# ORBITAL-LATTICE QUASIPARTICLES IN FERROMAGNETIC $\mathrm{LaMnO}_{3}{ }^{*}$ 

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We investigate the combined influence of electron-phonon and orbital polarization interactions on hole propagation in a ferromagnetic plane of orbitally ordered $\mathrm{LaMnO}_{3}$. The quasiparticle band found at the bottom of the hole spectrum is accompanied by broad structures representing vibrational side-bands resulting from the hole-lattice coupling.

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To explain the colossal magnetoresistence [1] and metal-insulator transition observed in manganese oxides beyond the simple double-exchange model one has to understand a complex interplay between magnetic, charge, and structural order as well as the mobility of itinerant strongly correlated $e_{g}$ carriers in undoped $\mathrm{LaMnO}_{3}$ with $A$-type antiferromagnetic order. Considering the hole motion within ferromagnetic $(a, b)$ planes one can constrain the effective model to the hole scattering on orbital [2] and phononic [3] excitations only. Both kinds of the excitations have been observed recently using Raman scattering measurements [4]. The propagation of a single hole is considered using the lattice-orbital-hole model,

$$
\begin{equation*}
H=H_{t}+H_{\Delta}+H_{J}+H_{\mathrm{JT}}+E_{l}+H_{\mathrm{ph}} \tag{1}
\end{equation*}
$$

which includes the kinetic energy of a hole $\left(H_{t}\right)$, the polarization of orbitals around a hole $\left(H_{\Delta}\right)[5]$, superexchange interaction between the $\mathrm{Mn}^{3+}-\mathrm{Mn}^{3+}$

[^0]ions due to charge excitations $\left(H_{J}\right)$ [6], the Jahn-Teller (JT) interaction $\left(H_{\mathrm{JT}}\right)$ with the distorted lattice energy $\left(E_{l}\right)$ [7], and the oxygen ion oscillations around their distorted positions $\left(H_{\mathrm{ph}}\right)$. The alternating orbital ordering is defined by two orbital sublattices with the occupied $e_{g}$ orbitals,
\[

$$
\begin{equation*}
|i \mu\rangle=\cos \left(\frac{\pi}{4}-\phi\right)|i z\rangle \pm \sin \left(\frac{\pi}{4}-\phi\right)|i x\rangle, \tag{2}
\end{equation*}
$$

\]

where $+(-)$ refers to $i \in A(i \in B)$ orbital sublattice, and $|i x\rangle(|i z\rangle)$ stands for the orbital $\left|x^{2}-y^{2}\right\rangle\left(\left|3 z^{2}-r^{2}\right\rangle\right)$ at site $i$, respectively. The angle $\phi$ describes the type of orbital ordering and depends on external pressure [8].

In the linear phonon-orbital-wave (LPOW) theory the effective Hamiltonian (1) represents a coupled hole-phonon-orbiton problem in momentum space [3],

$$
\begin{align*}
& H_{\mathrm{LPOW}}=\sum_{\boldsymbol{k}} \varepsilon_{\boldsymbol{k}} h_{\boldsymbol{k}}^{\dagger} h_{\boldsymbol{k}}+\sum_{\boldsymbol{q}}\left(\sum_{\xi=1,2} \Omega_{\boldsymbol{q}}^{(\xi)} \beta_{\boldsymbol{q}, \xi}^{\dagger} \beta_{\boldsymbol{q}, \xi}+\omega_{0} \sum_{\xi=1,3} B_{\boldsymbol{q}, \xi}^{\dagger} B_{\boldsymbol{q}, \xi}\right) \\
& +\sum_{\boldsymbol{k}, \boldsymbol{q}}\left\{h_{\boldsymbol{k}-\boldsymbol{q}}^{\dagger} h_{\boldsymbol{k}}\left[\sum_{\xi=1,3} M_{0}^{(\xi)} B_{\boldsymbol{q}, \xi}^{\dagger}+\sum_{\xi=1,2}\left(M_{\boldsymbol{k}, \boldsymbol{q}}^{(\xi)} \beta_{\boldsymbol{q}, \xi}^{\dagger}+N_{\boldsymbol{k}, \boldsymbol{q}}^{(\xi)} \beta_{\boldsymbol{q}+\boldsymbol{Q}, \xi}^{\dagger}\right)\right]+\mathrm{H.c.}\right\}, \tag{3}
\end{align*}
$$

with the free hole dispersion, $\varepsilon_{\boldsymbol{k}}=t[1-2 \sin (2 \phi)] \gamma_{\boldsymbol{k}}$, and the nesting vector $\boldsymbol{Q}=(\pi, \pi) . M_{0}^{(\xi)}$ and $\left\{M_{\boldsymbol{k}, \boldsymbol{q}}^{(\xi)}, N_{\boldsymbol{k}, \boldsymbol{q}}^{(\xi)}\right\}$ are the structureless hole-phonon and mixed orbiton-phonon vertices, respectively, while $B_{\boldsymbol{q}, \xi}$ and $\beta_{\boldsymbol{q}, \xi}$ are bosonic operators for the phonon and mixed excitations [9], respectively, which depend on the JT coupling $\propto \lambda$ and on the polarization interactions $\propto \Delta$. The Green's function, $G(\boldsymbol{k}, \omega)=\left[\omega-\varepsilon_{\boldsymbol{k}}-\Sigma(\boldsymbol{k}, \omega)\right]^{-1}$, is determined in the selfconsistent Born approximation [10] by the hole self-energy obtained from the dressed Green's function,

$$
\begin{align*}
& \quad \Sigma(\boldsymbol{k}, \omega)=\sum_{\boldsymbol{q}} \sum_{\xi=1,2}\left\{\left(M_{\boldsymbol{k}, \boldsymbol{q}}^{(\xi)}\right)^{2} G\left[\boldsymbol{k}-\boldsymbol{q}, \omega-\Omega_{\boldsymbol{q}}^{(\xi)}\right]\right. \\
& \left.+\quad\left(N_{\boldsymbol{k}, \boldsymbol{q}}^{(\xi)}\right)^{2} G\left[\boldsymbol{k}-\boldsymbol{q}, \omega-\Omega_{\boldsymbol{q}+\boldsymbol{Q}}^{(\xi)}\right]\right\}+3 M_{0}^{2} \sum_{\boldsymbol{q}} G\left[\boldsymbol{k}-\boldsymbol{q}, \omega-\omega_{0}\right] \tag{4}
\end{align*}
$$

leading to the hole spectral functions, $A(\boldsymbol{k}, \omega)=-\frac{1}{\pi} \operatorname{Im} G\left(\boldsymbol{k}, \omega+i 0^{+}\right)$.
Here, we have concentrated on three representative alternating orbital orderings: $\left|x^{2}-z^{2}\right\rangle /\left|y^{2}-z^{2}\right\rangle,(|x\rangle+|z\rangle) /(|x\rangle-|z\rangle)$, and $\left|3 x^{2}-r^{2}\right\rangle /\left|3 y^{2}-r^{2}\right\rangle$, realized for $\phi=\pi / 12,0$, and $-\pi / 12$, respectively. At finite momenta the spectra consist of quasiparticle (QP) peaks at low energies and the incoherent background at higher energies, whereas at $\boldsymbol{k} \simeq(0,0)$ one finds a completely


Fig. 1. The hole spectral functions $A(\boldsymbol{k}, \omega)$ calculated on a grid with $20 \times 20$ $\boldsymbol{q}$-points, as obtained along the $(0,0)-(\pi, \pi)$ direction for the staggered $(|x\rangle-$ $|z\rangle) /(|x\rangle+|z\rangle)$ orbital ordering $(\phi=0)$ for $\lambda / t=7$ with: (a) $\Delta=0$ and (b) $\Delta=t$. Other parameters as in Ref. [3].
incoherent spectrum. As presented in Figs. 1 and 2, the QP at $\boldsymbol{k} \rightarrow(\pi, \pi)$ is accompanied by a broad $(\Delta \omega \sim t)$ structure above, which represents a sideband effect for the anti-JT distortions predicted by Allen and Perebeinos for $\mathrm{LaMnO}_{3}$ [11]. Increasing the in-plane hopping by changing the orbital ordering to $\phi=-\pi / 12$, we find a band-like structure at $\boldsymbol{k} \rightarrow(0,0)$ and $\omega \simeq 3 t$ which gets broader as a result of the JT interaction [see Fig. 2(a) and (b)].


Fig. 2. The hole spectral functions $A(\boldsymbol{k}, \omega)$ as in Fig. 1, but for the staggered directional $\left|3 x^{2}-r^{2}\right\rangle /\left|3 y^{2}-r^{2}\right\rangle$ orbital ordering $(\phi=-\pi / 12)$.

TABLE I
The QP spectral weight $\left(Z_{\boldsymbol{k}}\right)$ and the QP binding energy $\left(E_{b}\right)$ found at the bottom of the QP band $[k=(\pi, \pi)]$ as a function of $\Delta / t$, obtained for the orbital orderings given by $\phi=0$ and $\pm \pi / 12$, respectively.

|  | $\phi=-\pi / 12$ |  | $\phi=0$ |  | $\phi=\pi / 12$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $\Delta / t$ | $Z_{\boldsymbol{k}}$ | $E_{b} / t$ | $Z_{\boldsymbol{k}}$ | $E_{b} / t$ | $Z_{\boldsymbol{k}}$ | $E_{b} / t$ |
| 0.0 | 0.375 | 0.900 | 0.274 | 1.280 | 0.110 | 1.685 |
| 0.25 | 0.362 | 0.970 | 0.232 | 1.295 | 0.047 | 1.705 |
| 0.50 | 0.341 | 1.095 | 0.157 | 1.430 | 0.027 | 1.940 |
| 0.75 | 0.315 | 1.275 | 0.084 | 1.710 | 0.024 | 2.215 |
| 1.0 | 0.285 | 1.510 | 0.048 | 2.105 | 0.003 | 2.550 |

The orbital polarization does not influence the orbital excitation energy, but contributes instead new vertices $\propto \Delta$ (see [12]) to the hole-orbiton scattering. These local processes around a hole drastically decrease the width of the QP band, increasing simultaneously the polaron binding energy [see Figs. 1(b) and 2(b)]. The binding energy originates in this case from the local hole hopping within the orbital polaron leading to the localization of a hole and its large effective mass. This process is also accompanied by a decrease of the QP spectral weight which is particularly striking for the $\left|x^{2}-z^{2}\right\rangle /\left|y^{2}-z^{2}\right\rangle(\phi=\pi / 12)$ orbital ordering (Table I).

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