# SUSY MASS RECONSTRUCTION METHODS IN ATLAS\*

# SANDRINE LAPLACE

## On behalf of the ATLAS Collaboration

## Laboratoire d'Annecy-le-Vieux de Physique des Particules LAPP IN2P3/CNRS, Université de Savoie 9 Chemin de Bellevue, BP 110 F-74941 Annecy-le-Vieux CEDEX, France

## (Received November 15, 2006)

Methods to measure the sparticle masses with the ATLAS detector at the LHC are reported. The supersymmetric phenomenology is first briefly discussed in the context of the mSUGRA constrained model. Many examples of recent studies aiming at measuring the sparticle masses are then described. Most of these examples are based on recent full simulation of the ATLAS detector.

PACS numbers: 12.60.Jv, 14.80.Ly

#### 1. Introduction

The ATLAS experiment [1] at LHC will search for Supersymmetry (SUSY), one of the most attractive extension of the Standard Model (SM) that pairs fermions and bosons to solve the hierarchy problem. The minimal *R*-parity conserving SUSY extension of the SM (MSSM)<sup>1</sup> brings 105 additional free parameters to those of the SM, thus preventing a systematic study of the full parameter space. Most of these new parameters appear during the soft breaking of SUSY and one can thus reduce their number by constraining this breaking. The mSUGRA model [2], in which the breaking is transmitted from the hidden sector to the observable sector by gravity, assumes that the gauginos and scalars masses, as well as the trilinear couplings, are unified at the GUT scale, leading to only 5 fundamental parameters: respectively  $m_{1/2}$ ,  $m_0$  and  $A_0$  for the previously cited parameters, as well as

<sup>\*</sup> Presented at the "Physics at LHC" Conference, Kraków, Poland, July 3–8, 2006.

<sup>&</sup>lt;sup>1</sup> The MSSM contains terms that violate the baryon (B) and lepton (L) numbers conservation. The *R*-parity, defined as  $R = (-1)^{3(B-L)+2s}$ , is a symmetry that forbids these terms.

 $\tan \beta$ , the ratio of the vacuum expectation values of the scalar fields and  $\operatorname{sgn}(\mu)$ , the sign of the Higgsino mass term. Constraints on mSUGRA are usually displayed in the  $m_0 - m_{1/2}$  plane, fixing the remaining 3 parameters to characteristic values, as shown in Fig. 1.



Fig. 1. The bottom triangular area is theoretically excluded (the LSP is the lightest stau and is thus charged); the light (bottom-left) area is favored by g - 2; the dark line area is favored by WMAP. The spin-independent elastic-scattering cross-sections are also shown and labeled by their exponents in units of picobarns. Generic decay chains originating from a gluino (right, top) or a squark (right, bottom).

The measurements from WMAP,  $b \to s\gamma$  and g-2 put strong constraints on this plane. In particular, the dark matter (thus the Lightest Supersymmetric Particle, LSP) density should be kept low according to the WMAP measurement, and the allowed regions are thus those where the LSP annihilation is large: the *bulk* at small  $m_0$ ,  $m_{1/2}$  values (LSP =  $\tilde{\chi}_1^0$ ), where sleptons<sup>2</sup> are light, allows a large  $\chi\chi$  annihilation by slepton exchange in the *t*-channel; the *stau co-annihilation* region (small  $m_0$ , LSP =  $\tilde{\chi}_1^0$ ) where  $m_{\text{LSP}} \simeq m_{\tilde{\tau}}$ allowing for a large  $\tilde{\tau}\chi$  annihilation; the *focus point* (small  $m_{1/2}$ ) where the LSP is mostly a Higgsino allowing a large annihilation into W and Z.

The *R*-parity conservation implies that the LSP is stable. It is not detected and leads to significant missing transverse energy  $(\not\!\!\!E_T)$ . On the one hand, this provides a distinct signature for the SUSY events compared to the SM events, but on the another hand this prevents the reconstruction of the full event and thus of the mass peaks. Instead, one has to exploit the kinematics of long decay chains, such as those shown in Fig. 1, originating

 $<sup>^2</sup>$  Note that in this report, the word "sleptons" stands for selectrons and smuons. Staus are explicitly designated as such.

from gluino or squark production. Note that these chains produce many jets and leptons. Which route is being taken from  $\tilde{g}\tilde{g}$ ,  $\tilde{g}\tilde{q}$  or  $\tilde{q}\tilde{q}$  production down to the LSP depends on which decay channels are opened and their branching ratio.

Understanding SUSY is usually done in three steps: the first step is to discover SUSY by an inclusive search; the second step is to look for particular SUSY signatures to measure the sparticle masses; the third step is to find back the fundamental model parameters from the measured masses. This report mainly concerns the second step, but the next section shortly describes the first step as well.

# 2. Discovering SUSY

The value of  $M_{\text{eff}}$  at which the signal exceeds the SM backgrounds, provides a first estimate of the SUSY masses  $(m_{\text{SUSY}} = \min(m_{\tilde{g}}, m_{\tilde{q}}))$  [4,5], as shown in Fig. 2 (right).



Fig. 2. Left: Distributions of  $M_{\text{eff}}$  for the SUSY signal (error bars) and the SM background (full line) simulated with PYTHIA (parton shower generator). The signal went through a full ATLAS simulation, but not the background. Note that simulating the background from a matrix element generator such as ALPGEN would increase it by a factor 2 to 3. Right: Correlation between  $M_{\text{eff}}$  and  $m_{\text{SUSY}}$ .

## 3. Sparticle mass measurement using the endpoint method

3.1. Looking at  $\tilde{q}_L \to \tilde{\chi}_2^0 q \to \tilde{l}_R lq \to \tilde{\chi}_1^0 llq$  (SPS1a Point)

The  $\tilde{q}_{\rm L} \rightarrow \tilde{\chi}_2^0 q \rightarrow \tilde{l}_{\rm R} lq \rightarrow \tilde{\chi}_1^0 llq$  decay chain (bottom, right in Fig. 1) allows to measure the masses of the  $\tilde{q}_{\rm L}^{\ 3}$ ,  $\tilde{l}_{\rm R}$ ,  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_1^0$  sparticles. This decay chain occurs in a large region of the  $m_0 - m_{1/2}$  plane, in particular along the SPS1a line defined by  $m_0 = -A_0 = 0.4 \ m_{1/2}$ ,  $\tan \beta = 10$  and  $\operatorname{sgn}(\mu) = + [6]$ .

One computes various invariant masses of the visible products in this decay chain: their endpoints correspond to particular kinematic configurations driven by the masses of the sparticles contained in the chain. Since many sparticles enter the chain, one needs to measure several endpoints in order to unambiguously determine the masses.



Fig. 3. Invariant mass of the dilepton (left) and quark–lepton–lepton (right) systems [6] for 300 fb<sup>-1</sup> (fast simulation [7], SPS1a point). The SF (resp. DF) curve shows the same flavor (resp. different flavor) SUSY events. After DF subtraction, one obtains the black dots which overlays with the signal chain (SC). The lower curve shows the SM background.

Most of the background comes from SUSY itself: the opposite-sign SUSY events have correlated (*e.g.* same flavor, SF) and uncorrelated (*e.g.* 50% SF, 50% different flavour, DF) lepton sources, the latter being dom-

620

<sup>&</sup>lt;sup>3</sup> In mSUGRA,  $\tilde{\chi}_1^0$  in mostly a bino and  $\tilde{\chi}_2^0$  a wino. Therefore, the dominant decay channels are  $\tilde{q}_L \to q \tilde{\chi}_2^0$  and  $\tilde{q}_R \to q \tilde{\chi}_1^0$ : only  $\tilde{q}_L$  enters the long decay chains described here, whereas  $\tilde{q}_R$  decays directly to the LSP (its mass can still be measured via this short decay chain, though).

inant. The SF uncorrelated part can be subtracted using the DF events since the DF events have the same experimental characteristics as the SF events.

Fig. 3 shows the dilepton (ll) and quark–lepton–lepton (qll) invariant masses for the SUSY and SM events. The endpoints are fitted from these distributions to obtain the mass differences. The statistical error is usually negligible compared to systematic error due to the lepton or jet energy scale of respectively 0.1% and 1%.

The potential of extracting the masses from the endpoint measurements is evaluated with a toy Monte Carlo of 10000 experiments. The masses are not always unambiguously determined depending on which endpoints are considered. Fig. 4 shows the results of this study. The obtained masses are correlated via the LSP mass. With 300 fb<sup>-1</sup>, the masses are well determined.



Fig. 4. Sparticle masses (empty dark histograms) and mass differences (filled histograms) for the SPS1a point. The empty light histograms show the wrong solutions that are returned in 17% of the Monte Carlo experiments.

## 3.2. Dilepton endpoint in co-annihilation and focus points

To illustrate the dependence of the decay chain configuration on the mSUGRA point, the dilepton endpoints are shown in Fig. 5 for the coannihilation and focus points [8].

In the co-annihilation point, both the right-handed and left-handed slepton masses are lower (but close) than the  $\tilde{\chi}_2^0$  mass. Therefore, both kinds of sleptons are produced in the decay chain inducing two endpoints in the dilepton invariant mass distribution.

In the focus point,  $m_0$  is very large and thus the squarks and sfermions have masses above 2 TeV. The SUSY production is dominantly done via gaugino pairs but these events are hardly distinguishable from the SM. Only 10% of the SUSY production occurs via gluinos that decay to gauginos and jets. The gauginos decay directly to leptons. One looks at  $\tilde{\chi}_3^0 \to l l \tilde{\chi}_1^0$  and  $\tilde{\chi}_2^0 \to l l \tilde{\chi}_1^0$  and thus one observes two endpoints that measure the mass difference between the heavy gauginos and the LSP.

In both analyses, the SF–DF subtraction is used to remove the SUSY uncorrelated backgrounds. The plots show that the endpoints are well measurable already with less than 10  $\text{fb}^{-1}$ .



Fig. 5. Left: Dilepton invariant mass for the co-annihilation point (full simulation, 20.6 fb<sup>-1</sup>). The full (resp. dashed) curves corresponds to the left-handed (resp. right-handed) squark decay chains. After DF subtraction, one obtains the dots corresponding to the signal events. Right: Dilepton invariant mass for the focus point (full simulation, 6.9 fb<sup>-1</sup>). The empty (full) histograms shows the SF and DF distributions. Apart from the Z peak, one observes two endpoints measuring  $m_{\tilde{\chi}_1^0} - m_{\tilde{\chi}_1^0}$  and  $m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}^{-0}$ .

## 3.3. Sbottom and gluino masses

Several methods are foreseen to measure the sbottom and gluino masses using gluino-initiated decay chain with the gluino decaying to  $\tilde{b}b$ .

The first method [9] considers the events close to the dilepton endpoint: in this case, the LSP and the dilepton system are almost at rest in the  $\tilde{\chi}_2^0$  frame, and the  $\tilde{\chi}_2^0$  momentum can be approximated by the expression:

$$p_{\tilde{\chi}_{2}^{0}}^{-} \simeq p_{ll}^{-} \sqrt{1 - m_{\tilde{\chi}_{1}^{0}}/m_{ll}} \, ^{4}$$

If the  $\tilde{\chi}_1^0$  and  $\tilde{\chi}_2^0$  masses are known, one can then compute the sbottom mass as  $m_{\tilde{b}} = m(\tilde{\chi}_2^0 b)$  and the gluino mass as  $m_{\tilde{g}} = m(\tilde{\chi}_2^0 bb)$ . The correlation between these two invariant masses is shown in Fig. 6 (left): the off-diagonal events corresponds to badly associated *b*-jets and are thus removed.

622

<sup>&</sup>lt;sup>4</sup> Note that this approximation works well for the chosen point, but this would not be the case for other points where  $m_{\tilde{\ell}_T}$  is close to either  $m_{\tilde{\chi}_2^0}$  or  $m_{\tilde{\chi}_1^0}$ .

The spread of the remaining good events is due to the  $\tilde{\chi}_2^0$  momentum approximation. The gluino mass can be precisely measured with 300 fb<sup>-1</sup> as shown in Fig. 6 (right).



Fig. 6. Left: Correlation between  $m(\tilde{\chi}_2^0 b)$  and  $m(\tilde{\chi}_2^0 bb)$ . The off-diagonal events correspond to badly associated *b*-jets. Right: Gluino mass given by  $m(\tilde{\chi}_2^0 bb)$  for 300 fb<sup>-1</sup>, fast simulation.

Fig. 7 (left) shows the difference  $m(\tilde{\chi}_2^0 bb) - m(\tilde{\chi}_2^0 b)$  in which the spread due to the  $\tilde{\chi}_2^0$  momentum approximation is factored out. The two states  $\tilde{b}_1$  and  $\tilde{b}_2$  are not well separated but can still be distinguished with a large luminosity (300 fb<sup>-1</sup>).



Fig. 7. Left: Sbottom mass given by  $m(\tilde{\chi}_2^0 b)$ . The two states of the sbottom quarks are distinguishable with 300 fb<sup>-1</sup>. Right: The two solutions of the Mass Reconstruction Method. The two sbottom peaks are well separated.

### S. LAPLACE

The second method [10], called the Mass Reconstruction Method, makes use of all the events. The idea is to completely solve the kinematics of the SUSY cascade decay by using the assumption that the selected events satisfy the same mass shell conditions of the sparticles involved in the cascade decay. Knowing the  $\tilde{\chi}_1^0$ ,  $\tilde{l}_R$  and  $\tilde{\chi}_2^0$  masses, one can determine the gluino and sbottom mass and discriminate the two sbottom states.

A third method makes use of additional endpoints using the quark from the gluino decay into  $\tilde{l}_{\rm L}$ . It is not described here, see [11] for more details.

## 3.4. Conclusion

At a few months of the LHC startup, a new era has started in the ATLAS experiment: a large scale production of Monte Carlo events using the full detector simulation is currently being analyzed. Systematic errors are being more precisely inferred and methods are being developed to evaluate the backgrounds more precisely. Also, new models and new analysis techniques are being investigated. In most models, a few fb<sup>-1</sup> are sufficient to observe squarks and gluinos up to a mass of 1 or 2 TeV/ $c^2$  and sleptons up to 300 GeV/ $c^2$  and to precisely measure their mass using cascade decays.

I would like to thank E. Richter-Was, D. Zervas, R. Lafaye, S. Asai and D. Tovey and the members of the ATLAS SUSY working group for their useful input to the presentation.

### REFERENCES

- ATLAS Collaboration, ATLAS TDR, CERN/LHCC/99-14, http://atlasinfo.cern.ch/Atlas/GROUPS/PHYSICS/TDR/access.html
- [2] L. Alvarez-Gaume, J. Polchinski, M.B. Wise, Nucl. Phys. B221, 495 (1983);
  L. Ibanez, Phys. Lett. B118, 73 (1982); J. Ellis, D.V. Nanopoulos, K. Tamvakis, Phys. Lett. B121, 123, (1983).
- [3] J.R. Ellis, K.A. Olive, Y. Santoso, V.C. Spanos, *Phys. Rev.* D71, 095007 (2005).
- [4] I. Hinchliffe, F.E. Paige, M.D. Shapiro, J. Soderqvist, W. Yao, *Phys. Rev.* D55, 5520 (1997).
- [5] D.R. Tovey, *Phys. Lett.* **B498**, 1 (2001).
- [6] B.K. Gjelsten, D.J. Miller, P. Osland, J. High Energy Phys. 0412, 003 (2004).
- [7] E. Richter-Was, D. Froidevaux, L. Poggioli, ATLFAST 2.0: A fast simulation Package for ATLAS, ATL-PHYS-98-131 (1998).
- [8] I. Borjanovic [ATLAS Collaboration], PoS HEP2005, 350 (2006).

- [9] B.K. Gjelsten, E. Lytken, D.J. Miller, P. Osland, G. Polesello, ATL-PHYS-2004-007.
- [10] K. Kawagoe, M.M. Nojiri, G. Polesello, Phys. Rev. D71, 035008 (2005).
- [11] B.K. Gjelsten, D.J. Miller, P. Osland, J. High Energy Phys. 0506, 015 (2005).