

DOUBLE-PARTON SCATTERING EFFECTS IN HEAVY MESON PRODUCTION*

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We present results of our theoretical investigation of double-parton scattering (DPS) effects in production of heavy flavour mesons (charm and bottom). We discuss production of charm–bottom and bottom–bottom meson–meson pairs in proton–proton collisions at the LHC. The calculation of DPS mechanism is performed within factorized Ansatz where each parton scattering is calculated in the framework of the k_T -factorization. The hadronization is done with the help of independent parton fragmentation picture. For completeness, we compare results for double- and single-parton scattering (SPS). As in the case of double charm production, also here the DPS dominates over the SPS, especially for small transverse momenta. We present several distributions and integrated cross sections with realistic cuts for simultaneous production of $D^0 B^+$ and $B^+ B^+$, suggesting future experimental studies at the LHCb detector.

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1. Introduction

In the ongoing era of LHC, a precise theoretical description of high-energy proton–proton collisions requires inclusion of multiple-parton interactions (MPI). Over last years, several experimental and theoretical studies of soft and hard MPI effects for different processes have been performed (see *e.g.* Refs. [1, 2]). A major part of those analyses concentrate in particular on phenomena of double-parton scattering (DPS). Usually, examination of DPS mechanism needs dedicated experimental analyses and is strongly limited due to the large background coming from standard single-parton scattering (SPS).

We have clearly shown in our previous papers that double open charm meson production $pp \rightarrow DD X$ is one of the best reactions to study hard double-parton scattering effects at the LHC [3–6]. In this case, the standard

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SPS contribution is much smaller than the DPS one and the cross sections for the DPS at the LHC are predicted to be quite large, in particular, much larger than for other reactions previously studied in this context in the literature.

Here, we wish to present results of similar phenomenological studies of DPS effects in the case of associated open charm and bottom $pp \rightarrow D^0 B^+ X$ as well as double open bottom $pp \rightarrow B^+ B^+ X$ production.

2. A sketch of our approach

2.1. Single-parton scattering

In the k_T -factorization approach [7, 8], the SPS cross section for $pp \rightarrow Q\bar{Q}Q\bar{Q}X$ reaction can be written as

$$\begin{aligned} & d\sigma_{pp \rightarrow Q\bar{Q}Q\bar{Q}X} \\ &= \int dx_1 \frac{d^2 k_{1T}}{\pi} dx_2 \frac{d^2 k_{2T}}{\pi} \mathcal{F}_g(x_1, k_{1T}^2, \mu^2) \mathcal{F}_g(x_2, k_{2T}^2, \mu^2) d\hat{\sigma}_{gg \rightarrow Q\bar{Q}Q\bar{Q}}. \end{aligned} \quad (1)$$

In the formula above, $\mathcal{F}_g(x, k_T^2, \mu^2)$ is the unintegrated gluon distribution function (uGDF). The uGDF depends on longitudinal momentum fraction x , transverse momentum squared k_T^2 of the gluons initiating the hard process, and also on a factorization scale μ^2 . The elementary cross section in Eq. (1) can be calculated with the help of off-shell matrix element that takes into account that both gluons entering the hard process has virtualities $k_1^2 = -k_{1T}^2$ and $k_2^2 = -k_{2T}^2$. We limit the numerical calculations to the dominant at high energies gluon–gluon fusion channel for the $2 \rightarrow 4$ mechanism under consideration.

The off-shell matrix elements for higher final-state parton multiplicities are available, *e.g.* through numerical methods based on the BCFW recursion [9]. Here, we use the **KaTie** code [10], which is a complete Monte Carlo parton-level event generator for hadron scattering processes, for any initial partonic state with on-shell or off-shell partons.

In the numerical calculation, we use $\mu^2 = \sum_{i=1}^4 m_{iT}^2/4$ as the renormalization/factorization scale, where m_{iT} s are the transverse masses of the outgoing heavy quarks. We take running α_s at next-to-leading order (NLO), charm quark mass $m_c = 1.5$ GeV and bottom quark mass $m_b = 4.75$ GeV. We use the Kimber–Martin–Ryskin (KMR) [11] unintegrated distributions for gluon calculated from the MMHT2014nlo PDFs [12]. The effects of the $c \rightarrow D^0$ and $b \rightarrow B^+$ hadronization are taken into account via the scale-independent Peterson model of fragmentation function (FF) [13] with $\varepsilon_c = 0.05$ and $\varepsilon_b = 0.004$.

2.2. Double-parton scattering

A textbook form of multiple-parton scattering theory (see *e.g.* Ref. [14]) is rather well-established, however, not yet applicable for phenomenological studies. Generally, the DPS cross sections can be calculated with the help of the double parton distribution functions (dPDFs). Unfortunately, the currently available models of the dPDFs are still rather at a preliminary stage. So far, they are formulated only for gluon or for valence quarks and only in a leading-order framework.

Instead of the general form, one usually follows the so-called factorized Ansatz, where the dPDFs are taken in the factorized form

$$D_{1,2}(x_1, x_2, \mu) = f_1(x_1, \mu) f_2(x_2, \mu) \theta(1 - x_1 - x_2). \quad (2)$$

Here, $D_{1,2}(x_1, x_2, \mu)$ is the dPDF and $f_i(x_i, \mu)$ are the standard single PDFs for the two generic partons in the same proton. The factor $\theta(1 - x_1 - x_2)$ ensures that the sum of the two parton momenta does not exceed 1.

The differential cross section for $pp \rightarrow Q\bar{Q}Q\bar{Q}X$ reaction within the DPS mechanism can be then expressed as follows:

$$\frac{d\sigma^{\text{DPS}}(Q\bar{Q}Q\bar{Q})}{d\xi_1 d\xi_2} = \frac{m}{\sigma_{\text{eff}}} \frac{d\sigma^{\text{SPS}}(gg \rightarrow Q\bar{Q})}{d\xi_1} \frac{\sigma^{\text{SPS}}(gg \rightarrow Q\bar{Q})}{d\xi_2}, \quad (3)$$

where ξ_1 and ξ_2 stand for generic phase-space kinematical variables for the first and second scattering, respectively. The combinatorial factor m is equal 1 for $c\bar{c}b\bar{b}$ and 0.5 for $b\bar{b}b\bar{b}$ case. When integrating over kinematical variables, one recovers the commonly used pocket-formula.

The effective cross section σ_{eff} provides normalization of the DPS cross section and is usually interpreted as a measure of the transverse correlation of the two partons inside the hadrons. The longitudinal parton-parton correlations are expected to be far less important when the energy of the collision is increased. For small- x partons and for low and intermediate scales, the possible longitudinal correlations can be safely neglected (see *e.g.* Ref. [15]). In this paper, we use world-average value of $\sigma_{\text{eff}} = 15$ mb provided by several experiments at different energies (see *e.g.* Ref. [2] for a review).

In our present analysis, cross sections for each step of the DPS mechanism are calculated in the k_T -factorization approach. The numerical calculations of the DPS are also done within the KaTie code. Here, the strong coupling constant α_s and uGDFs are taken the same as in the case of the calculation of the SPS mechanism. The factorization and renormalization scales for the two single scatterings are $\mu^2 = \frac{m_{1T}^2 + m_{2T}^2}{2}$ for the first, and $\mu^2 = \frac{m_{3T}^2 + m_{4T}^2}{2}$ for the second subprocess.

3. Numerical results

We start this section with presentation of results for inclusive production of $D^0 B^+$ pairs. This mode has the most advantageous $cb \rightarrow DB$ fragmentation probability and leads to the biggest cross sections. In Fig. 1, we show the transverse momentum distribution of D^0 (left panel) and B^+ (right panel) meson at $\sqrt{s} = 13$ TeV for the case of simultaneous $D^0 B^+$ -pair production in the LHCb fiducial volume defined as $2 < y < 4$ and $3 < p_T < 12$ GeV for both mesons. The SPS (dotted lines) and the DPS (dashed lines) components are shown separately, together with their sum (solid lines). The DPS component leads to an evident enhancement of the cross section, at the level of order of magnitude, in the whole considered kinematical domain. We predict that the $D^0 B^+$ data sample, that could be collected with the LHCb detector, should be DPS dominated in the pretty much the same way as in the case of double charm production (see *e.g.* Ref. [4]).

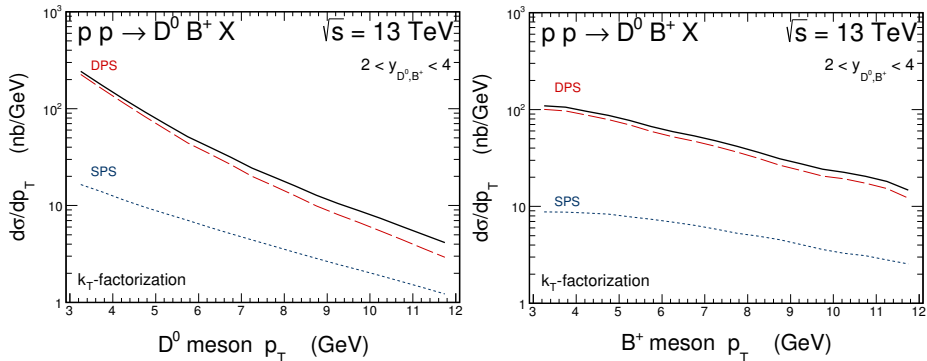


Fig. 1. Transverse momentum distribution of D^0 (left) and B^+ (right) meson at $\sqrt{s} = 13$ TeV for the case of inclusive $D^0 B^+$ -pair production in the LHCb fiducial volume. The SPS (dotted) and the DPS (dashed) components are shown separately. The solid lines correspond to the sum of the two mechanisms under consideration. The results are obtained within the k_T -factorization approach with the KMR uPDFs.

In Fig. 2, we present correlations observables that could be helpful in experimental identification of the predicted DPS effects. The characteristics of the di-meson invariant mass $M_{D^0 B^+}$ (left panel) as well as of the azimuthal angle $\varphi_{D^0 B^+}$ (right panel) differential distributions is clearly determined by the large contribution of the DPS mechanism.

The predictions for $B^+ B^+$ meson–meson pair production for the LHCb experiment leads to similar conclusions as those presented above. The predicted absolute normalization of the cross section and relative contribution of the DPS are only a bit smaller than in the $D^0 B^+$ case.

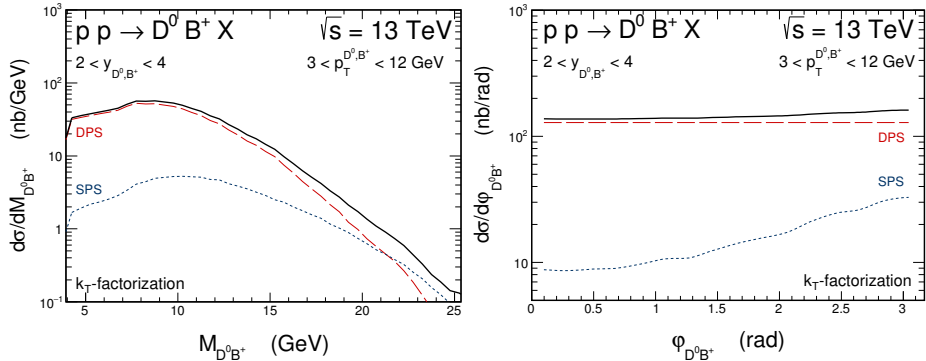


Fig. 2. The same as in Fig. 1 but for the $D^0 B^+$ -pair invariant mass (left) and azimuthal angle $\varphi_{D^0 B^+}$ (right) distributions.

To summarize the situation for the LHCb experiment, in Table I, we collect the integrated cross sections for $D^0 B^+$ and $B^+ B^+$ meson-meson pair production in nanobarns within the relevant acceptance: $2 < y_{D^0, B^+} < 4$ and $3 < p_T^{D^0, B^+} < 12$ GeV. We predict quite large cross sections, in particular, at $\sqrt{s} = 7$ TeV, the calculated cross section for $D^0 B^+$ -pair production is only 5 times smaller than the cross section already measured by the LHCb for $D^0 \bar{D}^0$ final state [17]. The cross sections for $B^+ B^+$ are order of magnitude smaller than in the mixed charm-bottom mode, however, still seem to be measurable. In both cases, the DPS component is the dominant one. The relative DPS contribution for both energies and for both experimental modes is at the very high level of 90%. This makes the possible measurements very interesting for the multi-parton interaction community.

TABLE I

The integrated cross sections for $D^0 B^+$ and $B^+ B^+$ meson-meson pair production (in nb) within the LHCb acceptance: $2 < y_{D^0, B^+} < 4$ and $3 < p_T^{D^0, B^+} < 12$ GeV, calculated in the k_T -factorization approach. The numbers include the charge conjugate states.

Final state	Mechanism	$\sqrt{s} = 7$ TeV	$\sqrt{s} = 13$ TeV
$D^0 B^+ + \bar{D}^0 B^-$	DPS	115.50	418.79
	SPS	21.13	51.46
$B^+ B^+ + B^- B^-$	DPS	11.04	43.40
	SPS	1.31	3.39

4. Conclusions

In the present studies, we have carefully examined production of charm-bottom and bottom-bottom meson-meson pairs. It was our aim to under-

stand the interplay of single- and double-parton scattering processes. The SPS results were obtained with the help of the KaTie code what allows for calculations based on k_T -factorisation approach. The DPS calculations have been done within the standard so far factorized Ansatz with two independent partonic scatterings. The so-called σ_{eff} parameter has been fixed at the same values as used in our previous studies for double charm production. We have considered several differential distributions for charmed and bottom mesons. The DPS mechanism has been shown to dominate for small invariant masses of the DB and BB systems. In both cases, we have predicted only a small correlation in relative azimuthal angle, typical for DPS dominance.

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