

# CONSTRAINING THE SNEUTRINO MASS IN CHARGINO PRODUCTION AND DECAY WITH POLARIZED BEAMS\* \*\*

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Production and decay of gaugino-like charginos are crucially determined by sneutrino exchange. Therefore we study the pair production of charginos  $e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-$  with polarized beams and the subsequent decay  $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 e^- \bar{\nu}_e$ , including the complete spin correlations between production and decay. The spin correlations have strong influence on the decay angular distribution and on the corresponding forward-backward asymmetry. We show for two representative scenarios for  $\sqrt{s} = 270$  GeV and for  $\sqrt{s} = 500$  GeV that forward-backward asymmetries for polarized beams are an important tool for constraining the sneutrino mass  $m_{\bar{\nu}_e}$ .

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## 1. Introduction

The search for supersymmetry (SUSY) is one of the main goals of the present and future colliders. In particular an  $e^+e^-$  linear collider will be an excellent discovery machine for SUSY particles [1]. Among them the charginos — mixtures of  $W$ -inos and charged higgsinos — are of particular interest. They belong to the lightest SUSY particles and are produced with large cross sections if kinematically accessible. Their properties depend on the SU(2) gaugino mass  $M$ , the higgsino mass parameter  $\mu$  and the ratio  $\tan\beta = v_2/v_1$  of the vacuum expectation values of the two neutral Higgs fields.

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A number of studies addressed the determination of these fundamental SUSY parameters from chargino production at  $e^+e^-$  colliders [2–4]. Recently a procedure was proposed to determine the parameters  $M$ ,  $\mu$  and  $\tan\beta$  independently from the decay dynamics [5]. For this, however, one has to assume that the selectron sneutrino mass  $m_{\tilde{\nu}_e}$  is already known, *e.g.* from sneutrino pair production.

Since for gaugino-like charginos the cross section sensitively depends on the sneutrino mass the possibility to measure  $m_{\tilde{\nu}_e}$  in chargino pair production at an  $e^+e^-$  collider has also been discussed [2, 4].

In this paper we study the prospects for constraining  $m_{\tilde{\nu}_e}$  with suitably polarized beams by combining information from the cross section

$$\sigma_{e^-} = \sigma(e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-) \times BR(\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 e^- \tilde{\nu}_e) \quad (1)$$

and the forward–backward asymmetry (FB–asymmetry)

$$A_{\text{FB}} = \frac{\sigma_{e^-}(\cos\Theta_- > 0) - \sigma_{e^-}(\cos\Theta_- < 0)}{\sigma_{e^-}(\cos\Theta_- > 0) + \sigma_{e^-}(\cos\Theta_- < 0)} \quad (2)$$

of the decay lepton  $e^-$  from the decay  $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 e^- \tilde{\nu}_e$ . In Eq. (2)  $\Theta_-$  is the angle between the incoming electron beam and the outgoing  $e^-$  in the laboratory system. For constraining  $m_{\tilde{\nu}_e}$  the simultaneous polarization of both beams turns out to be very useful [6].

In Section 2 the general formalism is presented and in Section 3 the numerical results are discussed.

## 2. General formalism

The production process  $e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-$  contains contributions from  $\gamma$ ,  $Z^0$  and  $\tilde{\nu}_e$  exchange and the decay process,  $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \ell^- \tilde{\nu}_e$  ( $\tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^0 \ell^+ \nu_e$ ) contains contributions from  $W$ ,  $\tilde{\ell}_L$  and  $\tilde{\nu}_e$  exchange. These processes have been studied in [7] properly taking into account the spin correlations between chargino production and decay.

In the following the amplitude for the production (decay) of  $\tilde{\chi}_1^-$  with helicity  $\lambda_1$  is denoted by  $P^{\lambda_1}$  ( $D_{\lambda_1}$ ). All other helicity indices are suppressed. Then the amplitude of the combined process is

$$T = \Delta_{\tilde{\chi}_1^-} \sum_{\lambda_1} P^{\lambda_1} D_{\lambda_1}. \quad (3)$$

In Eq. (3)  $\Delta_{\tilde{\chi}_1^-} = 1/[p_{\tilde{\chi}_1^-}^2 - m_{\tilde{\chi}_1^-}^2 + im_{\tilde{\chi}_1^-} \Gamma_{\tilde{\chi}_1^-}]^{-1}$ ,  $p_{\tilde{\chi}_1^-}^2$ ,  $m_{\tilde{\chi}_1^-}$  and  $\Gamma_{\tilde{\chi}_1^-}$  denote the propagator, the four–momentum squared, the mass and the width of  $\tilde{\chi}_1^-$ . For this propagator we use the narrow width approximation.

The amplitude squared  $|T|^2 = |\Delta_{\tilde{\chi}_1^-}|^2 \sum_{\lambda_1 \lambda_1'} \rho_P^{\lambda_1 \lambda_1'} \rho_{\lambda_1 \lambda_1}^D$  is thus composed of the unnormalized spin density matrix  $\rho_P^{\lambda_1 \lambda_1'} = P^{\lambda_1} P^{\lambda_1'*}$  of  $\tilde{\chi}_1^-$  and the decay matrix  $\rho_{\lambda_1 \lambda_1}^D = D_{\lambda_1} D_{\lambda_1}^*$ . Interference terms between various helicity amplitudes preclude factorization into a production factor  $\sum_{\lambda_1} |P^{\lambda_1}|^2$  times a decay factor  $\sum_{\lambda_1} |D_{\lambda_1}|^2$ . For the general case  $e^+e^- \rightarrow \tilde{\chi}_i^+ \tilde{\chi}_j^-$  ( $i, j = 1, 2$ ),  $\tilde{\chi}_i^+ \rightarrow \tilde{\chi}_k^0 \ell^+ \nu_\ell$ ,  $\tilde{\chi}_j^- \rightarrow \tilde{\chi}_l^0 \ell^- \bar{\nu}_\ell$  ( $k, l = 1, \dots, 4$ ) the complete analytical formulae for polarized beams with full spin correlations between production and decay are given in [7].

### 3. Numerical results

Our study is embedded in the Minimal Supersymmetric Standard Model (MSSM) for two representative scenarios with practically the same mass of the lighter chargino and the lightest neutralino  $\tilde{\chi}_1^0$ , respectively. The two scenarios differ, however, significantly in the mixing character of the chargino.

The chargino mass eigenstates  $\tilde{\chi}_i = \begin{pmatrix} \chi_i^+ \\ \chi_i^- \end{pmatrix}$  are defined by  $\chi_i^+ = V_{i1} w^+ + V_{i2} h^+$  and  $\chi_i^- = U_{i1} w^- + U_{i2} h^-$ . Here  $w^\pm$  and  $h^\pm$  are the two-component spinor fields of the W-ino and the charged higgsinos, respectively. Furthermore  $U_{ij}$  and  $V_{ij}$  are the elements of the  $2 \times 2$  matrices which diagonalize the chargino mass matrix.

Below we give the  $W$ -ino and higgsino components of the two-component spinor field  $\chi_1^-$ . Similarly we give the components of the neutralino  $\tilde{\chi}_1^0$  in the  $B$ -ino- $W$ -ino basis ( $\tilde{B}|\tilde{W}|\tilde{H}_a^0|\tilde{H}_b^0$ ). For details see [8,9].

**Scenario A :**  $M = 152$  GeV,  $M' = 78.7$  GeV,  $\mu = 316$  GeV,  $\tan \beta = 3$ .

Here we have used the GUT relation  $M' = \frac{5}{3} M \tan^2 \Theta_W$ . This set of parameters is inspired by the low  $\tan \beta$  mSUGRA reference scenario specified in [10]. The eigenstates and the masses of the lighter chargino and of the LSP  $\tilde{\chi}_1^0$  are

$$\begin{aligned} \chi_1^- &= (-0.91|+0.42) \quad \text{and} \quad m_{\tilde{\chi}_1^-} = 128 \text{ GeV}, \\ \tilde{\chi}_1^0 &= (-0.97|+0.15|-0.15|-0.15) \quad \text{and} \quad m_{\tilde{\chi}_1^0} = 71 \text{ GeV}. \end{aligned}$$

**Scenario B :**  $M = 400$  GeV,  $M' = 95$  GeV,  $\mu = 145$  GeV,  $\tan \beta = 3$ .

Here the parameters are chosen thus that the chargino is higgsino-like with only a small gaugino component. To obtain nearly the same masses as in Scenario A and an as large as possible higgsino component for  $\tilde{\chi}_1^0$  we take

$M$  and  $M'$  as independent parameters and do not use the GUT relation between them. The eigenstates and masses are

$$\begin{aligned}\chi_1^- &= (-0.19| + 0.98) \quad \text{and} \quad m_{\tilde{\chi}_1^-} = 129 \text{ GeV}, \\ \tilde{\chi}_1^0 &= (-0.82| + 0.11| - 0.45| - 0.33) \quad \text{and} \quad m_{\tilde{\chi}_1^0} = 71 \text{ GeV}.\end{aligned}$$

In both scenarios the LSP  $\tilde{\chi}_1^0$  has a dominating B-ino component.

We vary the sneutrino mass  $m_{\tilde{\nu}_e}$  between 80 GeV and 1000 GeV. The mass of the left selectron  $m_{\tilde{e}_L}$  is determined by the relation

$$m_{\tilde{e}_L}^2 - m_{\tilde{\nu}_e}^2 = -M_W^2 \cos 2\beta. \quad (4)$$

This sum rule is independent of any assumption on the gaugino mass parameters and of the assumption of a universal scalar mass  $m_0$  [11].

The influence of spin correlations between production and decay on the decay angular distributions is strongest near threshold. Therefore numerical results are presented for energies near threshold  $\sqrt{s} = 270$  GeV and for  $\sqrt{s} = 500$  GeV.

We have calculated for longitudinally polarized beams the cross section  $\sigma_{e^-}$ , Eq. (1), and the FB-asymmetry  $A_{\text{FB}}$ , Eq. (2), of the decay electron. For the polarization of the  $e^-$  beam we assume  $P_- = \pm 85\%$  and for the polarization of the  $e^+$  beam we take  $P_+ = \pm 60\%$ . Simultaneous polarization of both beams is not only useful to enlarge  $\sigma_{e^-}$  but it can also have strong influence on  $A_{\text{FB}}$  according to the mixing character of the charginos. Since the sneutrino couples only to left-handed electrons the polarization  $P_- < 0$  ( $P_+ > 0$ ) for the  $e^-$  ( $e^+$ ) beam is favourable for studying its properties.

### 3.1. Cross sections

For the gaugino-like scenario A and  $\sqrt{s} = 270$  GeV the cross section  $\sigma_{e^-}$  is shown in Fig. 1.

For  $m_{\tilde{\nu}_e}$  between 80 GeV and 400 GeV it is very sensitive on  $m_{\tilde{\nu}_e}$ . The deep dip at  $m_{\tilde{\nu}_e} \approx 130$  GeV is due to the destructive interferences between gauge boson and slepton exchange [9, 12]. For  $m_{\tilde{\nu}_e} < m_{\tilde{\chi}_1^-}$  the cross section increases owing to the two-body decay  $\tilde{\chi}_1^- \rightarrow \tilde{\nu}_e e^-$ . However, for  $\sqrt{s} = 270$  GeV this effect is suppressed by destructive interference effects.

For higher energy  $\sqrt{s} = 500$  GeV, Fig. 2, the destructive  $Z^0$ - $\tilde{\nu}_e$  interference in production is shifted to higher  $m_{\tilde{\nu}_e}$  and the two-body decay threshold is more apparent. For values of  $m_{\tilde{\nu}_e} > 200$  GeV the cross section  $\sigma_{e^-}$  for  $\sqrt{s} = 500$  GeV is smaller than for  $\sqrt{s} = 270$  GeV.

Beam polarization has strong influence on the magnitude of  $\sigma_{e^-}$ . For  $P_- = -85\%$  and  $P_+ = +60\%$  it increases by a factor of about 3, nearly

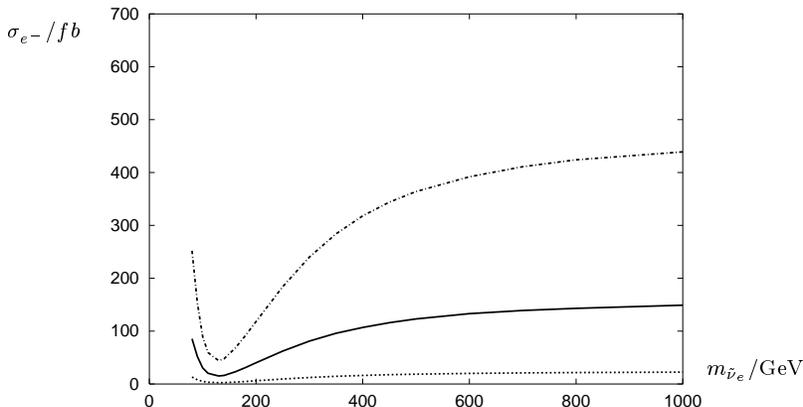


Fig. 1. Cross section  $\sigma_{e-}$  (see Eq. (1)) for  $\sqrt{s} = 270$  GeV in scenario A for unpolarized beams (solid line), with only  $e^-$  beam polarized  $P_- = +85\%$  (dotted line) and with both beams polarized  $P_- = -85\%$ ,  $P_+ = +60\%$  (dash-dotted line).

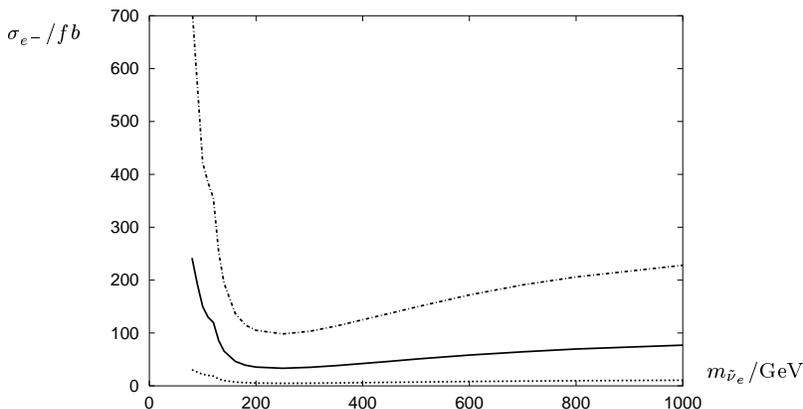


Fig. 2. Cross section  $\sigma_{e-}$  (see Eq. (1)) for  $\sqrt{s} = 500$  GeV in scenario A for unpolarized beams (solid line), with only  $e^-$  beam polarized  $P_- = +85\%$  (dotted line) and with both beams polarized  $P_- = -85\%$ ,  $P_+ = +60\%$  (dash-dotted line).

independent of  $\sqrt{s}$  and of  $m_{\tilde{\nu}_e}$ , Fig. 1 and Fig. 2. For the opposite polarization configuration,  $P_- = +85\%$ ,  $P_+ = -60\%$ , it would decrease by a factor of 0.06. If only the electron beam is polarized  $\sigma_{e-}$  increases for  $P_- = -85\%$  by a factor of 1.85 and for  $P_- = +85\%$  it decreases by a factor of 0.15.

In Fig. 3 and Fig. 4 we show  $\sigma_{e-}$  for the higgsino-like scenario B. Since the dominating higgsino components do not couple to sneutrinos, the small gaugino admixture causes only a weak dependence on  $m_{\tilde{\nu}_e}$ , Fig. 3. The destructive interference between  $Z^0$  and  $\tilde{\nu}_e$  exchange is suppressed by the

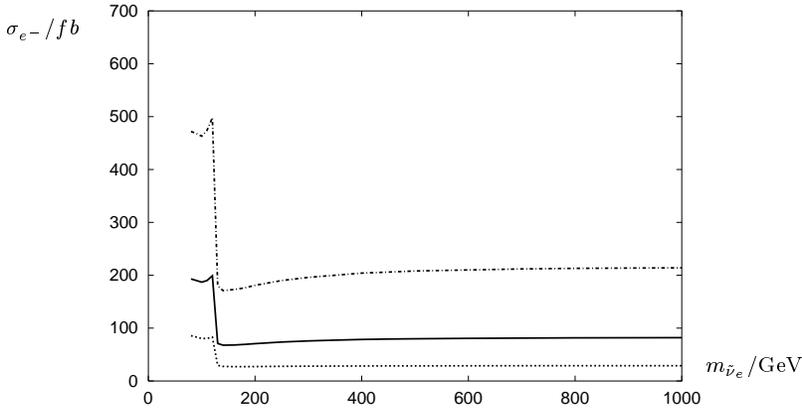


Fig. 3. Cross section  $\sigma_{e^-}$  (see Eq. (1)) for  $\sqrt{s} = 270$  GeV in scenario B for unpolarized beams (solid line), with only  $e^-$  beam polarized  $P_- = +85\%$  (dotted line) and with both beams polarized  $P_- = -85\%$ ,  $P_+ = +60\%$  (dash-dotted line).

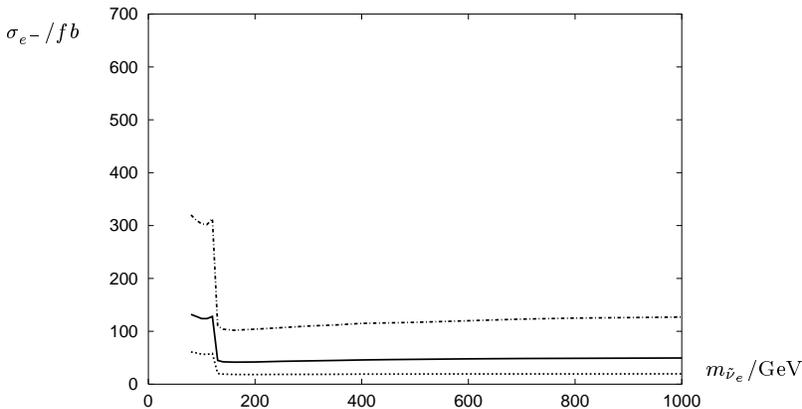


Fig. 4. Cross section  $\sigma_{e^-}$  (see Eq. (1)) for  $\sqrt{s} = 500$  GeV in scenario B for unpolarized beams (solid line), with only  $e^-$  beam polarized  $P_- = +85\%$  (dotted line) and with both beams polarized  $P_- = -85\%$ ,  $P_+ = +60\%$  (dash-dotted line).

dominating higgsino component. For  $m_{\tilde{\nu}_e} > m_{\tilde{\chi}_1^-}$  the cross section is practically independent of  $m_{\tilde{\nu}_e}$ . Only for  $m_{\tilde{\nu}_e} < m_{\tilde{\chi}_1^-}$  it shows a strong dependence on the sneutrino mass due to the two-body decay  $\tilde{\chi}_1^- \rightarrow \tilde{\nu}_e e^-$ .

For higher energy,  $\sqrt{s} = 500$  GeV, Fig. 4,  $\sigma_{e^-}$  is smaller. The dependence on  $m_{\tilde{\nu}_e}$ , however, is essentially unchanged.

Also for higgsino-like charginos beam polarization has a strong influence on the magnitude of  $\sigma_{e^-}$ . For  $P_- = -85\%$  and  $P_+ = +60\%$  and for both values of  $\sqrt{s}$ , Fig. 3 and Fig. 4,  $\sigma_{e^-}$  increases by a factor of about 2.5, which

is somewhat smaller as for the gaugino-like scenario A. For the opposite polarization,  $P_- = +85\%$ ,  $P_+ = -60\%$ ,  $\sigma_{e^-}$  decreases by a factor of 0.5. If only the  $e^-$  beam is polarized with  $P_- = -85\%$  ( $P_- = +85\%$ ) the cross section increases(decreases) by a factor of 1.6(0.4).

### 3.2. Forward-backward asymmetry of the decay lepton

In this section we study the FB-asymmetry  $A_{\text{FB}}$  of the decay electron, Eq. (2), for  $m_{\tilde{\nu}_e}$  between 80 GeV and 1000 GeV. Since the angular distribution of the chargino decay products is determined by the polarization of the decaying chargino, the FB-asymmetry of the decay lepton strongly depends on the spin correlations between production and decay. The dependence of  $A_{\text{FB}}$  on  $m_{\tilde{\nu}_e}$ , on the beam polarization and on  $\sqrt{s}$  is a result of the complex interplay between production and decay.

In scenario A for  $\sqrt{s} = 270$  GeV the dependence of  $A_{\text{FB}}$  on  $m_{\tilde{\nu}_e}$  is shown in Fig. 5. For high  $m_{\tilde{\nu}_e} > 400$  GeV it is about 8% and is nearly independent of  $m_{\tilde{\nu}_e}$ . For  $m_{\tilde{\nu}_e} < 400$  GeV, however,  $A_{\text{FB}}$  shows a complex and interesting mass dependence. The destructive  $Z^0$ - $\tilde{\nu}_e$  interference in the production causes large  $A_{\text{FB}} \approx 30\%$ . Since this destructive interference effect vanishes at about  $m_{\tilde{\nu}_e} \approx 200$  GeV the FB-asymmetry decreases for higher values of  $m_{\tilde{\nu}_e}$ . The deep dip at  $m_{\tilde{\nu}_e} \approx 140$  GeV is due to destructive  $W$ - $\tilde{\nu}_e$  ( $W$ - $\tilde{e}$ ) interference in the decay process  $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 e^- \tilde{\nu}_e$ . For  $m_{\tilde{\nu}_e} \leq m_{\tilde{\chi}_1^-}$  the FB-asymmetry strongly increases up to about 35%, owing to the two-body decay  $\tilde{\chi}_1^- \rightarrow \tilde{\nu}_e e^-$ .

For  $\sqrt{s} = 500$  GeV, Fig. 6, large values of  $A_{\text{FB}}$  up to 50% can be reached in scenario A. The  $Z^0$ - $\tilde{\nu}_e$  interference effect in production is shifted to higher  $m_{\tilde{\nu}_e}$  so that just for  $m_{\tilde{\nu}_e} \geq 250$  GeV  $A_{\text{FB}}$  decreases from 48% to 10% for  $m_{\tilde{\nu}_e} = 1000$  GeV. For  $\sqrt{s} = 500$  GeV the  $Z^0$ - $\tilde{\nu}_e$  interference in the decay process is less important because for higher energies the characteristics of the production process is more and more dominating. Therefore at  $m_{\tilde{\nu}_e} \approx 140$  GeV  $A_{\text{FB}}$  decreases only to about 43% in contrast to the deep dip at  $m_{\tilde{\nu}_e} \approx 140$  GeV for  $\sqrt{s} = 270$  GeV. Again, for  $m_{\tilde{\nu}_e} \leq m_{\tilde{\chi}_1^-}$  the two-body decay  $\tilde{\chi}_1^- \rightarrow \tilde{\nu}_e e^-$  involves large  $A_{\text{FB}} \approx 50\%$ .

Note that in the gaugino-like scenario A  $A_{\text{FB}}$  is nearly independent of beam polarization. This emerges as a consequence of the fact that in scenario A the beam polarization changes the magnitude of  $\sigma_{e^-}$  by a factor which is nearly independent of  $m_{\tilde{\nu}_e}$ . This factor cancels in  $A_{\text{FB}}$ , Eq. (2). Only for  $P_- > 0$  a small polarization effect can be observed, see Fig. 5 and Fig. 6.

In the higgsino-like scenario B, Fig. 7, the FB-asymmetry for  $\sqrt{s} = 270$  GeV is much smaller than in scenario A,  $A_{\text{FB}} \approx 5\%$  for  $m_{\tilde{\nu}_e} \geq m_{\tilde{\chi}_1^-}$ .

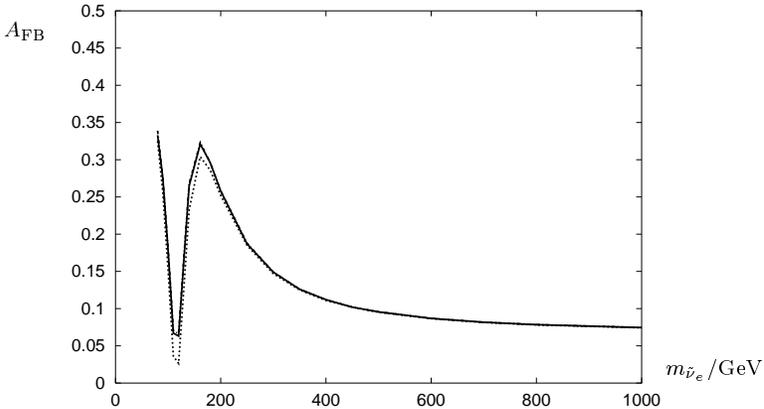


Fig. 5. Electron forward–backward asymmetry  $A_{\text{FB}}$  (see Eq. (2)) in the laboratory system for  $\sqrt{s} = 270$  GeV in scenario A for unpolarized beams (solid line), with only  $e^-$  beam polarized  $P_- = +85\%$  (dotted line) and with both beams polarized  $P_- = -85\%$ ,  $P_+ = +60\%$  (dash-dotted line).

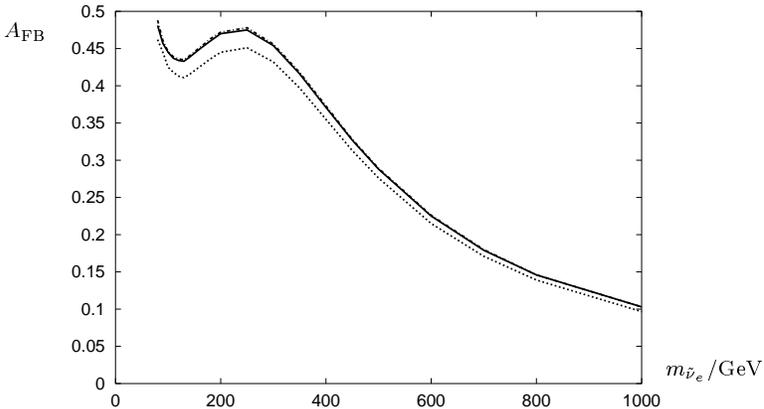


Fig. 6. Electron forward–backward asymmetry  $A_{\text{FB}}$  (see Eq. (2)) in the laboratory system for  $\sqrt{s} = 500$  GeV in scenario A for unpolarized beams (solid line), with only  $e^-$  beam polarized  $P_- = +85\%$  (dotted line) and with both beams polarized  $P_- = -85\%$ ,  $P_+ = +60\%$  (dash-dotted line).

Only for  $m_{\tilde{\nu}_e} \leq m_{\tilde{\chi}_1^-}$  when the two-body decay  $\tilde{\chi}_1^- \rightarrow e^- \tilde{\nu}_e$  is open large  $A_{\text{FB}} \approx 33\%$  can be reached for unpolarized beams.

For  $\sqrt{s} = 500$  GeV  $A_{\text{FB}}$  decreases,  $A_{\text{FB}} \leq 5\%$  for  $m_{\tilde{\nu}_e} \geq m_{\tilde{\chi}_1^-}$  and  $A_{\text{FB}} \approx 18\%$  for  $m_{\tilde{\nu}_e} \leq m_{\tilde{\chi}_1^-}$ , Fig. 8.

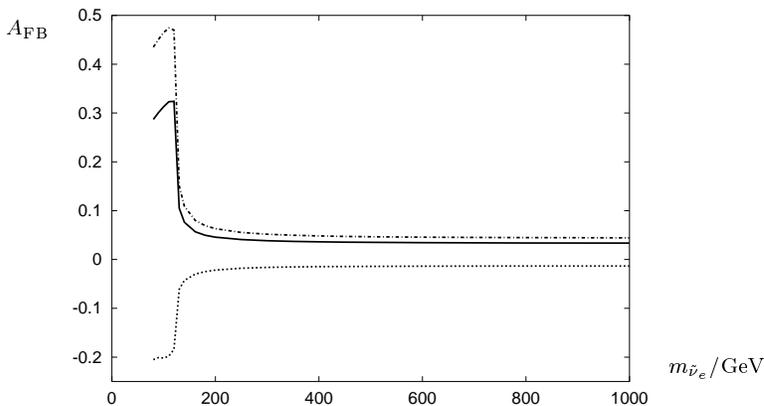


Fig. 7. Lepton forward–backward asymmetry  $A_{\text{FB}}$  (see Eq. (2)) in the laboratory system for  $\sqrt{s} = 270$  GeV in scenario B for unpolarized beams (solid line), with only  $e^-$  beam polarized  $P_- = +85\%$  (dotted line) and with both beams polarized  $P_- = -85\%$ ,  $P_+ = +60\%$  (dash-dotted line).

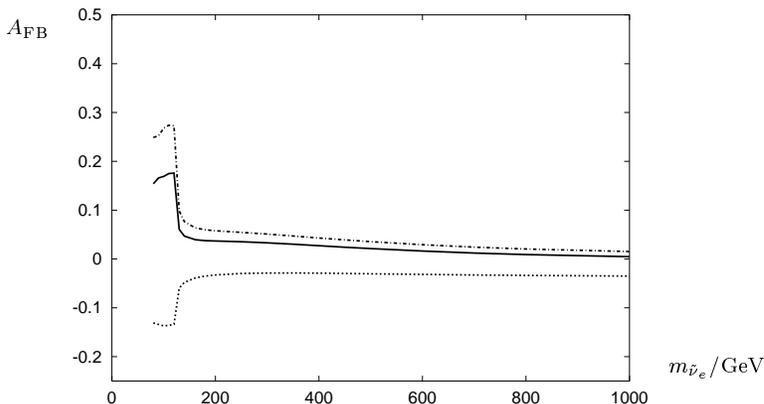


Fig. 8. Lepton forward–backward asymmetry  $A_{\text{FB}}$  (see Eq. (2)) in the laboratory system for  $\sqrt{s} = 500$  GeV in scenario B for unpolarized beams (solid line), with only  $e^-$  beam polarized  $P_- = +85\%$  (dotted line) and with both beams polarized  $P_- = -85\%$ ,  $P_+ = +60\%$  (dash-dotted line).

In this higgsino-like scenario B the FB–asymmetry sensitively depends on the beam polarization. For  $P_- = -85\%$ ,  $P_+ = +60\%$  the FB–asymmetry increases for  $m_{\tilde{\nu}_e} \leq m_{\tilde{\chi}_1^-}$  up to 48% for  $\sqrt{s} = 270$  GeV and up to 28% for  $\sqrt{s} = 500$  GeV. If only the electron beam is polarized with  $P_- = +85\%$ , one even obtains for  $m_{\tilde{\nu}_e} \leq m_{\tilde{\chi}_1^-}$  large negative FB–asymmetries,  $A_{\text{FB}} \approx -20\%$  ( $A_{\text{FB}} \approx -12\%$ ), for  $\sqrt{s} = 270$  GeV ( $\sqrt{s} = 500$  GeV).

### 3.3. Constraining $m_{\tilde{\nu}_e}$

In this section we study the prospects to constrain  $m_{\tilde{\nu}_e}$  by measuring  $\sigma_{e^-}$  and  $A_{\text{FB}}$  with different beam polarizations.

We assume that  $\tan\beta$ ,  $m_{\tilde{\chi}_1^-}$  and  $m_{\tilde{\chi}_1^0}$  are already known and we choose as an example the gaugino-like scenario A and the higgsino-like scenario B.

One obtains the largest cross sections for polarizations  $P_- < 0$ ,  $P_+ > 0$ . We therefore assume that  $\sigma_{e^-}$  has been measured for beam polarizations  $P_- = -85\%$ ,  $P_+ = +60\%$  and for energies  $\sqrt{s} = 270$  GeV and  $\sqrt{s} = 500$  GeV with an error of 5%. We study also the corresponding  $A_{\text{FB}}$  for two combinations of beam polarizations,  $P_- = -85\%$ ,  $P_+ = +60\%$  and  $P_- = +85\%$ ,  $P_+ = 0\%$ . For the second case we use unpolarized positrons since also switching the  $e^+$  polarization gives extremely small rates.

#### 3.3.1. Constraining $m_{\tilde{\nu}_e}$ for $\sqrt{s} = 270$ GeV

We assume that for  $\sqrt{s} = 270$  GeV and  $P_- = -85\%$ ,  $P_+ = +60\%$  a cross section of  $\sigma_{e^-} = 180$  fb  $\pm 5\%$  has been measured. As can be seen from Fig. 1 for scenario A and from Fig. 3 for scenario B this cross section is compatible with two regions for  $m_{\tilde{\nu}_e}$  in either case.

In scenario A the cross section is compatible with small values of  $m_{\tilde{\nu}_e}$  between 85 GeV and 89 GeV and with high  $m_{\tilde{\nu}_e}$  between 240 GeV and 255 GeV, Fig. 1. For the case of low  $m_{\tilde{\nu}_e}$  the FB-asymmetry is between 29% and 32% and for high  $m_{\tilde{\nu}_e}$  between 19% and 22%, Fig. 5. Accordingly  $A_{\text{FB}}$  allows to discriminate between the two regions for  $m_{\tilde{\nu}_e}$ . Changing the polarization to  $P_- = +85\%$ ,  $P_+ = 0\%$ , the FB-asymmetry gives no additional constraints for  $m_{\tilde{\nu}_e}$ , Fig. 5.

In scenario B the cross section is compatible with small  $m_{\tilde{\nu}_e}$  between 128 GeV and 140 GeV near the two-body decay threshold and with high  $m_{\tilde{\nu}_e} > 250$  GeV, Fig. 3. For the case of low  $m_{\tilde{\nu}_e}$  the FB-asymmetry is between 11% and 29% and for high  $m_{\tilde{\nu}_e}$   $A_{\text{FB}}$  is less than 5%, Fig. 7. Again  $A_{\text{FB}}$  allows to discriminate between the two regions for  $m_{\tilde{\nu}_e}$ .

In our examples with  $P_- = -85\%$ ,  $P_+ = +60\%$  the values of the FB-asymmetry for the low mass region of scenario B (11%–29%) overlaps with that for the low mass region of scenario A (29%–32%) as well as with that of the high mass region of scenario A (19%–22%).

However measuring  $A_{\text{FB}}$  for a suitably polarized electron beam and an unpolarized positron beam allows to discriminate between scenario A and scenario B. For  $P_- = +85\%$ ,  $P_+ = 0\%$  the FB-asymmetry in the low mass region of scenario B is negative between  $-5\%$  and  $-16\%$ , whereas for scenario A the respective regions for  $A_{\text{FB}}$  are unchanged, compare Fig. 5 and Fig. 7.

### 3.3.2. Constraining $m_{\tilde{\nu}_e}$ for $\sqrt{s} = 500$ GeV

In the same manner we study  $\sigma_{e^-}$  and  $A_{\text{FB}}$  for  $\sqrt{s} = 500$  GeV. We assume that for polarized beams with  $P_- = -85\%$ ,  $P_+ = +60\%$  the cross section  $\sigma_{e^-} = 130 \text{ fb} \pm 5\%$  has been measured. As can be seen from Fig. 2 for scenario A and Fig. 4 for scenario B this cross section is again compatible with two regions for  $m_{\tilde{\nu}_e}$  in either case.

In scenario A  $\sigma_{e^-}$  is compatible with small values of  $m_{\tilde{\nu}_e}$  between 161 GeV and 175 GeV and with high values of  $m_{\tilde{\nu}_e}$  between 420 GeV and 450 GeV, Fig. 2. For small  $m_{\tilde{\nu}_e}$  the FB-asymmetry is about 45% whereas for high  $m_{\tilde{\nu}_e}$  it is between 32% and 35%, clearly distinguishable from the case of low  $m_{\tilde{\nu}_e}$ , Fig. 6. As compared to the case of lower energies,  $\sqrt{s} = 270$  GeV, the values of  $A_{\text{FB}}$  are higher and restricted to smaller regions. Changing the beam polarization to  $P_- = +85\%$ ,  $P_+ = 0\%$  the FB-asymmetry gives practically no additional constraints for  $m_{\tilde{\nu}_e}$ , Fig. 6.

In scenario B  $\sigma_{e^-}$  is compatible with small  $m_{\tilde{\nu}_e}$  in the region between 122 GeV and 128 GeV near the two-body decay threshold and with high  $m_{\tilde{\nu}_e} > 750$  GeV, Fig. 4. For low  $m_{\tilde{\nu}_e}$  the FB-asymmetry is between 10% and 28% whereas for high values of  $m_{\tilde{\nu}_e}$  it is rather small,  $A_{\text{FB}} < 3\%$ . These two regions for  $m_{\tilde{\nu}_e}$  can clearly be distinguished by measuring  $A_{\text{FB}}$ , Fig. 8.

Similar as for lower energies,  $\sqrt{s} = 270$  GeV, the regions for  $A_{\text{FB}}$  for the case of high  $m_{\tilde{\nu}_e}$  in scenario A and for the case of  $m_{\tilde{\nu}_e} \approx m_{\tilde{\chi}_1^-}$  in scenario B are not well separated. Again a suitably polarized  $e^-$  beam and an unpolarized  $e^+$  beam allow to discriminate between scenario A and scenario B. For  $P_- = +85\%$ ,  $P_+ = 0\%$  the FB-asymmetry is negative between  $A_{\text{FB}} = -8\%$  and  $A_{\text{FB}} = -12\%$  in scenario B, whereas it has large positive values between  $A_{\text{FB}} = 31\%$  and  $A_{\text{FB}} = 34\%$  in scenario A, compare Fig. 6 and Fig. 8.

## 4. Summary and conclusions

For the determination of the MSSM parameters  $M$ ,  $\mu$  and  $\tan \beta$  from chargino production, the sneutrino mass plays a crucial role. With regard to the determination of the sneutrino mass we have studied chargino pair production  $e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-$  with polarized beams and the subsequent leptonic decay  $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 e^- \tilde{\nu}_e$  taking into account the complete spin correlations between production and decay. The spin correlations are crucial for the decay angular distributions and the forward-backward asymmetries of the decay leptons.

We have presented a method for constraining  $m_{\tilde{\nu}_e}$  if  $\tan \beta$  and the masses of  $\tilde{\chi}_1^-$  and of  $\tilde{\chi}_1^0$  are known. Accordingly we choose two representative scenarios with a dominating gaugino and with a dominating higgsino component of  $\tilde{\chi}_1^-$ , respectively. We have studied the prospect to constrain the sneu-

trino mass by measuring polarized cross sections and FB-asymmetries of the decay leptons in the laboratory system.

Simultaneous polarization of both beams is not only important for enlarging the cross section but it can also have rather strong influence on the FB-asymmetry of the decay electron depending on the mixing character of the charginos. For charginos with dominating gaugino character the FB-asymmetry is practically independent of the beam polarization. But for higgsino-like charginos beam polarization can considerably influence the FB-asymmetry.

In our examples  $\sigma_{e^-}$  measured for the beam polarization  $P_- = -85\%$ ,  $P_+ = +60\%$  with an error of 5%, *e.g.*, is compatible with two regions for  $m_{\tilde{\nu}_e}$ . For gaugino-like charginos as well as for higgsino-like ones the corresponding FB-asymmetry allows to distinguish between the two regions of  $m_{\tilde{\nu}_e}$ . Beyond that the two mixing scenarios can be distinguished by additional measurement of the FB-asymmetry with a right polarized  $e^-$  beam. Then the sign of  $A_{\text{FB}}$  changes for higgsino-like charginos.

We have presented numerical results for  $\sqrt{s} = 270$  GeV, near the chargino production threshold, and for  $\sqrt{s} = 500$  GeV. For gaugino-like charginos  $m_{\tilde{\nu}_e}$  can be constrained up to a few GeV, for higgsino-like charginos this is possible if  $m_{\tilde{\nu}_e}$  is in the vicinity of the chargino mass. Obviously a complete MC study with inclusion of experimental cuts would be indispensable for realistic predictions.

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