TENSOR GLUEBALL IN A TOP–DOWN HOLOGRAPHIC APPROACH TO QCD*

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Properties of the tensor glueball are discussed in the Witten–Sakai– Sugimoto Model, a top–down holographic approach to the non-perturbative region of Quantum Chromodynamics (QCD).

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1. Introduction

The existence of glueballs — bound states of gluons, the gauge bosons of Quantum Chromodynamics — is naturally expected due to the non-Abelian nature of the theory [1]. As a matter of principle, glueballs can possess various quantum numbers the most important of which are the total spin J, parity P and charge conjugation C. In practice, however, their experimental identification is often problematic given the possible overlap with quark bound states carrying the same quantum numbers [2]. Nonetheless, simulations in lattice QCD suggest the existence of a glueball spectrum [3].

Glueballs are noteworthy for at least two reasons. The Brout–Englert– Higgs mechanism, responsible for non-vanishing current quark masses, plays no role in the mass generation of glueballs that is a consequence of only the strong interaction. Additionally, glueballs possess integer spin and are thus classified as mesons whose spectrum without glueballs would be incomplete.

According to lattice-QCD simulations, the lightest tensor glueball has a mass between 2.3 GeV and 2.6 GeV [3]. Listings of the Particle Data Group (PDG [4]) contain four tensor states around 2 GeV termed as established: $f_2(1950), f_2(2010), f_2(2300)$ and $f_2(2340)$; several other states require confirmation, such as a narrow $f_J(2220)$ state that may have spin two or four. Tensor states have been subject of various low-energy effective approaches [5] but a tensor glueball has still not been clearly identified.

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In this article, a different approach is described: properties of the tensor glueball are examined by means of holographic QCD. The core of the study is the so-called AdS/CFT correspondence — the conjectured duality between supergravity theory (the weak-coupling limit of string theory) in an antide Sitter (AdS) space and a strongly coupled conformal field theory (CFT) in one dimension less. The full space of the supergravity theory contains a compact component (*n*-sphere S^n) such that the total number of dimensions equals 10 or 11, depending on whether string theory or M-theory is used. As an example, the original form of the correspondence entailed the equivalence between the supergravity limit of type-IIB string theory, containing fermions of the same chirality, on an AdS₅ × S^5 space and the large- N_c limit of an $\mathcal{N} = 4$ supersymmetric and conformal U(N_c) gauge theory on a 4-dimensional boundary of the AdS₅ space [6], where \mathcal{N} represents the number of the supersymmetry generators.

An application of the correspondence to QCD is only possible once the supersymmetry and the conformal symmetry are removed from the gauge theory and, in Ref. [7], Witten proposed a way to this goal in the 11-dimensional M-theory where, in the low-energy limit (supergravity with an $AdS_7 \times S^4$ background), the undesired symmetries are broken by suitable circle compactifications. Then, a pure Yang–Mills theory is obtained with the supergravity limit requiring a finite radius for the supersymmetrybreaking circle (the inverse radius determines the value of the so-called Kaluza–Klein mass $M_{\rm KK}$), and also a large 't Hooft coupling. Thus constructed holographic approaches to QCD derived directly from the string theory are referred to as *top–down* models [8,9]. An example is the Witten– Sakai–Sugimoto (WSS) Model; its implications for the tensor glueball presented here are based on the detailed discussions in Ref. [10].

2. The Witten–Sakai–Sugimoto Model and its implications for tensor glueballs

Witten's model contained no chiral quarks; in Ref. [9], a method for their inclusion was proposed by introducing N_f (number of flavours) probe D8- and anti-D8-branes [inducing $U(N_f) \times U(N_f)$ chiral symmetry] that extend along all dimensions of the supergravity space except for a (Kaluza– Klein) circle. In the simplest case, the branes and antibranes are located antipodally with regard to the circle; however, they merge at a certain point in the bulk space reducing the original $U(N_f) \times U(N_f)$ symmetry to its diagonal subgroup which is interpreted as a realisation of chiral-symmetry breaking. Up to a Chern–Simons term, the action for D8-branes reads

$$S_{\rm D8} = -T_{\rm D8} \operatorname{Tr} \int d^9 x e^{-\Phi} \sqrt{-\det\left(\tilde{g}_{MN} + 2\pi\alpha' F_{MN}\right)},\tag{1}$$

where $T_{\rm D8} = (2\pi)^{-8} l_{\rm s}^{-9}$ (and $l_{\rm s}^2 = \alpha'$, with $l_{\rm s}$ the string length), trace is taken with respect to flavour, g_{MN} is the metric of the D-brane world volume, Φ is the dilaton field and F_{MN} a field strength tensor whose components are, upon dimensional reduction, identified as meson fields of interest. Since no backreaction of the Witten-model background to D8-branes is considered, N_f is fixed and significantly smaller [9] than the number of colours (large- N_c limit).

The action of Eq. (1) can be expanded up to the second order in fields

$$S_{\rm D8}^{(2)} = -\kappa \,\mathrm{Tr} \int d^4x \int_{-\infty}^{\infty} dZ \left[\frac{1}{2} \,K^{-\frac{1}{3}} \eta^{\mu\rho} \eta^{\nu\sigma} F_{\mu\nu} F_{\rho\sigma} + M_{\rm KK}^2 \eta^{\mu\nu} F_{\mu Z} F_{\nu Z} \right] \,, \quad (2)$$

where $\kappa = \lambda N_c/(216\pi^3)$ [10], $\lambda = g_{\rm YM}^2 N_c$ is the 't Hooft coupling (and $g_{\rm YM}$ the 4-dimensional coupling), Z is essentially the holographic radial coordinate (and $K = 1 + Z^2$) and $\eta^{\mu\nu}$ is the flat metric diag(-, +, +, +). There are two undetermined quantities: $M_{\rm KK}$, that sets the model scale, and the coupling λ . They are usually calculated such that the mass of the rho meson and the pion decay constant correspond to their physical values leading to $M_{\rm KK} = 949$ MeV and $\lambda = 16.63$. Alternative determinations of λ and $M_{\rm KK}$ shift values of decay widths but do not alter overall conclusions regarding glueballs [10].

Masses and decay widths of the scalar glueball and its first excitation in the WSS Model have been extensively studied in Ref. [10] (see also Ref. [11]). Although the mixing patterns of $\bar{q}q$ and glueball states in the spectrum of f_0 resonances still bear many uncertainties [12], there are indications that the glueball ground state might be dominantly unmixed [13]; the analysis of Ref. [10] then prefers the $f_0(1710)$ resonance as a main candidate for the scalar glueball. This result, obtained in the chiral limit, is supported by the estimated consequences of finite pseudoscalar masses on the scalar-glueball decay [14], motivating exploration of the spin-two glueball in the model.

2.1. Mass and decays of the tensor glueball in the Witten-Sakai-Sugimoto Model

Once $M_{\rm KK}$ is known, the WSS Model predicts the tensor-glueball mass to be $M_{\rm T} = 1487$ MeV [the mass is the same as that of the dilaton glueball, preferentially identified as $f_0(1710)$ in Ref. [10], since the tensor and this scalar mode are associated with the same multiplet on the gravity side of the correspondence].

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The interaction Lagrangian containing the tensor glueball and pions is [10]

$$\mathcal{L} = \frac{1}{2} t_1 \operatorname{Tr}(T^{\mu\nu} \partial_{\mu} \pi \partial_{\nu} \pi), \qquad (3)$$

where the trace is over isospin and $t_1 = 42.195/(\sqrt{\lambda}N_c M_{\rm KK})$ [10]. The ensuing decay width reads (pions are massless [10])

$$\Gamma_{T \to \pi\pi} = \frac{1}{640\pi} t_1^2 M_{\rm T}^3 \,, \tag{4}$$

i.e., $\Gamma_{T\to\pi\pi} = 22$ MeV. Thus, the holographic tensor glueball appears to be quite narrow in the chiral limit.

It needs to be noted, however, that the result of Eq. (4) comes about with a tensor mass markedly lower than the lattice-QCD result of (2.3–2.6) GeV, discussed in Sec. 1. Additionally, $M_{\rm T} = 1487$ is below the 2ρ threshold whose opening can entail a significant contribution of the 4π decay channel to the total decay width of the tensor glueball. Therefore, a comparison with experimental data seems only justified if the tensor mass is extrapolated to the interval suggested by lattice QCD. (One also needs to keep in mind that, on the gravity side of the correspondence, α' corrections might conceivably shift the value of $M_{\rm T}$ towards the lattice-QCD result.)

The expectation is that in the holographic setup the tensor glueball does not couple to a pseudoscalar mass term. In that case, non-vanishing pseudoscalar masses would only have a kinematic effect in $\Gamma_{T\to\pi\pi}$. Then, in addition to raising $M_{\rm T}$, the tensor decay width can be recalculated with $m_{\pi} \neq 0$. It is even possible to estimate the decay widths into kaons and eta from $\Gamma_{T\to\pi\pi}$ by using flavour-symmetry factors 4:3 and 1:3, respectively, and also physical kaon and eta masses.

Calculation of the $T \to 4\pi$ decay width is significantly more complicated and involves integration over four-body phase space of massless final states with one or two vector propagators, depending on the interaction terms (that are all presented in Ref. [10] where calculation details can be found). Analogously to the calculation of 2K and 2η decay widths, it is also possible to estimate $\Gamma_{T\to\omega\omega\to6\pi}$ and $\Gamma_{T\to\phi\phi}$. All results are presented in Table I where an exemplary (lattice-compatible) value of $M_{\rm T} = 2400$ MeV is considered.

The holographic tensor glueball at $M_{\rm T} = 2400$ MeV is not narrow: quite contrarily, the WSS Model suggests this state to be very broad (approximately 700 MeV), with 4π as the most dominant decay channel contributing to more than half of the full decay width. Thus, if the tensor glueball is largely unmixed and located above 2 GeV, it may be difficult to ascertain in the experimental data. However, it is important to emphasise that the tensor decay width is strongly dependent on $M_{\rm T}$: should a (largely unmixed) tensor glueball have, *e.g.*, a mass $M_{\rm T} = 2000$ MeV then the full decay width

TABLE I

Decay	Width [MeV]
$T\to\rho\rho\to 4\pi$	382
$T\to\omega\omega\to 6\pi$	127
$T\to\phi\phi$	127
$T \to \pi\pi$	34
$T \to KK$	29
$T \to \eta \eta$	6
Total	705

Tensor decay widths for $M_{\rm T} = 2400$ MeV and other particle masses at their respective physical values. Uncertainty estimate: all values increase by $\simeq 30\%$ when an alternative method to determine λ and $M_{\rm KK}$ is considered [10].

 $\Gamma_{\rm T} = 320$ MeV is predicted [10]. Such a resonance would most certainly be more amenable to experimental analyses; indeed, in this case, the $f_2(1950)$ resonance [4], with a full decay width $\Gamma_{f_2(1950)} = (472 \pm 18)$ MeV, would be compatible with the holographic result.

3. Summary and outlook

A holographic top-down approach to non-perturbative QCD — the Witten–Sakai–Sugimoto Model — has been presented and its implications in the 2^{++} glueball channel have been discussed. Once the model coupling and scale have been determined, tensor decay widths at masses close to or above 2 GeV can be calculated. The full tensor decay width is dominated by the 4π channel above the 2ρ threshold. If the physical tensor glueball is located at 2 GeV, then the holographic decay width is compatible with that of the $f_2(1950)$ resonance; however, if the physical 2^{++} glueball is closer to 2.4 GeV, then the holographic result suggests it to be very broad (approximately 700 MeV). Notably, the identification of the tensor glueball is also hindered by uncertainties in the data [4] whose removal — *e.g.*, with measurements by the PANDA Collaboration at FAIR [15] — would facilitate the glueball search.

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