

# SATURATION AND SCALING OF MULTIPLICITY MEAN $p_T$ AND $p_T$ DISTRIBUTIONS FROM $200 \text{ GeV} \leq \sqrt{s} \leq 7 \text{ TeV}$ — ADDENDUM

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In the previous paper we have argued that the LHC data on multiplicity, average transverse momentum, and charged particle transverse momentum distributions are well described with minimal modeling in terms of a saturation scale  $Q_{\text{sat}}(s)$ . As a consequence, the  $p_T$  spectra should exhibit geometric scaling. In this short note we show that recently released CMS data at  $\sqrt{s} = 0.9, 2.36$  and  $7 \text{ TeV}$  fall on a universal curve when plotted in terms of suitably defined scaling variable  $\tau$ .

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In Ref. [1] we argued that the LHC data can be naturally described by assuming that particles in  $pp$  high energy collisions are produced from a saturated gluonic matter characterized by a saturation scale  $Q_{\text{sat}}^2(s) \sim Q_0^2(s_0/s)^{\lambda/2}$ , where  $Q_0 \sim 1 \text{ GeV}$  and  $s_0$  is the energy scale that depends on the observable in question. Power  $\lambda \sim 0.2 \div 0.3$  is related to the growth of the gluon distribution in proton with decreasing Bjorken  $x$  as measured at HERA [2]. This behavior has a natural explanation within the theory of saturation and the Color Glass Condensate. For details and relevant references we refer the reader to Ref. [1].

In Ref. [1] we have argued that if the saturation momentum is the only scale that controls  $p_T$  distributions, on dimensional grounds, these distributions should have a geometrical scaling [2]

$$\frac{dN_{\text{ch}}}{dy dp_T^2} = \frac{1}{Q_0^2} F(\tau), \quad (1)$$

where  $Q_0 \sim 1$  GeV has been factorized for convenience. Function  $F(\tau)$  is a *universal, energy independent*, dimensionless function of dimensionless scaling variable

$$\tau = \frac{p_T^2}{Q_0^2} \left( \frac{p_T}{W} \right)^\lambda, \quad (2)$$

where  $W \sim \sqrt{s}$  (in Ref. [1]  $W = \sqrt{s} \times 10^{-3}$  if all energy scales are in GeV).

At the time when Ref. [1] was published the  $p_T$  distributions measured by CMS [3] have not been publicly accessible yet. Therefore, we had to perform our analysis using Tsallis parametrizations of the CMS data. Now, when  $p_T$  distributions are available from the Durham Reaction Data Base [4], we repeat our analysis on the real data. In Fig. 1 we plot  $d^2N_{\text{ch}}/dyd^2p_T$  for full

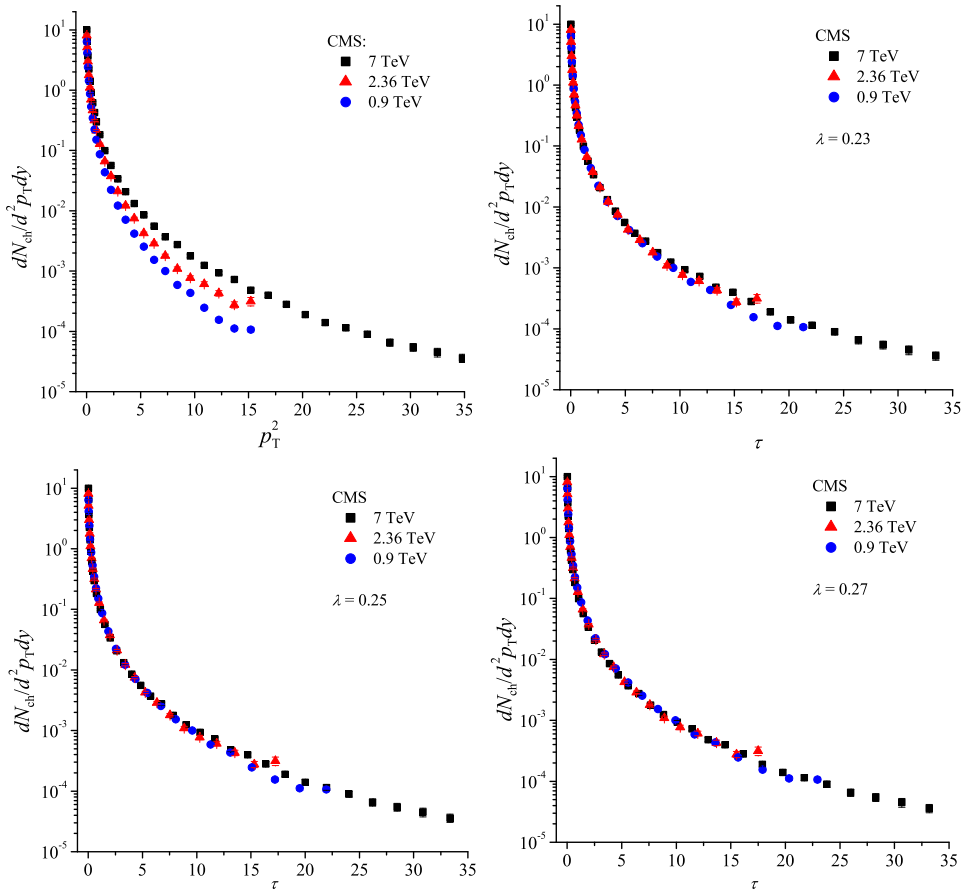


Fig. 1. Geometric scaling of the transverse momentum spectra that are plotted in terms of  $p_T^2$  and scaling variable  $\tau$  for three choices of  $\lambda = 0.23, 0.25$  and  $0.27$ .

CMS (pseudo)rapidity range  $|\eta| < 2.4$  firstly as a function of  $p_T^2$  (*i.e.* for  $\tau(\lambda = 0)$ ) and then as a function of scaling variable  $\tau$  for three choices of  $\lambda = 0.23, 0.25$  and  $0.27$ . We see that indeed the data follow the universal curve exhibiting geometric scaling. The quality of scaling depends on the actual value of  $\lambda$  and is best for the larger values shown. For all three choices examined in this note, the quality is very impressive. Similar conclusion can be drawn for the UA1 data on  $p\bar{p}$  [5] as shown in Fig. 2.

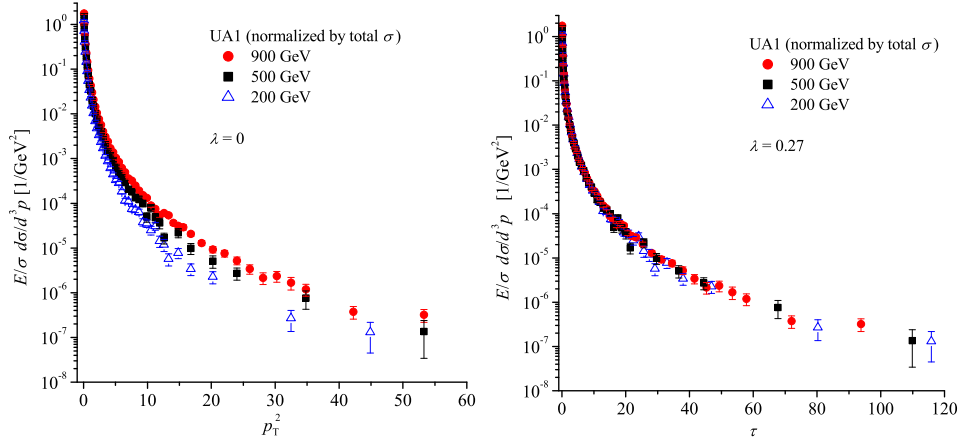


Fig. 2. Geometric scaling of the transverse momentum spectra that are plotted in terms of  $p_T^2$  and scaling variable  $\tau$  for  $\lambda = 0.27$ . Data points taken from Ref. [5] are normalized by total cross-section as given in Ref. [6].

We also show in Fig. 3 the fits to the central rapidity multiplicity and the average transverse momentum at central rapidity for the values of  $\lambda$  that describe the geometrical scaling in the transverse momentum distributions. The data on multiplicity show a slight preference for the smaller  $\lambda$  values, but the description is quite good for all values.

This small difference between the two powers (the power  $\lambda$  preferred by geometrical scaling and  $\lambda$  that fits multiplicity and  $\langle p_T \rangle$  growth with energy) can be easily understood as a consequence of geometrical scaling. Indeed

$$\frac{dN_{\text{ch}}}{dy} = \int \frac{d^2 p_T}{Q_0^2} F(\tau). \quad (3)$$

Simple change of variables gives

$$\frac{d p_T^2}{Q_0^2} = \frac{2}{2 + \lambda} \left( \frac{W}{Q_0} \right)^{\frac{2\lambda}{2 + \lambda}} \tau^{-\frac{\lambda}{2 + \lambda}} d\tau. \quad (4)$$

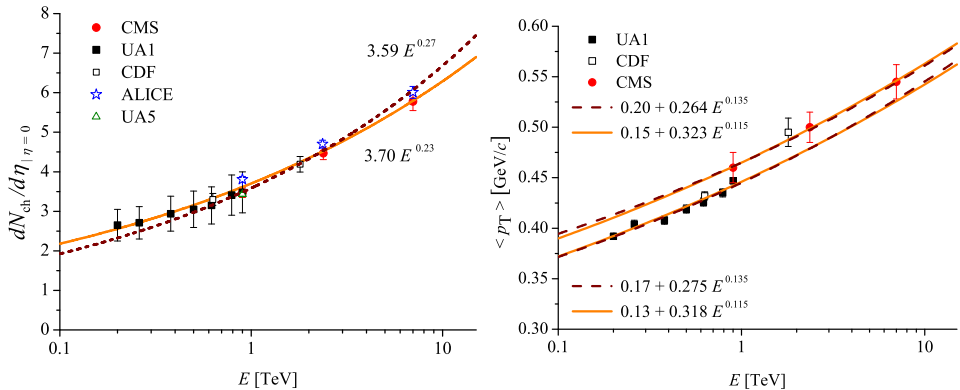


Fig. 3. Central multiplicity density and average  $p_T$  as functions of energy, plotted for energy dependence corresponding to the two  $\lambda$  values:  $\lambda = 0.23, 0.27$ . Experimental data are taken from Refs. [3] (CMS), [5] (UA1), [7] (UA5), [8] (CDF) and [9] (Alice).

The integral over  $d\tau$  is convergent and *universal*, *i.e.* it does not depend on energy. It follows from Eq. (4) that the effective power of the multiplicity growth is

$$\lambda_{\text{eff}} = \frac{2\lambda}{2 + \lambda} < \lambda \quad (5)$$

rather than  $\lambda$ . For  $\lambda = 0.27$  we have that  $\lambda_{\text{eff}} = 0.238$ .

It should be noted that in evolution equations, the parameter  $\lambda$  is of the order of  $\alpha_S$ . The deviation between  $\lambda_{\text{eff}}$  and  $\lambda$  is, therefore, of the order of  $\alpha_S^2$ . This gives us an estimate of the uncertainty of our considerations due to higher order effects. A proper treatment that builds in logarithmic corrections and corrections due to impact parameter may be expected to generate deviations from our results. It is quite exceptional that our naive considerations work so well.

In the meantime, after the publication of Ref. [1], other authors have undertaken a more ambitious task to calculate particle spectra from the models based on Color Glass Condensate that incorporate both HERA and RHIC data [10]. These studies show indeed that saturated gluonic matter dominates particle production in  $\gamma p$  collisions at small Bjorken  $x$  and in heavy ion and  $pp$  collisions at high energies. If so, some universal features must be present in the data of these three different reactions. Geometric scaling [2], as shown in Ref. [1] and in the present note, is one of them.

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