# ORIGIN OF THE METAL–INSULATOR TRANSITION IN $PrRu_4P_{12}^*$

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 $PrRu_4P_{12}$  shows a metal-insulator (M-I) transition with a structural phase transition and without magnetic anomaly. To investigate the origin of the M-I transition, we have calculated the band structures by using the FLAPW-LDA+U method with many types of lattice distortions. The result shows an insulator when P ions are slightly distorted with  $\Gamma_1$  mode, suggesting the M-I transition is caused by the perfect 3 dimensional nesting of the Fermi surface.

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## 1. Introduction

The filled skutterudites  $RT_4X_{12}$  (R=light Rare earth, Yb, Th and U; T= Fe, Ru and Os; X= P, As and Sb) have recently attracted much attention as improved thermoelectric materials [1] and for the variety of the electrical and magnetic properties. Among them,  $PrRu_4P_{12}$  shows a metal-insulator

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(MI) transition at  $T_{\rm MI} = 60$  K [2],  $\Pr Fe_4 P_{12}$  undergoes a non-magnetic ordering showing heavy fermion behaviour under magnetic fields [3,4]. Very recently, a new class of heavy fermion superconductivity has been reported in  $\Pr Os_4 Sb_{12}$  [5,6]. Such the interesting physical properties are expected to reflect the Fermi surface property and the  $4f^2$  states under the crystalline field. In fact, the Fermi surfaces of  $\operatorname{RT}_4 P_{12}$  (T=Fe, Ru) shows nesting property with q = (1, 0, 0) [7,8].

The phase transitions of  $PrFe_4P_{12}$  and  $PrRu_4P_{12}$  have been discussed as anti-quadrupolar ordering [9, 10]. However, no distinct magnetic anomaly has been observed at the M-I transition in  $PrRu_4P_{12}$  [11–14]. Then, it has been suggested that the charge density wave (CDW) is a possible origin of the M-I transition [14]. When the origin of the transition is non-magnetic one, the  $\Gamma_1$ -type lattice distortion should be considered [15].

#### 2. Band structure calculations

To investigate the origin of the M-I transition of  $PrRu_4P_{12}$ , band structure calculations are performed by using the FLAPW-LDA+U method [16] with many types of  $\Gamma_1$ -type lattice distortions.

PrRu<sub>4</sub>P<sub>12</sub> crystallises in a unique body-centered cubic (BCC) structure of a space group  $Im\bar{3}$  ( $T_h^5$ , # 204). The atomic parameters are obtained as a=8.0424 Å for the lattice constant and u = 0.3576, v = 0.1444 for 24gsite occupied by P [17]. The structural phase transition with q = (1, 0, 0)is observed suggesting that the unit cell becomes doubled to be a simple cubic structure  $Pm\bar{3}$  ( $T_h^1$ , # 200) [18]. However, the details of the distortion have remained undetermined experimentally. Now only P distortions are considered. In  $Pm\bar{3}$ , 12j-site ( $0, u + \delta_u^A, v + \delta_v^A$ ) and 12k-site ( $1/2, 1/2 + u + \delta_u^B, 1/2 + v + \delta_v^B$ ) are occupied by 24 P ions. When  $\delta_u^A = \delta_u^B$  and  $\delta_v^A = \delta_v^B$ , the lattice becomes back to  $Im\bar{3}$ . The calculations are performed with a variety of two parameters;  $\delta_u = \delta_u^A = -\delta_u^B$  and  $\delta_v = \delta_v^A = -\delta_v^B$ 

The details of the method follow the previous LDA+U calculation [8]. Now the calculations for the system containing 34 atoms are performed by using up to about 2,100 LAPW basis functions. The local symmetry for Pr-site is unchanged and no magnetic anomaly is observed at  $T_{\rm MI}$ , so the occupied 4f states are assumed as the singlet ground state ( $\Gamma_1 = \Gamma_7(j = 5/2) \times \Gamma_7(j = 5/2)$  in  $O_h$ ) for the starting potential, then determined selfconsistently. The occupied and unoccupied 4f states are located below and above the Fermi level, respectively, therefore they do not affect directly the band structure near the Fermi level.

The original Fermi surface in Im3 has a very good nesting property with the volume of a half of the BCC Brillouin zone [8], however, for many cases a small number of carriers survives when the Fermi surface is nested. There are two inequivalent Z axes, which are due to no four fold symmetry axes in  $Pm\bar{3}$ , and a band overlap between bands on the two Z axes tends to remain in the case of  $\delta_v = 0$ . In the case of  $\delta_u = 0$ , the degeneracy of the bands around the X points are hardly lifted. Therefore opening a band gap prefer that both of  $\delta_v$  and  $\delta_u$  are non zero. Moreover,  $\delta_v$  and  $\delta_u$  should have another sign, then will keep the Pr-P distance almost unchanged.

One successful result is obtained, as shown in Fig. 1, for  $\delta_u = 0.003a$ and  $\delta_v = -0.004a$ . Only 0.5% distortion wipes out a whole of the carrier, resulting in an insulator, indicating this is the 3 dimensional *perfect* nesting system. This type of the P distortion must be observed experimentally.



Fig. 1. The calculated (a) band structure and (b) the density of states for  $PrRu_4P_{12}$  with the  $\Gamma_1$ -type distortion, with the 1mRy band gap width.

Here we consider the 4f states do not participate the phase transition in  $PrRu_4P_{12}$ , assuming the singlet ground state. Therefore such the nesting is expected in another compound, *e.g.*,  $LaRu_4P_{12}$ . However, the existence of the other Fermi surfaces [19] would suppress such the nesting in  $LaRu_4P_{12}$ , while anti-quadrupolar ordering cooperates with the nesting in  $PrFe_4P_{12}$ , though also another Fermi surface appears.

#### 3. Conclusion

The band structure calculations reveal that  $PrRu_4P_{12}$  could be an insulator with  $\Gamma_1$ -type P-distortion in the doubled unit cell. It shows the origin of the M-I transition is the 3 dimensional Fermi surface *perfect* nesting. This work was partly supported by a Grant-in-Aid for Science Research from the Ministry of Education, Culture, Sports, Science and Technology, Japan.

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