

GAMOW–TELLER TRANSITION STRENGTHS
FOR SELECTED fp SHELL NUCLEIVIKAS KUMAR[†]Department of Physics, Central University of Kashmir
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We have reported a systematic shell model description of the experimental Gamow–Teller transition strength for $^{44}\text{Sc} \rightarrow ^{44}\text{Ca}$, $^{45}\text{Ti} \rightarrow ^{45}\text{Sc}$, $^{48}\text{Ti} \rightarrow ^{48}\text{V}$, $^{66}\text{Co} \rightarrow ^{66}\text{Ni}$, and $^{66}\text{Fe} \rightarrow ^{66}\text{Co}$ transitions using KB3G and GXPF1A interactions for fp model space. In order to see the importance of higher orbital for $^{66}\text{Co} \rightarrow ^{66}\text{Ni}$ and $^{66}\text{Fe} \rightarrow ^{66}\text{Co}$ transitions, we have reported the shell model results with $fp g_9/2$ space using GXPF1Br+ V_{MU} interaction. We have obtained the qualitative agreement for the individual transitions, while the calculated summed transition strengths closely reproduce the observed ones.

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1. Introduction

The Gamow–Teller (GT) transition is a nuclear weak interaction process which is used as a basic input to study the structure of atomic nuclei [1–12]. To estimate electron-capture (EC) reaction rates in the case of β^+ decay, we need Gamow–Teller (GT) strength [$B(\text{GT})$] distributions. The EC reactions on medium-mass nuclei play a significant role in astrophysical phenomena such as core-collapse (type II) supernovae (SNe); thermonuclear type (type Ia) SNe; heating and cooling processes in crusts of accreting neutron stars. Thus to understand these process, it is highly desirable to precisely calculate GT strengths using suitable nuclear models. Experimental

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GT strengths can be obtained from β -decay and charge-exchange reactions. The β -decay measurements are limited to small Q -value window, while with charge exchange reactions such as (p,n) , $({}^2\text{He},d)$ and $({}^3\text{He},t)$, they are useful tools to study the relative values of $B(\text{GT})$ strengths up to high excitation energies. The Gamow–Teller transition study for the ${}^{48}\text{Ti}({}^3\text{He},t){}^{48}\text{V}$ reaction is reported in Ref. [13], the highly fragmented GT strength distributions for ${}^{48}\text{Ti}$ are observed in this experiment. The experimental GT strengths corresponding to ${}^{66}\text{Co} \rightarrow {}^{66}\text{Ni}$ and ${}^{66}\text{Fe} \rightarrow {}^{66}\text{Co}$ transitions are available in Ref. [14]. Theoretical investigation to study strong magnetic dipole (M1) transitions and GT strengths for fp shell nuclei is reported in Refs. [15–22].

In the present work, our aim is to calculate the GT strengths and compare the theoretical results with the experimental data. We have also calculated GT strengths distributions at higher excitation energies. This might be very useful for upcoming experimental data. It is also possible to predict half-lives using GT strengths as an input.

In the present work, we have performed shell model calculations to obtain the GT strengths for ${}^{44}\text{Sc} \rightarrow {}^{44}\text{Ca}$, ${}^{45}\text{Ti} \rightarrow {}^{45}\text{Sc}$ and ${}^{48}\text{Ti} \rightarrow {}^{48}\text{V}$ transitions using GXPF1A and KB3G effective interactions in the full fp model space. We have also reported the GT strength results corresponding to ${}^{66}\text{Co} \rightarrow {}^{66}\text{Ni}$ and ${}^{66}\text{Fe} \rightarrow {}^{66}\text{Co}$ transitions using fp and $fp9_{9/2}$ spaces. In Table I, we have given a list of fp shell nuclei considered in the present work for GT strength calculations, the number of GT transitions, transitions up to the excitation energy in MeV, and the references are given in the last column for comparison with the theoretical results.

TABLE I

Initial and final nuclei, the number of GT transitions, transitions up to the excitation energy in MeV and the references are given in the last column for comparison with the theoretical results.

No.	Initial	Final	Transitions (No.)	EXPT.	GXPF1A	KB3G	GXPF1Br + V_{MU}	Ref.
1.	${}^{44}\text{Sc}(2^+)$	${}^{44}\text{Ca}(1^+, 2^+, 3^+)$	50	3.301	19.204	16.883	—	[23]
2.	${}^{45}\text{Ti}(\frac{7}{2}^-)$	${}^{45}\text{Sc}(\frac{5}{2}^-, \frac{7}{2}^-, \frac{9}{2}^-)$	50	1.662	10.022	9.384	—	[24]
3.	${}^{48}\text{Ti}(0^+)$	${}^{48}\text{V}(1^+)$	350	12.646	13.048	12.983	—	[13]
4.	${}^{66}\text{Co}(1^+)$	${}^{66}\text{Ni}(0^+, 1^+, 2^+)$	100*	3.752	15.506	19.540	18.730	[14]
5.	${}^{66}\text{Fe}(0^+)$	${}^{66}\text{Co}(1^+)$	100*	2.236	13.546	17.880	13.638	[14]

*For GXPF1Br+ V_{MU} interaction we have calculated 300 eigenvalues.

2. Details of the shell model calculation

The shell model effective Hamiltonian can be expressed in terms of single-particle energies and two-body matrix elements

$$H = \sum_{\alpha} \varepsilon_{\alpha} \hat{N}_{\alpha} + \frac{1}{4} \sum_{\alpha\beta\delta\gamma JT} \langle j_{\alpha} j_{\beta} | V | j_{\gamma} j_{\delta} \rangle_{JT} A_{JT;j_{\alpha} j_{\beta}}^{\dagger} A_{JT;j_{\delta} j_{\gamma}}, \quad (1)$$

where $\alpha = \{nljt\}$ is the single-particle orbital and ε_{α} is corresponding to the single-particle energy.

$\hat{N}_{\alpha} = \sum_{j_z, t_z} a_{\alpha, j_z, t_z}^{\dagger} a_{\alpha, j_z, t_z}$ is the particle number operator. A_{JT} and A_{JT}^{\dagger} are the fermion pair annihilation and creation operator, respectively. $\langle j_{\alpha} j_{\beta} | V | j_{\gamma} j_{\delta} \rangle_{JT}$ are the two-body matrix elements coupled to spin J and isospin T .

To obtain the GT strengths, we have performed shell model calculations in the *fp* model space using the KB3G [25] and GXPF1A [26] interactions. In order to see the importance of higher orbital for $^{66}\text{Co} \rightarrow ^{66}\text{Ni}$ and $^{66}\text{Fe} \rightarrow ^{66}\text{Co}$ transitions, we have also included the results with *fp* $g_{9/2}$ space using the GXPF1Br+ V_{MU} interaction [27]. Although GXPF1Br+ V_{MU} interaction is for *fp* $g_{9/2}d_{5/2}$ space, here we are not allowing protons/neutrons to occupy the $d_{5/2}$ orbital. For $^{66}\text{Co} \rightarrow ^{66}\text{Ni}$ and $^{66}\text{Fe} \rightarrow ^{66}\text{Co}$ transitions, we fix minimum six particles in the $f_{7/2}$ orbital, while for both protons and neutrons, we allow maximum 2 neutrons in the $g_{9/2}$ orbital. Thus, we put the same truncations for both protons and neutrons. The shell model calculations are performed using the code NuShellX@MSU [28].

The Gamow–Teller strength $B(\text{GT})$ is calculated using the following expression:

$$B(\text{GT}_{\pm}) = \frac{1}{2J_i + 1} f_q^2 |\langle f | \sum_k \sigma^k \tau_{\pm}^k | i \rangle|^2, \quad (2)$$

where $\tau_+ |p\rangle = |n\rangle$, $\tau_- |n\rangle = |p\rangle$, f_q is the quenching factor, the index k runs over the single-particle orbitals, $|i\rangle$ and $|f\rangle$ describe the state of the parent and daughter nuclei, respectively. The reported $B(\text{GT})$ and summed $B(\text{GT})$ values are quenched by a quenching factor $q = 0.66$ [29].

It is possible to improve further GT strengths results by adding the effect of two-body currents (2BCs) in the quenching factor [30–33]. Recently, for the *ab initio* calculations, it was suggested that if we use the evolve operator, then there is no need to use the quenching factor [34].

3. Comparison of theoretical and experimental $B(\text{GT})$ strength distributions

The comparison between calculated and experimental GT strengths distributions for different transitions are reported below.

3.1. $^{44}\text{Sc} \rightarrow ^{44}\text{Ca}$

Figure 1 shows the experimental and calculated shell model $B(\text{GT})$ strength distributions for the transition $^{44}\text{Sc} \rightarrow ^{44}\text{Ca}$. The $B(\text{GT})$ values from 2^+ ground state of $^{44}\text{Sc}(2^+) \rightarrow ^{44}\text{Ca}(1^+, 2^+, 3^+)$ states have been calculated without any truncation. Figure 1 (a) represents the experimental data observed through the β^+ -decay $^{44}\text{Sc} \rightarrow ^{44}\text{Ca}$ [23], Fig. 1 (b) represents the shell model calculation using the GXPF1A interaction, Fig. 1 (c), the shell model calculation using the KB3G interaction, and Fig. 1 (d), the running sums of $B(\text{GT})$ as a function of excitation energy $E_x(^{44}\text{Ca})$. The first $B(\text{GT})$ strength observed at 1.157 MeV is predicted by both the shell model calculations but the second one at 2.657 MeV is predicted to be slightly smaller than the experiment in both the shell model calculations. The third observed $B(\text{GT})$ strength at 3.301 MeV is predicted by both the shell model calculations at 4.148 and 3.947 MeV, respectively. From the sums of $B(\text{GT})$ strength figure, it is clear that both the shell model results are in good agreement with the observed summed $B(\text{GT})$ strengths, it indicates that the fp space is able to produce the observed results in the case of $^{44}\text{Sc} \rightarrow ^{44}\text{Ca}$ transition at low excitation energies. Both the shell model calculations predict a large number of $B(\text{GT})$ values at ~ 10 MeV which have not been yet observed in the experiment.

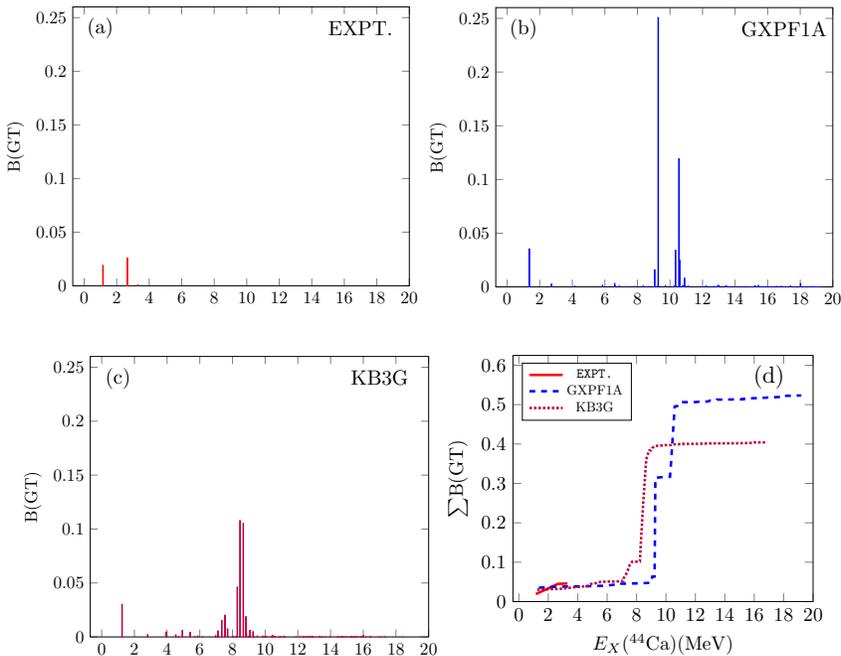


Fig. 1. Comparison of experimental and theoretical $B(\text{GT})$ distributions for ^{44}Sc .

3.2. $^{45}\text{Ti} \rightarrow ^{45}\text{Sc}$

Figure 2 displays a comparison between the shell model calculations and the experimental GT strength distribution for the transition $^{45}\text{Ti} \rightarrow ^{45}\text{Sc}$. We have calculated $B(\text{GT})$ values from the ground state of ^{45}Ti ($\frac{7}{2}^-$) \rightarrow ^{45}Sc ($\frac{5}{2}^-, \frac{7}{2}^-, \frac{9}{2}^-$) states without any truncation. Figure 2 (a) presents the experimental data observed through the β^+ -decay [24]. Figure 2 (b) depicts the shell model calculation using the GXPF1A interaction, Fig. 2 (c), the shell model calculation using the KB3G interaction, and Fig. 2 (d), the running sums of $B(\text{GT})$ as a function of the excitation energy $E_x(^{45}\text{Sc})$. There are four $B(\text{GT})$ transition strengths observed in the experiment at 0, 0.72, 1.408, and 1.662 MeV lying between 0.002–0.011. These low lying $B(\text{GT})$ strengths are successfully produced by both the shell model calculations. Both the shell model calculations predict the highly fragmented GT strengths at excitation energies $E_x(^{45}\text{Sc}) \sim 2$ –10 MeV which are not observed in the experiment. The concentrated GT strengths predicted by the theory at higher excitation energies may be observed in the future experiments. The calculated shell model results for the sum of $B(\text{GT})$ strengths at lowest energy states are in good agreement with the experiment and the trend of both the shell model results are following the same pattern at higher excitation energies.

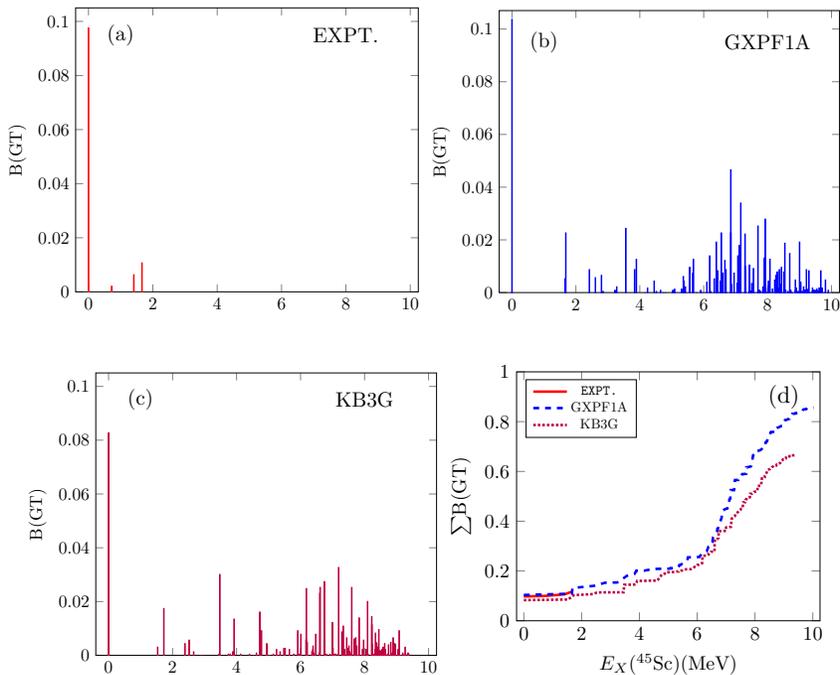


Fig. 2. Comparison of experimental and theoretical $B(\text{GT})$ distributions for ^{45}Ti .

3.3. $^{48}\text{Ti} \rightarrow ^{48}\text{V}$

Figure 3 displays a comparison between the shell model calculations and the experimental $B(\text{GT})$ strength distribution for the transition $^{48}\text{Ti} \rightarrow ^{48}\text{V}$. We have calculated $B(\text{GT})$ values from the ground state of $^{48}\text{Ti}(0^+)$ to $^{48}\text{V}(1^+)$ states without any truncation. Figure 3 (a) presents the experimental data observed through the charge-exchange reaction $^{48}\text{Ti}(^3\text{He},t)^{48}\text{V}$ [13], Fig. 3 (b) depicts the shell model calculation using the GXPF1A interaction, Fig. 3 (c), the shell model calculation using the KB3G interaction, and Fig. 3 (d), the running sums of $B(\text{GT})$ as a function of the excitation energy $E_x(^{48}\text{V})$. Figure 3 (a) shows that the GT strength is highly fragmented and distributed over many discrete states, the same pattern is also predicted from both the shell model calculations. The four dominated GT values range from 0.147 to 0.351 are observed for the transitions from the $J^\pi = 0^+$, ground state of ^{48}Ti to the 1^+ states of ^{48}V at excitation energies $E_x = 0.421, 2.406, 3.387,$ and 3.864 MeV. The calculated shell model intensities for these transitions are similar to the measured ones. At higher excitation energies, both the shell model calculations predict some more dominated transitions which are not observed in the experiment, while one dominated GT strength observed in the experiment at $E_x = 3.387$ MeV is missing in both the calculations. The GXPF1A interaction generated an excitation

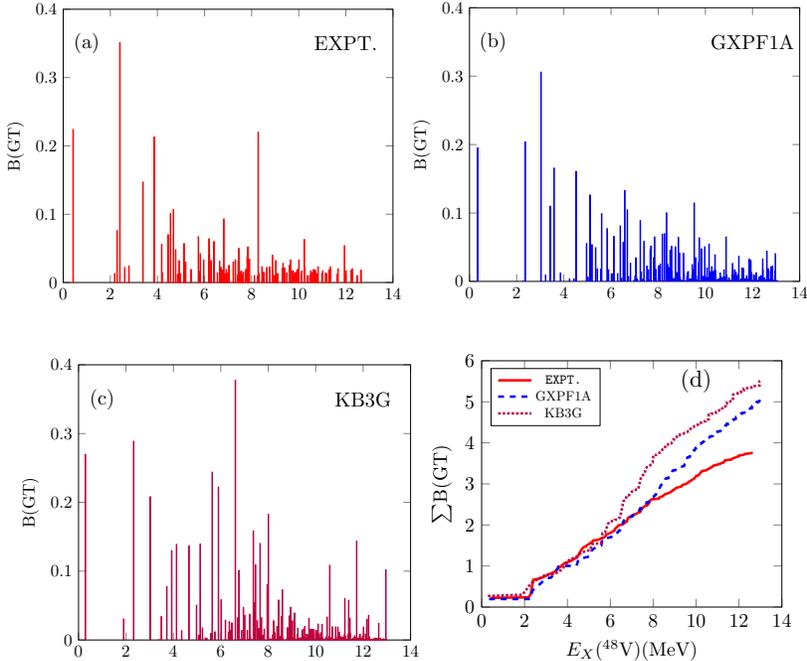


Fig. 3. Comparison of experimental and theoretical $B(\text{GT})$ distributions for ^{48}Ti .

energy closer to the experimental one than the energy obtained employing the KB3G interaction. From Fig. 3(d) summed $B(\text{GT})$ strength plot, the summed $B(\text{GT})$ strength predicted by the GXPF1A interaction is closer to the experiment than by the KB3G interaction. The summed $B(\text{GT})$ strength predicted by KB3G is in agreement with the experiment at lower excitation energy but not at higher excitation energy, overall, the summed $B(\text{GT})$ strength predicted by GXPF1A interaction matched with observed ones better than predicted by KB3G.

3.4. ${}^{66}\text{Co} \rightarrow {}^{66}\text{Ni}$

Figure 4 shows the experimental and calculated shell model $B(\text{GT})$ strength distributions for the transition ${}^{66}\text{Co} \rightarrow {}^{66}\text{Ni}$. We have calculated $B(\text{GT})$ values from the ground state of ${}^{66}\text{Co}(1^+) \rightarrow {}^{66}\text{Ni}(0^+, 1^+, 2^+)$ states

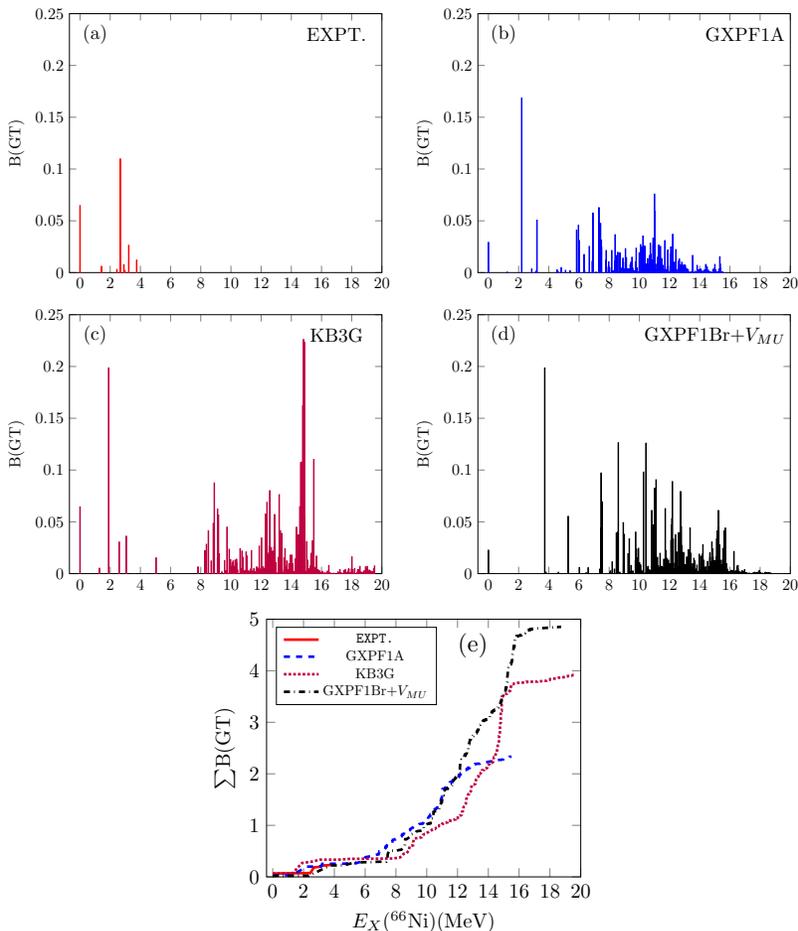


Fig. 4. Comparison of experimental and theoretical $B(\text{GT})$ distributions for ${}^{66}\text{Co}$.

without any truncation using GXPF1A and KB3G interactions. Figure 4 (a) represents the experimental data observed through the β^- -decay ${}^{66}\text{Co} \rightarrow {}^{66}\text{Ni}$ [14], Fig. 4 (b) represents the shell model calculation using the GXPF1A interaction, Fig. 4 (c), the shell model calculation using the KB3G interaction, Fig. 4 (d) represents the shell model calculation using the GXPF1Br+ V_{MU} interaction for $fp g_{9/2}$ model space, and Fig. 4 (e), the running sums of $B(\text{GT})$ as a function of excitation energy $E_x({}^{66}\text{Ni})$. There are eight GT transition strengths which are observed from the ground state of ${}^{66}\text{Co}$ to different excited states of ${}^{66}\text{Ni}$ at 0, 1.425, 2.443, 2.671, 2.907, 2.974, 3.228, and 3.752 MeV. All these eight GT transition strengths are also produced in all the shell model calculations. All the interactions predict several weakly excited states with $B(\text{GT})$ values, for example, the GXPF1A with $B(\text{GT})$ values of 0.001–0.174 in the range of 4.00–15.506 MeV, the KB3G with $B(\text{GT})$ values of 0.001–0.226 in the range of 4.00–19.540 MeV, and the GXPF1Br+ V_{MU} with $B(\text{GT})$ values of 0.001–0.127 in the range of 5.000–18.730 MeV. All these predicted weakly excited states are not observed in the experiment. Overall, the sum of $B(\text{GT})$ strengths predicted by GXPF1A interaction is more closer to experiment than other two interactions.

3.5. ${}^{66}\text{Fe} \rightarrow {}^{66}\text{Co}$

The shell model calculations and the experimental GT strength distributions for the transition ${}^{66}\text{Fe} \rightarrow {}^{66}\text{Co}$ are presented in Fig. 5. We have calculated $B(\text{GT})$ values from the ground state of ${}^{66}\text{Fe}(0^+) \rightarrow {}^{66}\text{Co}(1^+)$ states without any truncation using GXPF1A and KB3G interactions. The experimental data observed through the β^- -decay ${}^{66}\text{Fe} \rightarrow {}^{66}\text{Co}$ [14] are shown in Fig. 5 (a), in Fig. 5 (b), the shell model calculation using the GXPF1A interaction, in Fig. 5 (c), the shell model calculation using the KB3G interaction, in Fig. 5 (d), the shell model calculation using the GXPF1Br+ V_{MU} interaction, in Fig. 5 (e), the running sums of $B(\text{GT})$ as a function of the excitation energy $E_x({}^{66}\text{Co})$. Two dominant GT transition strengths are observed in the experiment from ${}^{66}\text{Fe}(0^+) \rightarrow {}^{66}\text{Co}(1^+)$ states at $E_x({}^{66}\text{Co}) = 0$ and 0.982 MeV. The first experimental GT transition strength is predicted in both GXPF1A and KB3G shell model calculations, while in GXPF1Br+ V_{MU} interaction, the first $B(\text{GT})$ value is shifted to the higher excitation energy. In all the shell model calculations, the second observed $B(\text{GT})$ value is missing. It is found that the GXPF1A interaction generated an excitation energy and $B(\text{GT})$ strengths closer to the experiment than the KB3G interaction. The shell model calculations predict several excited states with small $B(\text{GT})$ values in the 4–14 MeV region in GXPF1A, 6.5–17.8 MeV region in KB3G and 5.298–13.638 MeV region in GXPF1Br+ V_{MU} effective interaction. These several weakly GT transitions strengths are not observed in the experiment, these theoretical results may serve as the input for the future experiments.

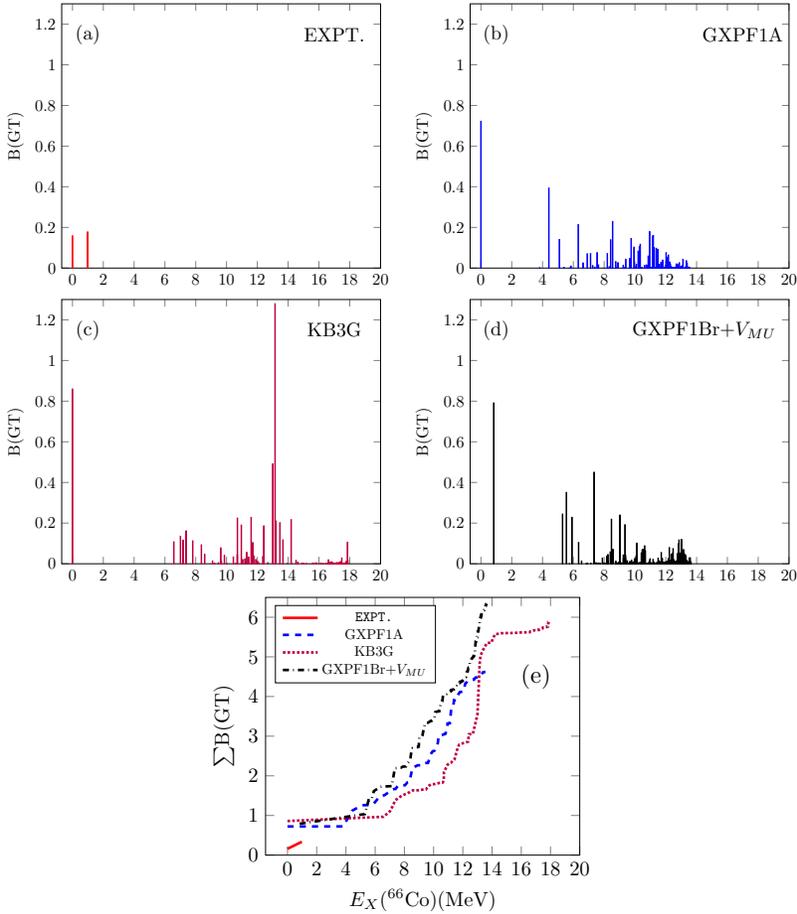


Fig. 5. Comparison of experimental and theoretical $B(\text{GT})$ distributions for ^{66}Fe .

The results of GT strengths with GXPF1A and KB3G are different, this might be due to different originality of these two interactions. The GXPF1A interaction is developed from G-matrix with state-of-art fitting procedures, while KB3G interaction is a monopole-corrected version of KB3 effective interaction. There are also differences in the single-particle energies adopted. Overall, the density of states are generally dense for the GXPF1A interaction.

4. Summary and conclusion

In the present work, we have reported shell model result in the fp model space for recently measured GT strengths of $^{44}\text{Sc} \rightarrow ^{44}\text{Ca}$, $^{45}\text{Ti} \rightarrow ^{45}\text{Sc}$, $^{48}\text{Ti} \rightarrow ^{48}\text{V}$, $^{66}\text{Co} \rightarrow ^{66}\text{Ni}$, and $^{66}\text{Fe} \rightarrow ^{66}\text{Co}$ transitions. To see the importance

of $g_{9/2}$ orbital, we have performed a calculation in $fp_{g_{9/2}}$ space for ${}^{66}\text{Co} \rightarrow {}^{66}\text{Ni}$ and ${}^{66}\text{Fe} \rightarrow {}^{66}\text{Co}$ transitions. The qualitative agreement is obtained for the individual $B(\text{GT})$ transitions, while the calculated summed transition strengths closely reproduce the observed ones. In the case of ${}^{48}\text{Ti} \rightarrow {}^{48}\text{V}$, ${}^{45}\text{Ti} \rightarrow {}^{45}\text{Sc}$, ${}^{66}\text{Co} \rightarrow {}^{66}\text{Ni}$ and ${}^{66}\text{Fe} \rightarrow {}^{66}\text{Co}$ transitions, theoretical strengths are larger than the experimental value. Thus, further experimental results are needed for these strengths. Results of the present work will add more information to earlier works.

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