

FROM CHIRAL  $NN(N)$  INTERACTIONS TO GIANT AND PYGMY RESONANCES VIA EXTENDED RPA\*

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The properties of giant and pygmy resonances are calculated starting from chiral two- and three-nucleon interactions. The aim is to assess the predictive power of modern Hamiltonians and especially the role of the three-nucleon force. Methods based on the random-phase approximation (RPA) provide an optimal description of the modes of interest with minimal computational requirements. Here, we discuss the giant resonances (GRs) of  $^{40,48}\text{Ca}$  isotopes and their low-energy dipole response. A comparison with previous results obtained with a transformed Argonne V18 two-nucleon potential points to certain improvements.

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**1. Introduction**

A starting point for nuclear structure theory ideally involves realistic two-plus-three nucleon ( $NN + NNN$ ) potentials and, most consistently, nuclear Hamiltonians derived from quantum chromodynamics. Starting from these interactions, unitary transformations can be employed, *e.g.* the Similarity Renormalization Group (SRG), to pre-diagonalize the Hamiltonian and to improve the convergence behavior of many-body methods. This approach has been applied successfully to light and medium-mass nuclei using interactions from chiral effective field theory ( $\chi\text{EFT}$ ) in the framework of the No-Core Shell Model and in Coupled-Cluster Theory and related methods.

In order to reach computationally heavy nuclei as well as higher-lying collective excitations, we have been exploring the performance of pre-diagonalized interactions within the Random Phase Approximation (RPA) and ex-

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tensions thereof, in particular the Second RPA (SRPA). A two-body Hamiltonian based on the Argonne V18 potential was used before in large-scale SRPA calculations [1] with promising results for giant resonances (GRs), notwithstanding the insufficient treatment of three-body effects. Since then,  $NN + NNN$   $\chi$ EFT interactions have become available [2, 3]. They can be utilized in a two-body formalism, by performing a normal ordering and neglecting the three-nucleon residual interaction — a truncation whose validity has been demonstrated [3]. Thanks to the above advances, we are now in a position to study collective phenomena with realistic potentials and with a reasonable computational effort.

As a linear-response theory, RPA would be the obvious many-body method of choice. There are two main reasons to go beyond first-order RPA, SRPA: The traditional phenomenologist's goal is to describe the resonances' fragmentation because of collisional damping. The many-body theorist's goal applicable here is convergence with respect to the model space, when the functional or interaction is not fitted to the mean field and RPA level.

This contribution focuses on recent results within RPA and SRPA [4] and the relevance of utilizing a realistic three-nucleon interaction.

## 2. Giant resonances

In the past, we employed the SRPA with the Argonne V18 potential transformed via the unitary correlation operator method (AV18+UCOM) and looked at the giant monopole resonance (GMR), giant dipole resonance (GDR), and giant quadrupole resonance (GQR) [1]. Within a 15-shell model space, a very good and almost-converged description of the GDR and GQR was obtained, including some very interesting applications in the observed fragmentation of the GQR [5, 6], but the energy of the GMR was underestimated. Overall, the energetic discrepancies were between, approximately,  $-10$  (GMR) to  $0$  (GQR) MeV. The calculated charge radii also were too small. We attributed the discrepancies to missing  $NNN$  effects.

One is now in a position to use  $NN + NNN$  interactions determined in a systematic way. The interaction used at present is a chiral  $NN$  (at  $N^3$ LO) and  $NNN$  (at  $N^2$ LO) interaction with a cutoff at 400 MeV, evolved within the SRG ( $\chi$ EFT+SRG). The  $NNN$  interaction is rewritten in a normal ordered form. The one- and two-body operators are kept, whereas the  $NNN$  residual interaction is neglected. Then the convenient two-nucleon formalism can be used.

Figure 1(a),(b) shows results for the GRs of the  $^{40,48}\text{Ca}$  isotopes obtained within a 13-shell model space. Previous results with the AV18+UCOM potential in the same space but within SRPA0 are shown for comparison, as well as experimental data. SRPA0 stands for the diagonal approximation [1],

whereby the couplings amongst the  $2p2h$  configurations are neglected. It has been found very good whenever tested against full SRPA. The energetic discrepancies, with respect to data, observed with the two potentials are of a different quality: When using the AV18+UCOM, the energies are underestimated, while with the use of the  $\chi$ EFT+SRG, they are overestimated. The latter results could be ameliorated still if we extend the harmonic-oscillator basis. The new results on GRs, therefore, constitute an improvement with respect to AV18+UCOM. However, the radii are still too small. In particular, the obtained values for the root-mean-square charge radii of  $^{16}\text{O}$ ,  $^{40}\text{Ca}$  and  $^{48}\text{Ca}$  are 2.41, 2.98 and 2.6 fm, to be compared with the measured values 2.70, 3.48 and 3.48 fm, respectively. Next, we may consider other versions of chiral interactions, for example the SAT family [7], or the new two-body Daejeon16 interaction [8], which promise improved radii.

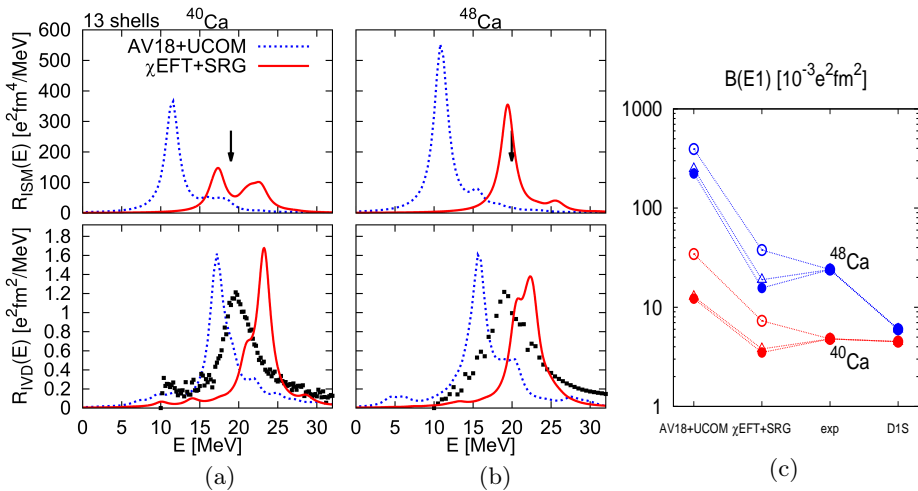


Fig. 1. (a), (b): The isoscalar monopole (ISM) and the isovector dipole (IVD) strength distributions of  $^{40,48}\text{Ca}$  calculated using the AV18+UCOM or the  $\chi$ EFT+SRG interaction. Measured centroid GR energies and photoabsorption data are displayed. (c)  $B(E1)\uparrow$  strength of the IS-LED. AV18+UCOM and  $\chi$ EFT+SRG: full points show the SRPA results, open symbols show the SRPA (triangles) and RPA results. Gogny DIS: only RPA. The experimental point for  $^{48}\text{Ca}$  includes the IV state in the immediate proximity of the IS-LED [10].

### 3. On the low-energy dipole spectrum

Another interesting benchmark, especially because it is qualitative, is the low-energy isovector (IV) dipole response of Ca isotopes and the nature of the low-energy isoscalar state (IS-LED) [9, 10]. The AV18+UCOM potential yields extremely strong low-energy transitions for  $^{40,48}\text{Ca}$  and pre-

dicts a neutron-skin oscillation for  $^{48}\text{Ca}$ . The result qualitatively contradicts observations [10]. Simple phenomenological corrections [11] could not improve this stiff result. Numerical results for the IS-LED in Ca with the new  $\chi\text{EFT}+\text{SRG } NN + NNN$  interaction are shown in Fig. 1 (c). They constitute an improvement of an order of magnitude. Furthermore, the IS-LED is not predicted to be a veritable neutron-skin oscillation in  $^{48}\text{Ca}$ . Whether the properties of a realistic  $NNN$  force are responsible for this outcome will have to be investigated using different  $NN(+NNN)$  potentials and different test nuclei.

#### 4. Prospects

The correct description of giant and pygmy resonances is a potential benchmark for chiral and other modern nuclear interactions. Results with a chiral  $NN + NNN$  potential are promising. Next, we shall examine the SAT family of chiral interactions and the two-nucleon Daejeon16 interaction. In the spirit of *ab initio* nuclear structure, we aim for a theoretical description of nuclear linear response based on chiral and, in general, microscopic interactions, for more-unbiased results and predictive power.

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