TIME-DEPENDENT CP VIOLATION AND MIXING AT B FACTORIES*

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In the last decade, two *B*-factory experiments, BaBar and Belle performed a large number of measurements related to time-dependent CP violation and $B-\overline{B}^0$ mixing. Achievements of those measurements are reviewed and possible room for New Physics is discussed.

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1. Introduction

In the Standard Model (SM) of elementary particle physics, CP violation in the quark sector is described by the Kobayashi–Maskawa (KM) theory [1]. In the KM scheme, a quark-mixing matrix has an irreducible complex phase that gives rise to CP-violating asymmetries. The quark-mixing matrix is written as [2]

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} , (1)$$

where V_{ub} and V_{td} have CP-violating complex phases. Due to the unitarity condition of this matrix, the following relation is expected to hold

$$V_{td}V_{tb}^* + V_{cd}V_{cb}^* + V_{ud}V_{ub}^* = 0.$$
 (2)

The CP-violating phenomena in B meson decays are related to the angles ϕ_1 , ϕ_2 and ϕ_3 defined as shown in Fig. 1. Here, the phase of V_{td} plays a fundamental role to cause CP violation by the interference with V_{cb} and V_{ub} resulting in determination of the CP-violating angles, ϕ_1 and ϕ_2 [3],

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Fig. 1. The unitarity triangle. The CP violation parameters are defined as the angles ϕ_1 , ϕ_2 and ϕ_3 .

respectively. The angle ϕ_3 is determined by the direct CP asymmetries in $B \to DK^{(*)}$ decays and mentioned in detail elsewhere [4]. Since V_{td} takes part through $B^0 - \overline{B}^0$ mixing, a measurement of time evolution of a B meson pair is required to see CP violation phenomena. In addition, since a B meson is so heavy that many decay modes are available, the branching fraction to the modes usable for CP violation is limited. Thus, huge $(\mathcal{O}(10^8))$ amount of B mesons is necessary.

In order to satisfy these requirements, two asymmetric-energy e^+e^- collider *B*-factory machines, KEKB and PEP-II were built at KEK and SLAC, respectively. Both achieved a peak luminosity of more than 10^{34} cm⁻²s⁻¹ and the KEKB integrated luminosity reached 1000 fb⁻¹ while PEP-II realized 550 fb⁻¹. Thanks to efficient operation of these machines, the recorded number of *B* meson pairs has been found to be 772 M $B\overline{B}$ at Belle and 470 M $B\overline{B}$ at BaBar. In this report, we discuss experimental tests of Kobayashi– Maskawa theory and search for New Physics through time-dependent measurements in the *B* meson system using these rich statistics data samples.

2. Time-dependent measurements of B meson system

By a measurement of time evolution of B meson pairs, we can get constraints for CP-violating angles, ϕ_1 and ϕ_2 , as well as the $B^0 - \overline{B}^0$ mixing parameter Δm_d . In the decay chain $\Upsilon(4S) \to B^0 \overline{B}^0 \to f_{\rm CP} f_{\rm tag}$, where one of the B mesons decays at time $t_{\rm CP}$ to a CP eigenstate $f_{\rm CP}$ and the other decays at time $t_{\rm tag}$ to a final state $f_{\rm tag}$ that distinguishes between B^0 and \overline{B}^0 , the decay rate has a time dependence on the $\Upsilon(4S)$ rest frame [5] given by

$$\mathcal{P}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left\{ 1 + q \left[\mathcal{S}\sin(\Delta m_d \Delta t) + \mathcal{A}\cos(\Delta m_d \Delta t) \right] \right\}.$$
 (3)

Here \mathcal{S} and \mathcal{A} are CP-violation parameters, τ_{B^0} is the B^0 lifetime, Δm_d is the mass difference between the two neutral B mass eigenstates, $\Delta t = t_{\rm CP} - t_{\rm tag}$,

and the *b*-flavor charge q = +1 (-1) when the tagging *B* meson is a $B^0 \left(\overline{B}^0\right)$. By selecting the neutral *B* decays into $f_{\rm CP}$ via the amplitudes containing no complex phase, the CP violation is caused by the interference between decay and V_{td} in mixing to give ϕ_1 determination, while the CP asymmetry is related to ϕ_2 in the case of $b \to u$ transition induced decays.

Instead of the *B* decays into $f_{\rm CP}$, collecting the events in which one neutral *B* meson decays into the flavor-specific final state enables us to determine the $B^0-\overline{B}^0$ mixing parameter Δm_d , by measuring opposite-same flavor asymmetry as a function of Δt . In this section, experimental determinations of these quantities are reviewed.

2.1. Measurements of $sin2\phi_1$

For the $b \to c\bar{c}s$ transition induced decay of the neutral B meson such as $B^0 \to (c\bar{c})K^0$, the SM predicts $S = -\xi_f \sin 2\phi_1$ and $\mathcal{A} = 0$ with very small theoretical uncertainty [5], where $\xi_f = +1$ (-1) corresponds to CP-even (-odd) final states and ϕ_1 is one of the three interior angles of the most symmetric KM unitarity triangle, defined as $\phi_1 \equiv \arg(-V_{cd}V_{cb}^*/V_{td}V_{tb}^*)$ [3]. Therefore, the BaBar and Belle collaborations have published increasingly more precise determinations of $\sin 2\phi_1$ [6,7]. The latest measurements were reported with $465 \times 10^6 \ B\overline{B}$ and $535 \times 10^6 \ B\overline{B}$ by BaBar [8] and Belle [9], respectively.

More recently, thanks to the successful operation of the KEKB accelerator, Belle accumulated 772 M $B\overline{B}$ on the $\Upsilon(4S)$ resonance by the end of its operation. Out of those, 620 M $B\overline{B}$ collected by the newer detector configuration with a 1.5 cm radius beampipe, a 4-layer silicon vertex detector and a small-cell inner drift chamber have been reprocessed with an improved charged track reconstruction algorithm and a finely returned CsI crystal hit threshold of shower reconstruction in the electromagnetic calorimeter. Using this large statistics data, Belle has recently performed its final measurement of $\sin 2\phi_1$ [10]. The *B* decays to the CP-odd eigenstates, $f_{\rm CP} = J/\psi K_{\rm S}^0, \psi(2S) K_{\rm S}^0$ and $\chi_{c1} K_{\rm S}^0$, and the CP-even eigenstate, $f_{\rm CP} = J/\psi K_L^0$ are reconstructed. As shown in Fig. 2, the $B^0 \to f_{\rm CP}$ decay signal other than $J/\psi K_L^0$ is identified by two kinematic variables calculated in the $\Upsilon(4S)$ rest frame (cms): the energy difference $\Delta E \equiv E_B^* - E_{\rm beam}^*$ and the beam-energy constrained mass $M_{\rm bc} \equiv \sqrt{(E_{\rm beam}^*)^2 - (p_B^*)^2}$, where $E_{\rm beam}^*$ is the beam energy in cms of the $\Upsilon(4S)$ resonance, and E_B^* and p_B^* are the cms energy and momentum of the reconstructed *B* candidate, respectively.

 $B^0 \rightarrow J/\psi K_L^0$ candidates are identified by the value of p_B^* calculated using a two-body decay kinematic assumption. In total, the signal yield of the CP-odd modes is 15560 events and $J/\psi K_L^0$ signal is obtained to be 10040 events. Taking flavor tagging [11] and reconstruction of $f_{\rm CP}$ as well as



Fig. 2. (color online) $M_{\rm bc}$ distribution within the ΔE signal region for $B^0 \rightarrow J/\psi K_{\rm S}^0$ (black), $\psi(2S)K_{\rm S}^0$ (blue) and $\chi_{c1}K_{\rm S}^0$ (magenta), the superimposed curve (red) shows the fit result from all those modes combined (top) and p_B^* distribution $B^0 \rightarrow J/\psi K_L^0$ candidates with the results of the fit separately indicated as signal (open histogram), background events with a real J/ψ and a real K_L^0 (pale grey/yellow), with a real J/ψ without a real K_L^0 (grey/green) and without a real J/ψ (dark grey/blue) (bottom).



Fig. 3. (color online) The background-subtracted Δt distribution for q = +1 (grey/red) and q = -1 (black/blue) events and asymmetry for good tag quality events in $(c\bar{c})K_{\rm S}^0$ (left) and $J/\psi K_{\rm S}^0$ (right) cases.

 f_{tag} vertices [12] into account, an unbinned maximum likelihood fit is done in the Δt distribution with the formula (3), two CP violation parameters, $\sin 2\phi_1 = -\xi_f S$ and A are obtained to be

$$\sin 2\phi_1 = 0.667 \pm 0.023 (\text{stat}) \pm 0.012 (\text{syst}), \qquad (4)$$

$$\mathcal{A} = 0.006 \pm 0.016(\text{stat}) \pm 0.012(\text{syst}).$$
(5)

The background-subtracted Δt distribution for q = +1 and q = -1events and asymmetry for good tag quality events are shown in Fig. 3. The world average of $\sin 2\phi_1$ is now 0.68 ± 0.02 that is a firm SM reference.

2.2. Measurements of CP violation in $B^0 \rightarrow D^+D^$ and $D^{*+}D^{*-}$ decays

In SM, $b \rightarrow c\bar{c}d$ transition induced neutral B meson decays also provide a possibility to access the CP violation angle ϕ_1 because leading order diagram of the decay amplitude contain same weak phase as $b \rightarrow c\bar{c}s$ case. On the other hand, if the $b \rightarrow d$ penguin diagram contribution or other New Physics effect are substantial, a precise measurement of CP violation in $b \rightarrow c\bar{c}d$ induced decay may reveal a deviation from the standard $\sin 2\phi_1$ measurement. The tree diagram of $B^0 \to D^+ D^-$ and $D^{*+} D^{*-}$ decays is the color favored one among $b \rightarrow c\bar{c}d$ amplitudes. These decay modes have been revisited by Belle using its full integrated luminosity accumulated at the $\Upsilon(4S)$ resonance. For $B^0 \to D^+D^-$, we get $\mathcal{S} = -1.06^{+0.21}_{-0.14} \pm 0.08$ and $\mathcal{A} = +0.43 \pm 0.16 \pm 0.08$ [13]. \mathcal{A} has decreased compared to the previous Belle publication with 535 M $B\overline{B}$ pairs [14] within a statistically consistent range. In $B^0 \to D^{*+}D^{*-}$, the CP violation parameters are measured to be $S = -0.79 \pm 0.13 \pm 0.03$ and $A = +0.15 \pm 0.08 \pm 0.02$. Especially in this mode, as a result of data reprocessing, the signal yield from 772 M BB pairs is 2.2 times larger than the yield with 657 M $B\overline{B}$ sample used in the previous result [15]. It gives us significant improvement, CP violation parameters' errors are down to 60% with respect to the previous publication. In spite of the improvement of this measurement precision, we observed no significant deviation from the SM expectation so far.

2.3. Determination of ϕ_2

In *B* decays into proper $f_{\rm CP}$ mediated by the $b \to u$ transition, its complex phase interferes with $B^0 - \overline{B}^0$ mixing and results in the CP violation that can determine the angle ϕ_2 . There would be the $b \to d$ penguin contribution that cause a complexity to extract the angle ϕ_2 from the observed CP violation, however we can solve it by isospin analysis. As the *B* decay final states to obtain ϕ_2 , there are three possibilities; $\pi\pi$, $\rho\rho$ and $\rho\pi$. From the $\pi\pi$ [16, 17], $\rho\rho$ [18, 19] and $\rho\pi$ [18, 19] modes, ϕ_2 is determined to be $(89.0^{+4.4}_{-4.2})^{\circ}$. In addition, the measurements related to the $a_1\pi$ decay mode have been performed [20, 21] which can determine effective ϕ_2 .

2.4. Measurements of Δm_d

By selecting the flavor specific final state of the neutral B meson decay, we can determine the $B^0 - \overline{B}^0$ mixing parameter Δm_d by measuring time evolution of opposite-same flavor asymmetry. For this purpose, semileptonic $\overline{B^0} \to D^{*+} \ell^- \bar{\nu}$ decay is the most suitable process because of its relatively high branching fraction and absence of the tag side interference. Based on a 88 M $B\overline{B}$ sample, BaBar took a partial reconstruction approach for the neutral B meson decay to the $D^{*+}\ell^-\bar{\nu}$ final state and the accompanying B meson flavor is identified by a high momentum lepton [22]. Belle applied a full reconstruction method for $\overline{B}^{0} \to D^{*+} \ell^{-} \bar{\nu}$ as well as hadronic decays such as $\overline{B}^0 \to D^{(*)+}\pi^-$, $D^{*+}\rho^-$ using a 152 M $B\overline{B}$ sample, and opposite side B flavor is tagged by the same method as the one for other time-dependent CP violation measurements [23]. BaBar and Belle results are approximately 5 times more precise than LEP and Tevatron experiments. Now the world average is obtained to be $\Delta m_d = 0.507 \pm 0.004 \text{ ps}^{-1}$, 1% precision has been achieved. This gives another reference point to constrain a unitarity triangle, *i.e.* $|V_{td}|$ in the SM framework.

3. Tension with $\mathcal{B}(B^+ \to \tau^+ \nu_{\tau})$ and room for New Physics

The KM scheme has been tested, however there is a noticeable tension reaching a 2.8 σ level between the global fit without $\mathcal{B}(B^+ \to \tau^+ \nu_{\tau})$ and experimental measurements of it, where a sin $2\phi_1$ measurement gives a stringent constraint on the former. Of course, New Physics (NP) could be present in $B^+ \to \tau^+ \nu_{\tau}$ process, thus we need an update of this measurement. However, in this section, other possible room to accommodate NP is to be discussed. As explained in Sec. 2.1, the time-dependent CP violation is the result of interference between decay and mixing of the neutral B meson system. Here, if NP is substantial and has a different phase from the SM in $b \to c\bar{c}s$ decay amplitudes, it should cause direct CP violation in $B^{\pm} \to J/\psi K^{\pm}$. Including Belle latest measurement [24], no direct CP violation has been observed so far, $(1 \pm 7) \times 10^{-3}$ in PDG2011. Therefore, NP room is unlikely in $b \to c\bar{c}s$ decays, but there is room in $B^0-\overline{B}^0$ mixing.

4. Search for New Physics in $b \rightarrow s$ penguin modes

The *B* decays caused by the penguin diagrams are expected to be good at probing the New Physics effects beyond the SM, because of their one loop nature. In SM, $b \to s$ penguin mediated *B* decays such as $B^0 \to \phi K^0$, $B^0 \to \eta' K0$, $B^0 \to K^0_S K^0_S K^0_S$ are expected to have effective $\sin 2\phi_1 (\sin 2\phi_1^{\text{eff}})$ which is same as the $\sin 2\phi_1$ obtained by $b \to c\bar{c}s$ induced *B* decay such as $B^0 \to J/\psi K^0$.

Recently, because $\phi \to K^+K^-$, $f_0 \to K^+K^-$ and non-resonant contributions overlap (as do $\rho^0 \to \pi^+\pi^-$ and $f_0 \to \pi^+\pi^-$), time-dependent Dalitz analyses have been performed in three-body decays such as $B^0 \to (K^+K^-)K_{\rm S}^0$ and $B^0 \to (\pi^+\pi^-)K_{\rm S}^0$ to resolve those overlapping contributions at the amplitude level. A statistical error is still dominant in the precision of $\sin 2\phi_1^{\rm eff}$ of $b \to s$ mediated *B* decays, typically $0.1 \sim 0.2$ [25]. Thus in order to obtain sensitivity in $\sin 2\phi_1^{\rm eff}$ of $\mathcal{O}(10^{-2})$, we need an integrated luminosity of $\mathcal{O}(10ab^{-1})$. This fact requires a Super *B*-factory as well as LHCb experiment results.

5. Summary

 $\sin 2\phi_1$ is now determined to be 0.68 ± 0.02 in world average, it is a firm SM reference point. Another CP violation angle ϕ_2 is constrained to be $89.0^{+4.4} - 4.2^{\circ}$, then the unitarity triangle appears to be a right triangle. Δm_d is precisely measured by *B* factories, 1% precision has been achieved and it gives another firm reference. Tension around $\mathcal{B}(B^+ \to \tau^+ \nu_{\tau})$ urges an update of measurement, while comparing to $\sin 2\phi_1$, we expect mixing has room for NP. In order to hunt for a NP effect by CP violation measurements in $\mathcal{O}(10^{-2})$ sensitivity, LHCb results and super *B*-factory experiments are awaited.

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