

# WOUNDED-QUARK EMISSION FUNCTION IN ASYMMETRIC HEAVY-ION COLLISIONS\*

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The wounded-nucleon and -quark models are compared using  $d$ +Au collisions at  $\sqrt{s_{NN}} = 200$  GeV. The shape of the wounded-quark emission function seems to be universal for different centralities, in contrast to the wounded-nucleon emission function. Predictions for  $dN_{ch}/d\eta$  distributions for various centrality classes in  $p$ +Al,  $p$ +Au,  $d$ +Au, and  $^3\text{He}$ +Au collisions are presented and compared to recent PHENIX results.

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## 1. Introduction

The wounded-nucleon and -quark models (WNM, WQM), among others, are frequently used [1–14] to describe soft particle production in relativistic heavy-ion collisions. In WNM, nucleus–nucleus collision is considered as multiple nucleon–nucleon interactions [1]. Any nucleon from one nucleus colliding inelastically with at least one nucleon from another nucleus is called a “wounded” nucleon and is assumed to populate charged particles independently of the number of collisions it undergoes. On the other hand, in WQM, it is postulated that a heavy-ion collision consists of quark–quark interactions [2]. By analogy, the wounded quarks produce particles independently of the number of collisions.

Deuteron–gold ( $d$ +Au) collisions at  $\sqrt{s_{NN}} = 200$  GeV measured by the PHOBOS Collaboration at the Relativistic Heavy Ion Collider (RHIC) [15] were used to compare both models. The wounded-source emission functions  $F(\eta)$  (pseudorapidity single particle density originating from one wounded source) for different centralities were extracted using the PHOBOS data and our Monte Carlo Glauber simulations.

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## 2. Two models

As described in detail in Ref. [16], WNM and WQM were taken into consideration. In both cases, the charged particle multiplicity distribution is given by

$$\frac{dN_{\text{ch}}}{d\eta} = w_L F(\eta) + w_R F(-\eta), \quad (1)$$

where in the wounded-nucleon (-quark) model,  $F(\eta)$  is the wounded-nucleon (-quark) emission function,  $w_L$  and  $w_R$  are the average numbers of the left-going and the right-going wounded nucleons (quarks), respectively. If  $w_L \neq w_R$ , the wounded-source emission function can be extracted separately for each centrality

$$F(\eta) = \frac{1}{2} \left[ \frac{N(\eta) + N(-\eta)}{w_L + w_R} + \frac{N(\eta) - N(-\eta)}{w_L - w_R} \right], \quad (2)$$

where  $N(\eta) := dN_{\text{ch}}/d\eta$  is taken from the PHOBOS measurement on  $d+\text{Au}$  collisions at  $\sqrt{s_{NN}} = 200$  GeV [15].

In our Monte Carlo Glauber simulation, the positions of nucleons in the gold nucleus are drawn according to the Woods–Saxon distribution [17, 18], whereas in the deuteron, the proton’s position is taken from the Hulthen distribution and the neutron is placed opposite to the proton [17, 19]. Two nucleons collide if a transverse distance,  $d$ , between them is  $d \leq \sqrt{\sigma_{nn}/\pi}$ . The inelastic nucleon–nucleon cross section  $\sigma_{nn} = 41$  mb corresponds to  $\sqrt{s_{NN}} = 200$  GeV [17].

Wounded nucleons populate particles according to a negative binomial distribution (NBD) with  $\langle n \rangle = 5$  and  $k = 1$  [20], where  $k$  measures the deviation from the Poisson distribution. For each centrality bin,  $w_L$  and  $w_R$ , were calculated to complete Eq. (2).

In WQM, the positions of three constituent quarks around the center of each nucleon were drawn using  $\varrho(\vec{r}) = \varrho_0 \exp(-r/a)$ , where  $a = r_p/\sqrt{12}$  with  $r_p = 0.81$  fm being the proton’s radius [6, 21]<sup>1</sup>.

Quarks collide if  $d \leq \sqrt{\sigma_{qq}/\pi}$ , where  $\sigma_{qq}$  is the inelastic quark–quark cross section. We took  $\sigma_{qq} \simeq 7$  mb to reproduce  $\sigma_{nn} = 41$  mb [16]. Each wounded quark emits charged particles according to NBD with  $k_q = k_p/1.3$  and  $\langle n_q \rangle = \langle n_p \rangle/1.3$ , where  $k_p = 1$  and  $\langle n_p \rangle = 5$  are the parameters of NBD used in our WNM calculations.

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<sup>1</sup> Quarks are shifted so that their center of mass is the center of a nucleon and we actually used  $\tilde{\varrho}(\vec{r}) = \varrho_0 \exp(-Cr/a)$ .  $C = 0.82$  was determined by the trial and error method.

### 3. Results

Using Eq. (2), the wounded-nucleon emission function was extracted for different centrality bins and is shown in Fig. 1 (left)<sup>2</sup>. Apparently, the shape of  $F(\eta)$  is different for various centralities.

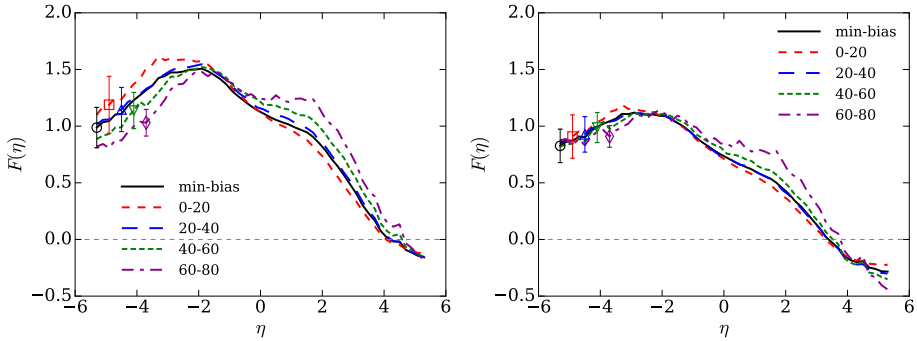


Fig. 1. The wounded-nucleon (left) and -quark (right) emission functions extracted from PHOBOS  $d+Au$  collisions at  $\sqrt{s_{NN}} = 200$  GeV. For clarity, the uncertainty bars are shown only for a limited number of points.

The extracted wounded-quark emission function, shown in Fig. 1 (right), is virtually universal for different centrality classes, see Ref. [16] for details. This observation was also verified recently in Ref. [22]. This could imply that the soft particle production in  $d+Au$  collisions is better described by WQM rather than WNM. Note that the wounded-quark emission function is physically meaningful for  $|\eta| \leq 3$  because in the fragmentation regions, other effects should be taken into account, *e.g.* contributions from unwounded quarks (within wounded nucleons) [5].

These results encouraged us to make predictions for  $p+Al$ ,  $p+Au$ ,  $d+Au$ , and  $^3He+Au$  collisions at the same energy for various centralities (as requested by the PHENIX Collaboration). We assumed that the wounded-quark emission function  $F(\eta)$  is universal also for various asymmetric systems at the same energy. Then, we determined  $w_L$  and  $w_R$  for each centrality class and using Eq. (1) we computed  $dN_{ch}/d\eta$  distributions for all colliding systems. The minimum-bias wounded-quark emission function  $F(\eta)$  has been used. The results are presented in Fig. 2. A very recent paper by the PHENIX Collaboration shows that the wounded-quark model with its universal wounded-quark emission function can reasonably well describe all measured asymmetric collisions [23].

<sup>2</sup> The errors represent the systematic uncertainties of  $N(\eta)$ . Thus, they are not expected to influence the shape of  $F(\eta)$ .

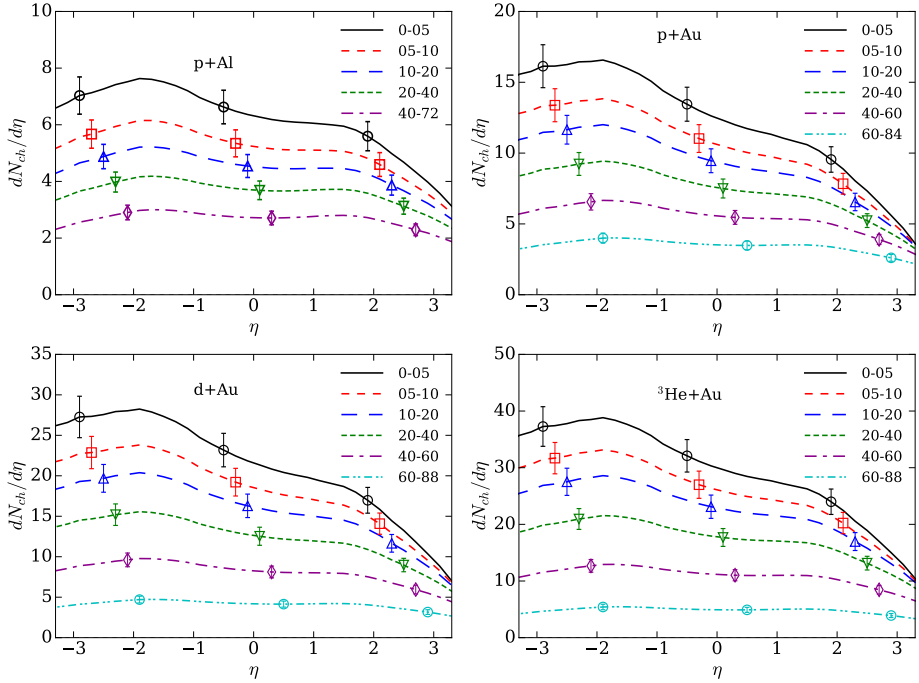


Fig. 2. Predicted charged particle  $dN_{\text{ch}}/d\eta$  distributions as functions of pseudorapidity for  $p+\text{Al}$ ,  $p+\text{Au}$ ,  $d+\text{Au}$ , and  ${}^3\text{He}+\text{Au}$  collisions at  $\sqrt{s_{NN}} = 200$  GeV for different centralities according to the wounded-quark model.

#### 4. Conclusions

To summarize, we argued that the wounded-quark emission function has a universal shape for various centrality classes (within uncertainties) in the range of  $|\eta| \leq 3$ , whereas the wounded-nucleon emission function differs across centralities [16]. The latest PHENIX results show that just one common wounded-quark emission function can successfully describe different systems ( $p+\text{Al}$ ,  $p+\text{Au}$ ,  $d+\text{Au}$ , and  ${}^3\text{He}+\text{Au}$ ) at  $\sqrt{s_{NN}} = 200$  GeV as our predictions are in reasonably good agreement with their measurement [23]. It suggests that the considered heavy-ion collisions and soft particle production are quite well described by the wounded-quark model. As a next step, we plan to take unwounded quarks from wounded nucleons into account for regions  $|\eta| > 3$  and also to study larger colliding systems such as  $\text{Au}+\text{Au}$  or  $\text{Cu}+\text{Cu}$ . For further research, it would be valuable to study event-by-event fluctuations of  $F(\eta)$  as well as to verify the model at different energies.

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