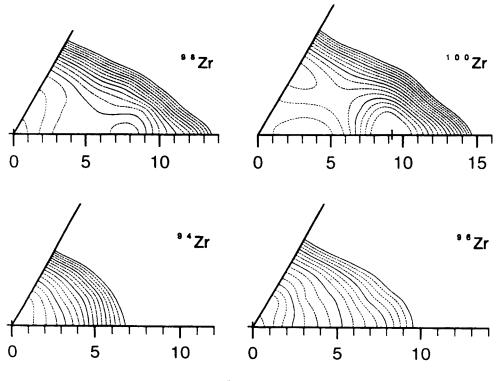


Figure 1

The HF energy, including PNP, of  $^{94-100}$ Zr in the Q- $\gamma$  plane ( $\beta_2 \approx 0.2$  at Q=5b) obtained with the Skyrme interaction SkM\* and the state dependent pairing generated by the  $\delta$  interaction with the strength  $V_0=240$  MeV for  $^{94,96}$ Zr and  $V_0=270$  MeV for  $^{98,100}$ Zr, both for neutrons and protons. The contour spacing is 250 keV.

One can hope that the full angular momentum projection which should be employed in this kind of analysis will solve some of the encountered descrepancies.

Acknowledgements One of the authors (J.S.) expresses his thanks to the staff of SPhNT of Université Libre de Bruxelles for the hospitality extended to him during his stay there. Partial support of the ULB in computation is also acknowledged.

Table 1

Nucleus	I*	E <sub>esp</sub> [MeV]	E <sub>GCM</sub> [MeV]	$\rho_{exp}^2 \times 10^3$	$\rho_{GCM}^2 \times 10^3$
94Zr	0+	1.300	2.54	11.9	37
	2+	0.919	1.35	-	
<sup>96</sup> Zr	0+	1.582	1.83	7.4	32
	2+	1.750	1.25	-	-
<sup>98</sup> Zr	0+	0.854	1.03	10	114
	2+	1.223	0.64	-	-
100Zr	0+	0.331	0.99	92	118
	2+	0.212	0.03	-	-

Experimental energies of the first excited  $0^+$  and  $2^+$  states and E0 strength  $\rho_{12}^2(0_2^+ \to 0_1^+) \times 10^3$  values (from refs.[2,17]) are given vs. corresponding GCM results from the Q- $\gamma$  calculation with parameters given in the figure caption.

# REFERENCES

- M. A. C. Hotchkis et al., Phys. Rev. Lett. 64 (1990) 3123; Nucl. Phys. A 530 (1991) 111
- 2. H. Mach et al., Phys. Lett. B 230 (1989) 21
- 3. G. Molnár et al., Nucl. Phys. A 500 (1989) 43
- 4. H. Mach et al., these proceedings
- P. Federman and S. Pittel, Phys. Lett. B 89 (1977) 385; Phys. Rev. C 20 (1979) 820
- H. Mach et al., Phys. Rev. C 42 (1989) 811
- 7. D. Galeriu, D. Bucurescu and M. Ivacscu, J. of Phys. G 12 (1986) 329
- 8. W. Nazarewicz and T. Werner, in Proc. Int. Workshop on nuclear structure in the zirconium region, Bad Honnef, FRG, 1988, ed. K. Sistemich, J. Eberth and R. A. Meyer (Springer, Berlin, 1988) p. 277
- 9. F. Tondeur, Nucl. Phys. A 359 (1981) 278
- 10. P.Bonche et al., Nucl. Phys. A 443 (1985) 39
- 11. J. Skalski, P.-H. Heenen, P. Bonche and H. Flocard, to be published
- 12. P. Bonche et al., Nucl. Phys. A 510 (1990) 466
- P. Bonche, J. Dobaczewski, H. Flocard and P.-H. Heenen, Nucl. Phys. A 530 (1991) 149
- 14. P.Bonche et al., Phys. Rev. Lett. 66 (1991) 876
- J. Bartel et al., Nucl. Phys. A 386 (1982) 79
- 16. S. J. Krieger et al., Nucl. Phys. A 517 (1990) 275
- 17. K. Heyde and R. A. Meyer, Phys. Rev. C 37 (1988) 2170