

# NERNST COEFFICIENT IN HIGH- $T_c$ SUPERCONDUCTORS: THE ROLE OF SUPERCONDUCTING FLUCTUATIONS\*

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In hole-doped high- $T_c$  cuprates, the Nernst coefficient ( $\nu$ ) as well as the magnetoresistance ( $\Delta\rho/\rho$ ) increase drastically below the pseudo-gap temperature,  $T^*$ . This unexpected result attracts much attention in that it reflects the fundamental feature of the electronic state in the pseudo-gap region, which has been a central issue on high- $T_c$  cuprates. In this article, we study these transport phenomena in terms of the fluctuation-exchange (FLEX)+ $T$ -matrix approximation. We focus on the role of the vertex corrections (VC's) which are necessary to keep the conservation laws, and find that both  $\nu$  and  $\Delta\rho/\rho$  are strongly enhanced by the VC's due to the antiferromagnetic (AF) and the superconducting (SC) fluctuations. In conclusion, the pseudo-gap region in high- $T_c$  cuprates is well described by the AF and SC fluctuation scenario based on the Fermi liquid theory.

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## 1. Introduction

For years, various striking anomalous transport phenomena have been a central issue on high- $T_c$  cuprates. Recently, it is found that the Nernst coefficient ( $\nu$ ) in hole-doped compounds increases drastically below the pseudo-gap temperature,  $T^*$  [1]. Here, we study this mysterious behavior of  $\nu$  in terms of the FLEX+ $T$ -matrix approximation. In this theory, the  $d$ -wave SC fluctuations, which are mediated by the antiferromagnetic (AF) fluctuations, become dominant below  $T^*$ . In the present article, we analyze the role of the VC's for currents in the framework of the conserving approximation, and calculate various transport coefficients for high- $T_c$  cuprates.

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## 2. FLEX+ $T$ -matrix approximation

In the self-consistent FLEX+ $T$ -matrix approximation, the full Green function and the self-energy are given by

$$G_{\mathbf{k}}(\epsilon_n) = (i\epsilon_n + \mu - \epsilon_{\mathbf{k}}^0 - \Sigma_{\mathbf{k}}(\epsilon_n))^{-1}, \quad (1)$$

$$\Sigma_{\mathbf{k}}(\epsilon_n) = \Sigma_{\mathbf{k}}^{\text{FLEX}}(\epsilon_n) + \Sigma_{\mathbf{k}}^{\text{SCF}}(\epsilon_n), \quad (2)$$

where  $\Sigma^{\text{FLEX}}$  is given by the diagrams for the FLEX approximation, and  $\Sigma^{\text{SCF}}$  is given by the  $T$ -matrix approximation. Namely, the former and the latter are given by the one-loop approximation in terms of the AF and  $d$ -SC fluctuations, respectively.  $\epsilon_{\mathbf{k}}^0$  is the tight binding dispersion of a non-interacting electron, and  $\epsilon_n$  is a Matsubara frequency for fermion.  $\Sigma_{\mathbf{k}}^{\text{FLEX}}(\epsilon_n)$  and  $\Sigma_{\mathbf{k}}(\epsilon_n)$  are caused by the AF and SC fluctuations, respectively. The formalism for the FLEX+ $T$ -matrix approximation is explained in Ref. [2] in detail.

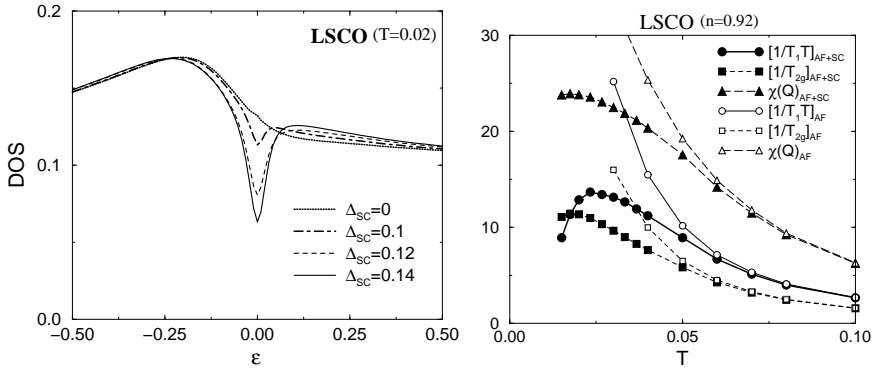


Fig. 1. DOS,  $\chi_Q$ ,  $1/T_1T$  and  $1/T_{2g}$  studied by the FLEX+ $T$ -matrix approximation (AF+SC). Results by the FLEX approximation (AF) is also shown.  $T = 0.1$  corresponds to 500K.

In the present numerical study for the Hubbard model, we put  $U = 4.5$  and  $(t, t', t'') = (-1, 0.15, -0.05)$  for  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  (LSCO). where  $t, t', t''$  are the nearest, the next-nearest and the third-nearest neighbor hoppings, respectively. Figure 1 shows the obtained density of state (DOS),  $\rho(\epsilon) = \sum_{\mathbf{k}} \text{Im}G_{\mathbf{k}}(\epsilon - i\delta)/\pi$ : The pseudo-gap opens around  $\epsilon = 0$  as the SC fluctuations grow, *i.e.*, as  $\Delta_{\text{SC}}$  increases. Figure 1 also shows the staggered susceptibility ( $\chi_Q$ ) and the nuclear relaxation rates ( $1/T_1T$ ,  $1/T_{2g}$ ). As for  $1/T_1T$ , the pseudo-gap behavior is recognized below  $T^* \approx 0.03$ , which cannot be reproduced by the FLEX approximation.

### 3. Transport phenomena

Next, we calculate various transport coefficients by using the FLEX+ $T$ -matrix approximation, in the framework of the conserving approximation. We calculate the VC's for electron current and the heat one self-consistently, by including all the Maki–Thompson-type diagrams given by both AF and SC fluctuations. The method of calculating the VC's is explained in Ref. [2] and Ref. [3] in detail.

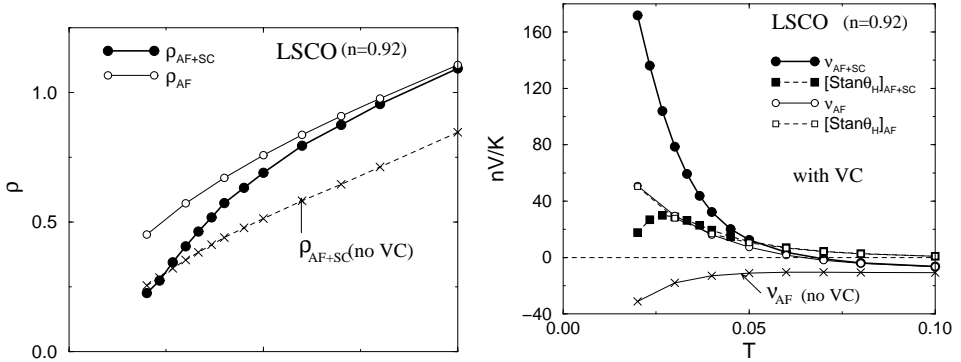


Fig. 2.  $\rho$ ,  $\nu$  and  $S \tan \theta_H$  given by the FLEX+ $T$ -matrix approximation (AF+SC) for LSCO.

Figure 2 shows the obtained results for LSCO; the resistivity  $\rho$ , the Nernst coefficient ( $\nu$ ) and  $S \tan \theta_H \equiv S \sigma_{xy} / \sigma$  ( $S$  being the thermoelectric power). As for the resistivity,  $\rho_{AF+SC}$  shows a  $T^2$ -like behavior at lower temperatures in the pseudo-gap region, which is observed in some hole-doped compounds. Next, we discuss the drastic enhancement of the Nernst coefficient below  $T^*$ , which is much mysterious and intriguing phenomenon in the pseudo-gap region. In Fig. 2,  $\nu_{AF+SC}$  starts to increase drastically below  $T^*$ , and its magnitude is consistent with experimental values [1]. In contrast,  $S \tan \theta_H$  decreases at lower temperatures, reflecting the suppression of the AF fluctuations below  $T^*$ .

On the other hand,  $\nu$  in the electron-doped compound (NCCO) is positive and very large below the room temperatures. As shown in Fig. 3, the present study is also able to reproduce this behavior successfully.

We note that other transport quantities like the Hall coefficient, the magnetoresistance, and the thermoelectric power show anomalous temperature and doping dependences in high- $T_c$  cuprates. They are well reproduced by the present study based on the FLEX+ $T$ -matrix approximation [2–5].

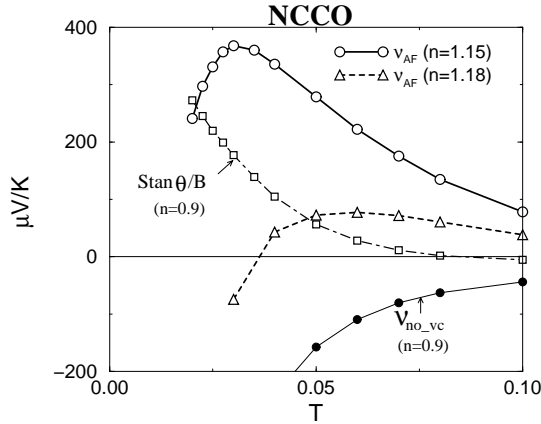


Fig. 3.  $\nu$  and  $S \tan \theta_H$  given by the FLEX approximation for NCCO

#### 4. Summary

In summary, we studied the electronic properties and the transport phenomena in the pseudo-gap region using the FLEX+T-matrix approximation. Below  $T^*$  in hole-doped compounds, the Nernst coefficient increase drastically. In the present study, we could reproduce the characteristic behaviors of all the coefficients satisfactorily. Especially, the drastic increases of  $\nu$  and  $\Delta\rho/\rho$  are naturally explained as the quasiparticle origin, by taking the VC's due to the AF and SC fluctuations correctly. As a result, the present study gives the concrete evidence that the pseudo-gap region in high- $T_c$  cuprates is well described as the Fermi liquid with strong AF and SC fluctuations.

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