

# THE REACTION $\pi N \rightarrow \pi\pi N$ IN THE FRAMEWORK OF A MESON EXCHANGE MODEL \*

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We investigate the process  $\pi N \rightarrow \pi\pi N$  in a coupled channel meson exchange model. Preliminary results for  $\pi^- p \rightarrow \pi^+ \pi^- n$  total cross sections and angular correlation functions are presented.

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## 1. Introduction

Pion induced two-pion production on the nucleon has been under both experimental and theoretical [1,2] examination for many years. In particular one hopes to find the so-called "missing resonances", states which have been predicted by semi-relativistic quark model calculations [3] but have not yet been observed in  $\pi N$ -reactions. Most of the missing states are predicted to have small decay amplitudes to  $\pi N$  [4] which makes it necessary to look for them in reactions other than  $\pi N$  scattering.

On the theoretical side, coupled channel meson exchange models including the  $\eta N$ ,  $\rho N$ ,  $\sigma N$  and the  $\pi\Delta$  channels have been successful in describing  $\pi N$  scattering in an energy range up to 1.9 GeV [5]. The intention of this work is to apply the model of Ref. [5] to the reaction  $\pi N \rightarrow \pi\pi N$ .

## 2. The model

As a first step to study the two-pion decay of nucleon resonances, we performed a calculation at tree level with resonance parameters and coupling constants derived from the full model of Ref. [5]. The processes included are shown in Fig. 1.

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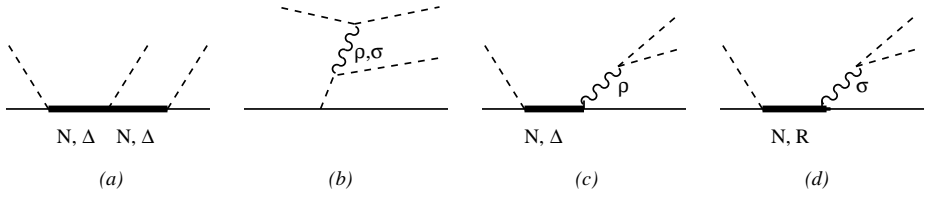


Fig. 1. Tree level diagrams

In this model,  $\sigma$ - and  $\rho$ -exchange are understood to be an effective parameterization of a correlated pion pair in the scalar-isoscalar channel respectively the  $\rho$ -channel, which has been calculated microscopically in Ref. [6].

So far the Roper resonance is only included in diagrams of the type of 1(d), where it makes a non-negligible contribution. But as we go to higher energies, we will also have to include the Roper resonance in diagrams 1(a) and 1(c).

### 3. Results and discussion

Our preliminary results for the  $\pi^- p \rightarrow \pi^+ \pi^- n$  total cross sections are displayed in Fig. 2. Tree level  $t$ -channel  $\rho$ -exchange in processes 1(b) overestimates  $\pi\pi$  scattering, therefore also the  $\pi N \rightarrow \pi\pi N$  cross sections. So the explicit inclusion of unitarization effects has to be considered next.

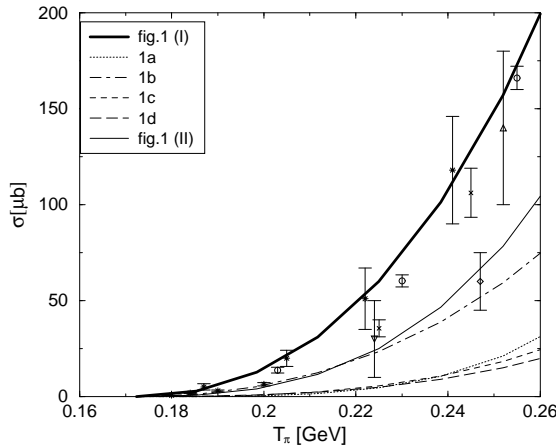


Fig. 2. Total cross sections for  $\pi^- p \rightarrow \pi^+ \pi^- n$ . The line labels 1a–1d refer to the diagrams of Fig.1. “fig.1 (I)” is calculated including all diagrams, in “fig.1 (II)”  $t$ -channel  $\rho$ -exchange in 1d is omitted. Data are taken from Ref. [7].

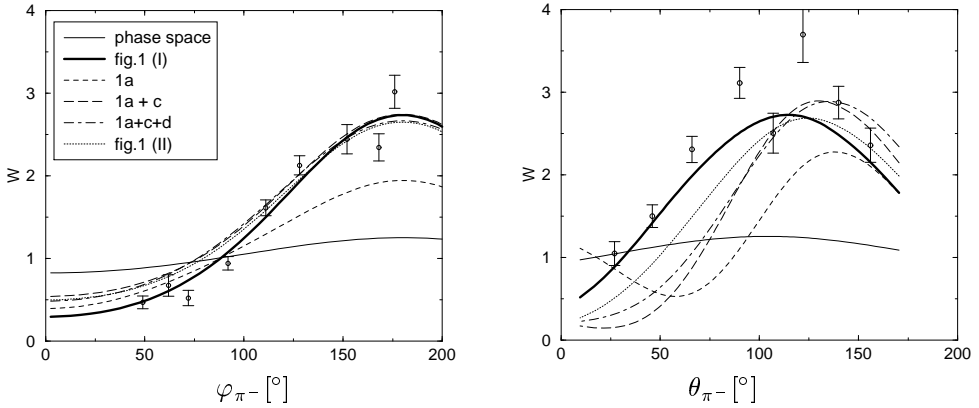


Fig. 3. Angular correlation functions for  $\pi^- p \rightarrow \pi^+ \pi^- n$ . The kinematics are fixed to  $T_\pi^{\text{in}} = 0.284$  GeV,  $k_{\pi^+}^{\text{lab}} = 0.112$  GeV and  $\theta_{\pi^+}^{\text{cm}} = 78^\circ$ . The left-hand side shows the angular correlation function  $W(\varphi_{\pi^-}^{\text{cm}})$  with  $\theta_{\pi^-}^{\text{cm}}$  fixed to  $115^\circ$ , the right-hand side shows  $W(\theta_{\pi^-}^{\text{cm}})$  for  $\varphi_{\pi^-}^{\text{cm}} = 175^\circ$ . The data are from Ref. [8].

In Fig. 3 we show angular correlation functions  $W$  for the reaction channel  $\pi^- p \rightarrow \pi^+ \pi^- n$ . The processes of Fig. 1(a) alone already reproduce the trend of the  $W(\varphi_{\pi^-})$  data. By successive addition of the other processes one obtains a gradual improvement of the description for the  $W(\varphi_{\pi^-})$  distribution as well as for  $W(\theta_{\pi^-})$ . The results hardly depend on the inclusion of  $t$ -channel  $\rho$ -exchange in diagrams 1(b).

Our meson exchange model is definitely successful in describing the  $\pi^- p \rightarrow \pi^+ \pi^- n$  data. Calculations for the other reaction channels are in process.

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