TESTING PRODUCTION SCENARIOS FOR (ANTI-)(HYPER-)NUCLEI WITH MULTIPLICITY-DEPENDENT MEASUREMENTS AT THE LHC*

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The production of light anti- and hyper-nuclei provides unique observables to characterise the system created in high-energy proton-proton (pp), proton-nucleus (pA) and nucleus-nucleus (AA) collisions. In particular, nuclei and hyper-nuclei are special objects with respect to non-composite hadrons (such as pions, kaons, protons, etc.), because their size is comparable to a fraction or the whole system created in the collision. Their formation is typically described within the framework of coalescence and thermal-statistical production models. In order to distinguish between the two production scenarios, we propose to measure the coalescence parameter B_A for different anti- and hyper-nuclei (that differ by mass, size and internal wave function) as a function of the size of the particle emitting source. The latter can be controlled by performing systematic measurements of light anti- and hyper-nuclei in different collision systems (pp, pA, AA) and as a function of the multiplicity of particles created in the collision. While it is often argued that the coalescence and the thermal model approach give very similar predictions for the production of light nuclei in heavy-ion collisions, our study shows that large differences can be expected for hypernuclei with extended wave functions, as the hyper-triton. We compare the model predictions with data from the ALICE experiment and we discuss perspectives for future measurements with the upgraded detectors during the High-Luminosity LHC phase in the next decade.

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1. Introduction: the "anti-nuclei" puzzle

The formation of light anti- and hyper-nuclei in high-energy protonproton (pp), proton-nucleus (pA) and nucleus-nucleus (AA) collisions provides unique observables for the study of the system created in these reactions, and can be used to understand both the internal structure and the formation mechanisms of loosely-bound composite objects. The production of (anti-)(hyper-)nuclei in high-energy collisions is commonly described by the following two distinct approaches: formation by nucleon coalescence at the system (kinetic) freeze-out [1-4] or thermal-statistical production at the chemical freeze-out [5, 6]. Thanks to the large data samples of pp, p-Pb and Pb–Pb collisions collected during the first ten years of operations of the CERN Large Hadron Collider (LHC), A Large Ion Collider Experiment (ALICE) Collaboration has measured the production of light nuclei and anti-nuclei at several centre-of-mass energies [7-12], thus providing a crucial experimental input and a boost to theoretical and phenomenological investigations [13-19]. In small collision systems, the experimental results seem to confirm the validity of the coalescence picture, with the most recent multiplicity-differential measurements pointing toward a dependence of the coalescence process on the volume of the particle-emitting source ("source size" hereafter). In heavy-ion collisions, coalescence approaches that do not take into account the source size are not able to reproduce the data. At the same time, the production of light nuclei, anti-nuclei and hyper-triton as measured in Pb–Pb collisions is found to be consistent with statisticalthermal model predictions and a non-zero deuteron elliptic flow is observed. This is surprising as (anti-)nuclei produced at chemical freeze-out are not expected to survive the hadronic phase: the deuteron is a "fragile object" when surrounded by the fireball created in heavy-ion collisions, because its binding energy $(B_E = 2.2 \text{ MeV})$ is much lower than the characteristic temperatures of the system ($T_{\rm chem} \approx 153$ MeV, $T_{\rm kin} \approx 100$ MeV). Moreover, the cross section for pion-induced deuteron breakup is significantly larger than the typical (pseudo)-elastic cross sections for the re-scattering of hadronic resonance decay products [19–22]. These observations pose the "(anti-)nuclei puzzle": how can loosely-bound composite objects survive in the dense and hot fireball, freeze-out and develop collective flow like the other light-flavour non-composite hadrons?

In our study [14], we have extended and combined known formalisms used to describe (anti-)(hyper-)nuclei production in order to allow, for the first time, a direct comparison of the thermal and coalescence models as well as a direct comparison to the ALICE data. Identifying the coalescence parameter (B_A) as the key observable, we present a consistent picture across different collision systems (pp, p-Pb, Pb-Pb) for light (anti-)(hyper-)nuclei with mass number A = 2, 3 and 4. We also suggest to address the open questions by looking at the production of nuclei and hyper-nuclei up to A = 4that differ by size and properties, measured as a function of multiplicity used as a proxy for the source size. Whereas the (anti-)deuteron production has been measured multi-differentially and quite precisely with the LHC Run 1 and 2 data, the study of heavier objects with A = 3 and 4 will greatly profit from the increase in integrated luminosity foreseen at the LHC Runs 3 and 4 in all collision systems [23]. A comprehension of (anti-)nuclei production mechanisms is not only relevant for nuclear and hadronic physics, but has applications in astrophysics and indirect dark matter searches [24]. In recent years, it has been suggested that the detection of light anti-nuclei in space could provide a signature for the presence of dark matter in the Cosmos, see for instance [25, 26]. Anti-deuterons and ³He might indeed be produced by coalescence of antiprotons and antineutrons coming from the annihilation of Weakly Interacting Massive Particles into Standard Model particles, for which anti-nuclei created in reactions between primary cosmic ray protons and interstellar matter (pp, pA collisions) represent a source of background.

The main features of the theoretical frameworks employed for our study are briefly summarised in Sec. 2, while we address the reader to [14] for the full details. Section 3 presents the main results and conclusions follow.

2. Modelling light (anti-)(hyper-)nuclei production

For our study, we consider nuclei and hyper-nuclei with mass number A = 2,3 and 4, whose properties are summarised in Table I. Those properties are the same as for their anti-matter counterparts and we assume that the same formation mechanisms are at play for matter and anti-matter¹. Nuclei and hyper-nuclei are special objects with respect to non-composite hadrons (pions, protons, etc.), because their size is comparable to a fraction or the whole system created in pp, p-Pb and Pb-Pb collisions. The size is typically defined in two ways: (a) as the r.m.s. of the (charge) distribution (λ_A) , typically measured in electron scattering experiments, or (b) as the size parameter of the object wave function (r_A) , typically taken as the Gaussian solution of an isotropic harmonic oscillator potential in coalescence calculations. For light nuclei, $\lambda_A \approx 2$ fm. For the hyper-triton, theoretical calculations indicate a charge r.m.s. radius $\lambda_A \approx 5$ fm [27], driven by the average separation of the Λ relative to the two other nucleons. Assuming a similar structure (e.g. an s-wave interaction for a bound state of an n or a Λ with a deuteron), the hyper-triton results in a much larger object than the other non-strange nuclei with A = 3. A simple relation holds between λ_A and r_A , see [14]. In Table I, the binding energy (B_E) is also reported.

¹ For brevity, in the following we refer to "nuclei" and "hyper-nuclei" but we imply both matter and anti-matter.

The most tightly bound nucleus is ⁴He, whereas the most loosely bound object is ³_AHe, that is also the largest one. For the latter, we report the separation energy of the Λ baryon from the deuteron ($B_{\Lambda} = 0.13$ MeV). The large size and the low binding energy of the ³_AHe with respect to the other (hyper-)nuclei has important consequences on its production, as discussed in what follows.

TABLE I

Properties of nuclei and hyper-nuclei with mass number $A \leq 4$. B_E is the binding energy in MeV. The size parameter, r_A , is chosen to approximately reproduce the measured/expected r.m.s., λ_A^{meas} [fm]. The proton r.m.s. charge radius $\lambda_p =$ 0.879(8) fm is subtracted quadratically from the measured r.m.s. charge radius λ_A^{meas} of the nucleus $\lambda_A = \sqrt{(\lambda_A^{\text{meas}})^2 - \lambda_p^2}$ to account for the finite extension of the constituents. Implicitly, we assume here that $\lambda_A \approx \lambda_n \approx \lambda_p$.

Mass number	Nucleus	Compo- sition	B_E [MeV]	$\begin{array}{c} {\rm Spin} \\ J_A \end{array}$	(Charge) r.m.s. radius λ_A^{meas} [fm]	Harmonic oscillator size parameter r_A [fm]	Refs.
A = 2	d	pn	2.224575 (9)	1	2.1413 ± 0.0025	3.2	[28, 29]
A = 3	$^{3}\mathrm{H}$ $^{3}\mathrm{He}$ $^{3}_{\Lambda}\mathrm{H}$	$pnn \ ppn \ p\Lambda n$	$\begin{array}{c} 8.4817986 \ (20) \\ 7.7180428 \ (23) \\ 0.13 \pm 0.05 \end{array}$	$1/2 \\ 1/2 \\ 1/2$	$\begin{array}{c} 1.755 \pm 0.086 \\ 1.959 \pm 0.030 \\ 4.910.0 \end{array}$	2.15 2.48 6.8–14.1	[30] [30] [27, 31]
A = 4	${}^{4}\text{He}$ ${}^{4}_{\Lambda}\text{H}$ ${}^{4}_{\Lambda\Lambda}\text{H}$ ${}^{4}_{\Lambda}\text{He}$	ppnn pAnn pAAn ppAn	$\begin{array}{c} 28.29566 \ (20) \\ 2.04 \pm 0.04 \\ 0.39 0.51 \\ 2.39 \pm 0.03 \end{array}$	0 0 1 0	$\begin{array}{c} 1.6755 \pm 0.0028 \\ 2.0 - 3.8 \\ 4.2 - 7.1 \\ 2.0 - 3.8 \end{array}$	$1.9 \\ 2.4-4.9 \\ 5.5-9.4 \\ 2.4-4.9$	$\begin{bmatrix} 32, 33 \\ [27, 31] \\ [27] \\ [27, 31] \end{bmatrix}$

2.1. The coalescence approach

In the coalescence picture, nucleons are produced in the collision coalesce into nuclei if they are close in space and have similar velocities [1–3]. The coalescence probability is encoded in the coalescence parameter, B_A . Considering that at the LHC energies the number of produced protons and neutrons at midrapidity as well as their momentum distributions are expected to be equal, B_A is defined as

$$E_A \frac{\mathrm{d}^3 N_A}{\mathrm{d} p_A^3} = B_A \left(E_{p,n} \frac{\mathrm{d}^3 N_{p,n}}{\mathrm{d} p_{p,n}^3} \right)^A \Big|_{\vec{p}_p = \vec{p}_n = \frac{\vec{p}_A}{A}} , \qquad (1)$$

where $p_{p,n}$ are the proton and neutron momenta and $E_{p,n}$ their energies. Equation (1) represents also the operative definition of B_A that is used by experiments like ALICE to extract the coalescence probability starting from the measured nucleus and nucleon (proton) distributions. Starting from the model described in [3, 4], we have obtained in [14] a generalised expression for B_A

$$B_A = \frac{2J_A + 1}{2^A} \frac{1}{\sqrt{A}} \frac{1}{m_{\rm T}^{A-1}} \left(\frac{2\pi}{R^2 + \left(\frac{r_A}{2}\right)^2}\right)^{\frac{3}{2}(A-1)}, \qquad (2)$$

which is a function of the spin of the particle J_A , its transverse mass $m_{\rm T}$, its size parameter r_A and the source radius R. Very importantly, Eq. (2) takes explicitly into account the source size (R), as the coalescence probability naturally decreases for nucleons with similar momenta that are produced far apart in configuration space. Moreover, the source size is identified with the effective sub-volume of the whole system that is governed by the (momentum-dependent) homogeneity length of the interacting nucleons and experimentally accessible with the Hanbury Brown–Twiss (HBT) interferometry [3, 4]. Figure 1 shows the source radius dependence of B_A for nuclei and hyper-nuclei with A = 2, 3 and 4 whose properties are reported in Table I. For the cases in which more than one estimate for r_A is available, we have adopted the lowest value for the calculations in Fig. 1. We observe that the coalescence probability decreases with increasing mass number and



Fig. 1. (Colour on-line) Coalescence parameter B_A as a function of the source radius R as predicted from the coalescence model (Eq. (2)) for various composite objects with $p_T/A = 0.75 \text{ GeV}/c$. For each (hyper-)nucleus, the radius r used for the calculation is reported in the legend.

 B_A decreases with increasing volume. For a given A, the larger the object radius, the lower is B_A , as clearly visible by comparing ³He and ³_AH. For objects with the same A, mass and spin (e.g. the isobars ³H and ³He), B_A differs only due to the different radius r_A . This difference is more relevant in small systems, because in large systems, the difference between nucleus radii is much smaller than the size of the source. Incidentally, this could be experimentally verified with high-precision measurements of the production of ³H relative to ³He in pp and p-Pb collisions. The production of objects with radius larger than the source is strongly suppressed, indicating that the process is driven by the length scale defined by the object radius relative to the source radius.

2.2. Thermal + blast-wave model

Thermal-statistical models [5, 6] have been successful in describing the production of light (anti-)(hyper-)nuclei across a wide range of energies in AA collisions, including production at the LHC. In this approach, particles are produced from a fireball in thermal equilibrium with temperatures of $T_{\rm chem} \approx 156$ MeV. Particle yields are derived from the partition function assuming a Grand Canonical ensemble² and depend only on the mass of the particle and the temperature of chemical freeze-out, $dN/dy \propto (2J_A+1)$ $\exp(-m_A/T_{\rm chem})$. The thermal model cannot — alone — be compared to the $p_{\rm T}$ -dependent coalescence description because it provides only predictions for $p_{\rm T}$ -integrated yields. A thermal particle production implies a Boltzmann distribution of the momenta only for a static source, which is not the case of the rapidly expanding system produced in heavy-ion collisions. The thermal model (*i.e.* the GSI-Heidelberg implementation we have considered here) needs to be complemented by a hydrodynamic description of the rapidly expanding source. To that end, we use the blast-wave model [35]. which has been proven to describe reasonably well the measured momentum distributions of protons [36]. Our "thermal+blast-wave" approach results from the combination of the two models: the $p_{\rm T}$ -dependence is modelled by the blast-wave whereas the normalisation (*i.e.* the $p_{\rm T}$ -integrated yield) is taken from the thermal model predictions. In particular, to describe the (hyper-)nucleus transverse momentum distributions, we use the blast-wave parameters obtained from the simultaneous fit to pion, kaon and proton spectra measured in Pb–Pb collisions by ALICE for several centralities/multiplicities and reported in [36]. We, therefore, inherit the multiplicity dependence of the radial expansion of the system from the measurements.

² Extensions to small systems employ a canonical ensemble partition function to account for the exact conservation of quantum numbers in a finite size system, see for instance [34].

The object size does not enter in the formulation of the blast-wave model. In our thermal+blast-wave model, for each centrality/multiplicity class, the coalescence parameter is extracted according to Eq. (1) (as done for data) from the predicted (hyper-)nucleus spectrum and the proton spectrum measured by ALICE [36].

3. Results and discussion

As discussed in the previous sections, the coalescence model provides an analytical expression for B_A as a function of the source size R. The thermal+blast-wave approach allows us to extract the B_A as a function of the average charged particle multiplicity density, $\langle dN_{ch}/d\eta_{lab} \rangle$. Measurements are performed differentially in centrality/multiplicity. In order to compare models and data, we need to map multiplicity into source radius or vice versa. As discussed more extensively in [14], we perform this mapping based on the parameterisation $R = 0.473 \ \langle dN_{ch}/d\eta_{lab} \rangle^{1/3}$ for $p_T/A = 0.75 \ \text{GeV}/c$. The slope is smaller for larger $p_{\rm T}$ s and larger for lower $p_{\rm T}$. The value of the empirical slope parameter is obtained by tuning the parameterisation such that the measured (anti-)deuteron B_2 in the most central Pb–Pb class falls onto the coalescence prediction. In other words, we constrain the coalescence volume with the more differential (anti-)deuteron data and assume that it is the same for all (hyper-)nuclei. In [14], we used the parameterisation to map the $\langle dN_{ch}/d\eta_{lab} \rangle$ into R. Here, we chose to apply the inverse relation and compare B_A from models with ALICE data as a function of the experimentally accessible observable $\langle dN_{ch}/d\eta_{lab} \rangle$. The two choices are equivalent. This comparison is reported in Fig. 2. With respect to [14], we have now extended our study up to A = 4 (hyper-)nuclei.

We observe that for deuterons, the coalescence and thermal+blast-wave approaches lead to similar predictions and describe reasonably the Pb– Pb data. For ³He, the models exhibit a qualitatively similar multiplicity dependence with the magnitude of B_A differing by a factor 1.5 to 2 going from large to small systems. The currently available data for ³He are consistent with both models within 2σ to 3σ , where σ is the total uncertainty on data. Both approaches show large differences (a factor 5 to 6 for central Pb–Pb collisions and a factor larger than 50 for $\langle dN_{ch}/d\eta_{lab}\rangle < 100$) for the ³_AH caused by the significantly larger size of ³_AH with respect to ³He. The only data point available so far in Pb–Pb collisions is in agreement with the thermal+blast-wave model but differs by 6σ from our coalescence calculation. Also for ⁴He and ⁴_AHe, the coalescence probability is a steeply falling function of multiplicity in both approaches, which differ in magnitude from few units at high multiplicities to O(10²) in small systems. We conclude that the difference between the two approaches increases from large to small sys-



Fig. 2. (Colour on-line) Coalescence parameter B_A as a function of the average charged particle multiplicity density for various (hyper-)nuclei, up to A = 4. The coalescence calculations (continuous or dash-dotted black lines) are compared to the thermal+blast-wave predictions (dashed blue line), as well as to pp (green square) and Pb–Pb (red circles) collision data from ALICE [7–9].

tems, which advocates for new multiplicity-differential data in all collision systems to distinguish between the two production scenarios. For ${}^{3}_{A}$ H and ${}^{3}_{A}$ He, we also report in Fig. 2 the coalescence calculations obtained assuming wider wave functions, which result in even lower production probabilities.

The Grand Canonical thermal Ansatz is no longer valid when going to small collision systems, because one needs to account for the exact conservation of quantum numbers in a finite volume and thus a canonical ensemble has to be used. As an example, we have also computed B_A for ³He according to the thermal+blast-wave approach for the *p*-Pb system by using yield predictions from the Canonical Statistical Model from [34] and the blastwave parameters from [37]. The result is reported in Fig. 3 with the dashed blue line. We notice that the thermal+blast-wave prediction in this case does not exhibit a significant dependence on multiplicity and is relatively close to the coalescence curve. As expected, in high multiplicity *p*-Pb collisions, the CSM+blast-wave curve tends to merge with the Grand Canonical prediction.



Fig. 3. (Colour on-line) Coalescence parameter B_3 for ³He as a function of the average charged particle multiplicity density $\langle dN_{ch}/d\eta_{lab}\rangle$. The coalescence calculation (continuous black line) is compared to two thermal+blast-wave predictions (dashed lines), obtained by using the Grand Canonical (GC, red) [6] and Canonical Statistical Model (CSM, blue) [34] expectations for the ³He yield, respectively. ALICE data from pp (green circles) and Pb–Pb (red circles) collisions [7, 9] are reported.

4. Conclusions

We have presented a direct comparison of the coalescence and thermal+blast-wave production scenarios for light nuclei and hyper-nuclei as a function of multiplicity, used as a proxy for the source size. To clarify the production mechanism of composite loosely-bound QCD objects, we show the importance of new and precise measurements of (hyper-)nuclei production up to A = 4 as a function of multiplicity in different collision systems, in order to fully exploit the sensitivity of production mechanisms to the size of the object relative to the size of the source. Particularly sensitive to production mechanisms is the hyper-triton with its large size. The increase in integrated luminosity foreseen in all collision systems during the LHC Runs 3 and 4 in years 2021–2029 should allow the ALICE Collaboration to perform these multi-differential measurements, which will provide crucial insights into the "anti-nuclei puzzle" and the (hyper-)nuclei formation.

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